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STATISTICAL METHODS

WITH SPECIAL REFERENCE TO

BIOLOGICAL VARIATION.

BY

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FIRST EDITION.

FIRST THOUSAND.

NEW YORK:

JOHN WILEY & SONS.

LONDON: CHAPMAN & HALL, LIMITED.

1899.

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PRÉFACE.

This book has been issued in answer to a repeated call for a simple presentation of the newer statistical methods in their application to biology. The immediate need which has called it forth is that of a handbook containing the working formulæ for use at summer laboratories where material for variation-study abounds. In order that the book should not be too bulky the text has been condensed as much as is consistent with clearness.

This book was already in rough draft when the work of Duncker appeared in Roux's Archiv. I have made much use of Duncker's paper, especially in Chapter IV. I am indebted to Dr. Frederick H. Safford, Assistant Professor of Mathematics at the University of Cincinnati and formerly Instructor at Harvard University, for kindly reading the proofs and for valuable advice. To Messrs, Keuffel and Esser, of New York, I am indebted for the use of the electrotypes of Figures 1 and 2. Finally, I cannot fail to acknowledge the cordial cooperation which the publishers have given in making the book serviceable.

C. B. DAVENPORT.

BIOLOGICAL LABORATORY OF THE BROOKLYN INSTITUTE, COLD SPRING HARBOR, LONG ISLAND, June 29, 1899.





ERRATA.

Page 18, bottom. Denominator of last term in equation for y should read

$$e^{x^2/2\sigma^2}$$
.

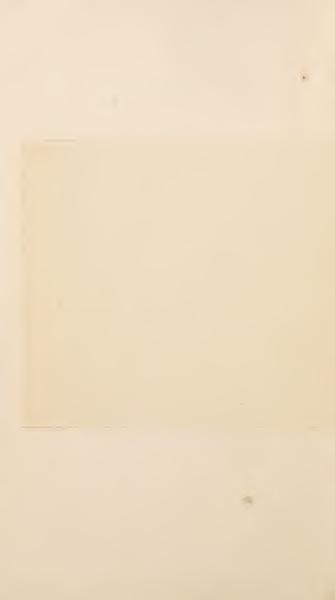
Page 23, 9th line. Denominator of last term in equation for y₀ should read

$$\Gamma(m_1+1)\Gamma(m_2+1).$$

" Tth line from bottom. Denominator of last term in equation for y_0 should read

$$\sqrt{\pi} T(m+1)$$
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STATISTICAL METHODS

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CHAPTER I.

ON METHODS OF MEASURING ORGANISMS.

Preliminary Definitions.

An *individual* is a segregated mass of living matter, capable of independent existence. Individuals are either simple or compound, *i.e.*, stocks and corms. In the case of a compound individual the morphological unit may be called a person.

A character is any quality common to a number of individuals.

The magnitude of a character is a quantitative expression of the character.

A variate is a single magnitude-determination of a character.

A class includes variates of the same or nearly the same magnitude.

Integral variates are magnitude-determinations of characters which from their nature are expressed in integers. Such magnitudes are determined by counting; e.g., the number of teeth in a porpoise.

Graduated variates are magnitude-determinations of characters which do not exist as integers and which may conse-

quently differ in different individuals by any degree of magnitude however small; e g., the stature of man.

Methods of Collecting Individuals for Measurement,

In collecting a lot of individuals for the study of the variability of any character undue selection must be avoided. The rule is:

Having settled upon the general conditions, of race, sex, locality, etc., which the individuals to be measured must fulfil, take the individuals methodically at random and without possible selection of individuals on the basis of the magnitude of the character to be measured. If the individuals are simply not consciously selected on the basis of magnitude of the character they will often be taken sufficiently at random.

Processes Preliminary to Measuring Characters.

Some characters can best be measured directly; e.g., the stature of a race of men. Often the character can be better studied by reproducing it on paper. The two principal methods of reproducing are by photography and by camera drawings.

For photographic reproductions the organs to be measured will be differently treated according as they are opaque or transparent. Opaque organs should be arranged if possible in large series on a suitable opaque or transparent background. The prints should be made on a rough paper so that they can be written on; blue-print paper is excellent. This method is applicable to hard parts which may be studied dry; e.g., mollusc shells, echinoderms, various large arthropods, epidermal markings of vertebrates and parts of the vertebrate skeleton. Shadow photographs may be made of the outlines of opaque objects, such as birds' bills, birds' eggs, and butterfly wings, by using parallel rays of light and interposing the object between the source of light * and the photo-

^{*} A Welsbach burner or an electric light are especially good. Minute

graphic paper. More or less transparent organs, such as leaves, petals, insect-wings, and appendages of the smaller Crustacea, may be reproduced either directly on blue-print paper or by "solar prints," either of natural size or greatly enlarged. For solar printing the objects should be mounted in series on glass plates. They may be fixed on the plate by means of balsam or albumen and mounted between plates either dry or in Canada balsam or other permanent mounting media. Wings of flies, orthoptera, neuroptera, etc., may be prepared for study in this way; twenty-five to one hundred sets of wings being photographed on one sheet of paper, say 16 × 20 inches in size. Microphotographs will sometimes be found serviceable in studying small organisms or organs, such as shells of Protozoa or cytological details.

Camera drawings are a convenient although slow method of reproducing on paper greatly enlarged outlines of microscopic characters, such as the form and markings of worms and lower Crustacea, sponge spicules, bristles, scales and scutes, plant-hairs, cells and other microscopic objects. In making such camera drawings a low-power objective, such as Zeiss A*, will often be found very useful.

The Determination of Integral Variates.— Methods of Counting.

While the counting of small numbers offers no special difficulty, the counting becomes more difficult with an increase of numbers. To count large numbers the general rule is to divide the field occupied by the numerous organs into many small fields each containing only a few organs. Counting under the microscope, e.g., the number of spines, scales or plant-hairs per square millimetre, may be aided by cross-hair rectangles in the eyepiece. The number of blood-corpuscles in a drop of blood, or of organisms in a cubic centimetre of water, have long been counted on glass slides ruled in small squares.

electric lamps such as are fed by a single cell give sharp shadows of small objects.

The Determination of Graduated Variates .-Methods of Measurement.

Straight lines on a plane surface are easily measured by means of a measuring-scale of some sort. The meas-



urement should always be metric because this is the universal scientific system. Various kinds of scales may be obtained of optical companies and hardware dealers,such as steel measuring-tapes, graduated to millimetres (about \$1.00), and steel rules (6 cm. to 15 cm.) graduated to 1 of a millimetre. Steel "spring-bow" dividers with milled-head screw are useful for getting distances which may be laid off on a scale. Tortuous lines, e.g., the contour of the serrated margin of a leaf or the outer margin of the wing of a sphinx moth, may be measured by a map-measurer ("Entfernungsmesser," Fig. 1), supplied at artist's and engineer's supply stores at about \$3.50.

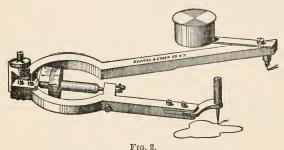
Distances through solid bodies or cavities are measured by calipers of some sort. Calipers for measuring diameters of solid bodies are made in various styles. Micrometer screw calipers ("speeded") reading to one-hundredths of a millimetre and sold by dealers in physical apparatus for

about \$5.00 are excellent for determining diameters of bones, birds' eggs, gastropod shells, etc. Leg calipers for rougher work can be obtained for from 30 cents to \$4.00. micrometer "caliper-square," available for inside or outside measurements and measuring to hundredths of a millimetre, is a useful instrument.*

The area of plane surfaces, as, e.g., of a wing or leaf, is easily determined by means of a sheet of colloidin scratched in millimetre squares. By rubbing in a little carmine the

^{*} Many of the instruments described in this section are made by the Starrett Co., Athol, Mass., and by Brown and Sharpe, Providence, tool cutters.

scratches may be made clearer. The number of squares covered by the surface is counted (fractional squares being mentally summated) and the required area is at once obtained. If the area has been traced on paper it may be measured by the planimeter (Fig. 2). This instrument may be obtained at



engineer's supply shops. It consists of two steel arms hinged together at one end; the other end of one arm is fixed by a pin into the paper, the end of the second arm is provided with a tracer. By merely tracing the periphery of the figure whose area is to be determined the area may be read off from a drum which moves with the second arm. This method is less wearisome than the method of counting squares.

The area of a curved surface, like that of the elvtra of a beetle or the shell of a clam, is not always easy to find. To get the area approximately, project the curved surface on a plane by making a camera drawing or photograph of its outline. By means of parallel lines divide the outline drawing into strips such that the corresponding parts of the curved surface are only slightly curved across the strips, but greatly curved lengthwise of the strips. Measure the length of each plane strip and divide the magnitude by the magnification of the drawing. Measure also, with a flexible scale, the length of the corresponding strip on the curved surface. Then, the area of any strip of the object is to the area of the projection as the length of the strip on the object is to the length of its projection. The sum of the areas of the strips will give the total area of the surface.

The form of a plane figure of irregular outline has been expressed qualitatively by botanists, who have invented a complicated nomenclature for the purpose; this is reproduced in part here.

Linear, more than thrice longer than wide and of nearly the same breadth throughout (Fig. 3).

Lanceolate, more than thrice longer than wide and tapering towards one or both ends (Fig. 4).

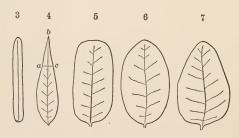
Oblong, twice to thrice as long as broad (Fig. 5).

Elliptical, of the shape of an ellipse with an eccentricity more than .5 (Fig. 6).

Oval, elliptical, with eccentricity from .5 to .1.

Orbicular, nearly circular, with eccentricity less than .1.

Orate, with the outline of a hen's egg, one end broader than the other (Fig. 7).



Figs. 3-7.

Cuneate or cuneiform, wedge-shaped.

Spatulate, rounded at one end, long and narrow at the other, like a spatula.

Acuminate, tapering to an angle of less than 15° (Fig. 8).

Acute, ending in an angle of from 15° to 90° (Fig. 9).

Obtuse, ending in an angle of over 90° (Fig. 10).

Truncate, terminating as though cut off (Fig. 11).

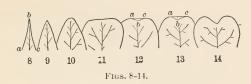
Retuse, with a re-entering obtuse end (Figs. 12–14).

Serrate, with small saw-like teeth (Fig. 15).

Dentate, with larger, more obtuse teeth (Fig. 16).

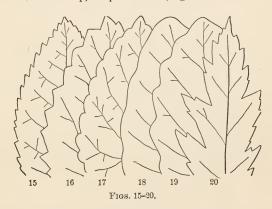
Crenate, rounded teeth (Fig. 17).

Repand, wavy margin, teeth broadly rounded, height less than breadth (Fig. 18).



Sinuate, still stronger waves, height equals or exceeds breadth (Fig. 19).

Incised, with sharp, deep incisions (Fig. 20).



The quantitative expression of variation in these forms can usually be easily obtained by using an index, or ratio of two dimensions.

Index of Linearness, greatest length greatest breadth

- " Lanceolateness, greatest length greatest breadth, also angle abc.
- " "Oblongness, $\frac{\text{greatest length}}{\text{greatest breadth}}$, also $\frac{\text{area}}{\text{breadth}}$
- " Ellipticity, (greatest lgth.)—(greatest brdth.) (greatest length)

for values from 1 to .50.

Index of Ovalness, (greatest length) — (greatest breadth)
(greatest length)

for values from .50 to .1.

" Orbicularness, (greatest diam.) - (greatest brdth.)
(greatest diameter)
for values from .1 to 0.

" Ovateness or obovateness, $\frac{\text{radius of curvature of }}{\text{radius of smaller end}}$.

" Cuneateness, $\frac{\text{diameter}}{\text{diameter}} \frac{\text{at } \frac{1}{3}}{\text{at } \frac{2}{3}}$, or angle abc (line a-c passing through middle of major diameter).

'' 'Spatulateness, length of radius of curve at broad end of organ transverse diameter of narrow part of organ

- " Acuminateness, angle abc at apex (Fig. 8).
- " Acuteness, angle abc at apex.
- " " Obtuseness, angle abc at apex and radius of curvature.
- " Truncatedness, angle abe at apex and radius of curvature.
- " Retuseness, $\frac{\text{cosine}}{2 \times \text{sine}}$ of $\frac{1}{2}$ angle abc.
- " Serrateness, number of teeth per linear unit of edge, average angle of tooth.
- " Dentateness, number of teeth, average angle of tooth,
- " "Crenateness, number of waves, average radius of curvature of waves.
- " Repandness, depth of waves average radius of curvature of waves.
- " Sinuateness, depth of waves, average radius of curvature of waves."
- " " Incisedness, depth of incision opening of incision."

Characters occupying three dimensions of space may be quantitatively expressed by volume. The volume of water or sand displaced may be used to measure volume in the case of solids. The volume of water or sand contained will measure a cavity. Irregular form is best measured by getting, either by means of photography or drawings, projections of the object on one or more of the three rectangular fundamental planes of the organ, and then measuring these plane figures as already described. Or two or more axes may be measured and their ratio found.

Characters having weight are easily measured; the only precautions being those observed by physicists and chemists.

Color Characters. Color may be qualitatively expressed by reference to named standard color samples. Such standard color samples are given in Ridgeway's book, "Nomenclature of Color," and also in a set of samples manufactured by the Milton Bradley Co., Springfield, Mass., costing 6 cents. The best way of designating a color character is by means of the color wheel, a cheap form of which (costing 6 cents) is made by the Milton Bradley Co. The colors of this "top" are standard and are of known wave-length as follows:

Red, 656 to 661 Green, 514 to 519 Orange, 606 to 611 Blue, 467 to 472 Yellow, 577 to 582 Violet, 419 to 424.

It is desirable to use Milton Bradley's color top as a standard. Any color character can be matched by using the elementary colors and white and black in certain proportions. The proportions are given in percents. In practice the fewest possible colors necessary to give the color character should be employed and two or three independent determinations of each should be made at different times and the results averaged. So far as my experience goes any color character is given by only one least combination of elementary colors. (See Science, July 16, 1897.)

When there is a complex color pattern the color of the different patches must be determined separately. In case of a close intermingling of colors, the colored area may be rapidly rotated on a turntable so that the colors blend and the result-

ant may then be compared with the color wheel. By this means also the total melanism or albinism, viridescence, etc., may be measured.

Marking-characters. The quantitative expression of markings or color patterns will often call for the greatest ingenuity of the naturalist. Only the most general rules can here be laid down. Study the markings comparatively in a large number of the individuals, reduce the pattern to its simplest elements, and find the law of the qualitative variation of these elements. The variation of the elements can usually be treated under one of the preceding categories. Find in how far the variation of the color pattern is due to the variation of some number or other magnitude, and express the variation in terms of that magnitude. Remember that it is rarely a question whether the variation of the character can be expressed quantitatively but rather what is the best method of expressing it quantitatively.

CHAPTER II.

ON THE SERIATION AND PLOTTING OF DATA AND THE FREQUENCY POLYGON.

The data obtained by measuring any character in a lot of individuals consists either of a mass of numbers for the character in each individual; or, perhaps, two numbers which are to be united to form a ratio; or, finally, a series of numbers such as are obtained by the color wheel, of the order: W 40%, N (Black) 38%, Y 12%, G 10%. The first operation is the simplification of data. Each variate must be represented by one number only. Consequently, quotients of ratios must be determined and that single color of a series of colors which shows most variability in the species must be selected, e.g., N.

The process of seriation, which comes next, consists of the grouping of similar magnitudes into the same magnitude class. The classes being arranged in order of magnitude, the number of variates occurring in each class is determined. The number of variates in the class determines the frequency of the class.

or the chass.

The method of seriation may be illustrated by two examples; one of integral variates, and the other of graduated variates.

Example 1. The magnitude of 21 integral variates are found to be as follows: 12, 14, 11, 13, 12, 12, 14, 13, 12, 11, 12, 12, 11, 12, 10, 11, 12, 13, 12, 13, 12, 12, 12. In scriation they are arranged as follows:

Classes: 10, 11, 12, 13, 14. Frequency: 1, 4, 11, 4, 2.

Example 2. In the more frequent case of graduated variates our magnitudes might be more as follows:

3.2	4.5	5.2	5.6	6.0
3.8	4.7	5.2	5.7	6,2
4.1	4.9	5.3	5.8	6.4
4.3	5.0	5.3	5.8	6.7
4.3	5.1	5,4	5.9	7.3

In this case it is clear that our magnitudes are not exact, but are merely approximations of the real (forever unknowable) value. The question

arises concerning the inclusiveness of a class—the class range. An approximate rule is: Make the classes only just large enough to have no or very few vacant classes in the series. Following this rule we get

	(3.0-3.4;	3.5-3.9;	4.0-4.4;	4.5-4.9;	5.0-5.4;
Classes	3.2	3.7	4.2	4.7	5.2
	(1	2	3	4	5
Frequency	1	1	3	3	7
Classes	(5.5-5.9;	6.0-6.4;	6.5-6.9;	7.0-7.4;	
Classes	₹ 5.7	6.2	6.7	7.2	
	(6	7	8	9	
Frequency	5	3	1	1	

The classes are named from their middle value, or better, for ease of subsequent calculations, by a series of small integers (1 to 9).

In case the data show a tendency of the observer towards estimating to the nearest round number, like 5 or 10, each class should include one and only one of these round numbers.

As Fechner ('97) has pointed out, the frequency of the classes and all the data to be calculated from the series will vary according to the point at which we begin our seriation. Thus if, instead of beginning the series with 3.0 as in our example, we begin with 3.1 we get the series:

Classes	3.1-3.5;	3.6-4.0;	4.1-4.5;	4.6 - 5.0;	5.1-5.5
Classes	3.3	3.8	4.3	4.8	3,5
Frequency	1	1	4	3	6
Classes {	5.6-6.0;	6.1-6.5;	6.6-7.0;	7.1-7.5;	
Classes	5.8	6.3	6.8	7.3	
Frequency	6	2	1	1	

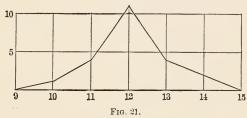
which is quite a different series. Fechner suggests the rule: Choose such a position of the classes as will give a most normal distribution of frequencies. According to this rule the first distribution proposed above is to be preferred to the second.

In order to give a more vivid picture of the frequency of the classes it is important to plot the frequency polygon. This is done on coordinate paper.*

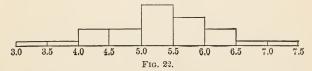
A different method should be adopted according as integral or graduated variates are under consideration. In the case of integral variates proceed as follows: At equal intervals along a horizontal line (axis of X) draw a series of (vertical) ordinates whose successive heights shall be proportional to the frequency of the classes. Join the tops of the ordinates. Thus for the example given, the curve will be as shown in Fig. 21. This method of drawing the frequency polygon is known as the method of leaded ordinates.

^{*} This paper may be obtained at any artists' supply store.

In the case of *graduated variates* proceed as follows: Lay off along a horizontal line equal contiguous spaces each of which shall represent one class, number the spaces in order



from left to right with the class magnitudes in succession, and erect upon these bases rectangles proportionate in height to the frequency of the respective classes (Fig. 22).



This method of drawing the frequency polygon is known as the **method** of **rectangles**. If the tops of the middle ordinates of successive contiguous rectangles be connected by an oblique line a polygon made up of **trapezia** is obtained. The outline of the polygon will be fairly close to that of a curve passing through the tops of the central ordinates of the rectangles.

CERTAIN CONSTANTS OF THE FREQUENCY POLYGON.

After the data have been gathered and arranged it is necessary to determine the law of distribution of the variates. To get at this law we must first determine certain constants.

The **mean** (M) is the abscissa of the centre of gravity of the variates or of the frequency polygon. It is found by the formula

$$M = \frac{\sum (V, f)}{n},$$

in which V is the magnitude of any class; f its frequency;

 Σ indicates that the sum of the products for all classes into frequency is to be got, and n is the number of variates.

Thus in the last example:

$$\begin{aligned} M &= (3.2 \times 1 + 3.7 \times 1 + 4.2 \times 3 + 4.7 \times 3 + 5.2 \times 7 + 5.7 \times 5 + 6.2 \times 3 \\ &+ 6.7 \times 1 + 7.2 \times 1) + 25 = 5.24, \\ \text{or} \\ M_1 &= (1 \times 1 + 2 \times 1 + 3 \times 3 + 4 \times 3 + 5 \times 7 + 6 \times 5 + 7 \times 3 + 8 \times 1 + 9 \times 1) + 25 = 5.08, \end{aligned}$$

 $M_1 = (1 \times 1 + 2 \times 1 + 3 \times 3 + 4 \times 3 + 5 \times 7 + 6 \times 5 + 7 \times 3 + 8 \times 1 + 9 \times 1) + 25 = 5.08,$ $M_1 = 5.2^* + .08(5.7 - 5.2) = 5.24$

A still shorter method of finding M is given on page 17.

The mode is the class with the greatest frequency.

In the example, the mode is 5.2.

The **median magnitude** is one above which and below which 50% of the variates occur. It is such a point on the axis of X of the frequency polygon that an ordinate drawn from it bisects the polygon of rectangles or the continuous curve, but not the polygon of loaded ordinates.

To find its position: Divide the variates into three lots: those less than the middle class, of which the total number is a; those of the middle class, b; and those greater, c. Then a+b+c=n= the total number of variates. Let l'= the lower limiting value of the middle class, and l''= the upper limiting value, and let x= the abscissal distance of the median ordinate above the lower limit or below the upper limit of the median class according as x is positive or negative. Then $\frac{1}{2}n-a$; b=x; l''-l' when x is positive, or $\frac{1}{2}n-c$; b=x: l''-l' when x is negative.

Thus in the last example: 12.5 - 8:7 = x:0.5; x = .32; the median magnitude = 5.0 + .32 = 5.32. Or 12.5 - 10:7 = -x:0.5; x = -.18; the median magnitude = 5.5 - .18 = 5.32. (Cf. p. 11.)

Every determination of a constant of the frequency polygon is an approximation only to the true value of the constant. The closeness of the approximation to the truth is measured by the so-called *probable error of the determination*. This is a pair of values lying one above and one below the value determined. We can say that there is an even chance that the true value lies between these limits; the chances are 4 to 1 that the true value lies within twice these limits, and 19 to 1 that it lies within thrice these limits.

The probable error of the mean is given by the formula

$$\pm$$
 0.6745 $\times \frac{\text{standard deviation [see below]}}{\sqrt{\text{number of variates}}} = \pm 0.6745 \frac{\sigma}{\sqrt{n}}$.

It will be seen that the probable error is less, that is, that the result is more accurate, the greater the number of variates

^{* 5.2} is the true class magnitude corresponding to the integer 5.

measured, but the accuracy does not increase in the same ratio as the number of individuals measured, but as the square root of the number. The probable error of the mean decreases as the standard deviation decreases.

The index of the variability, σ , of the variates when they group themselves about one mode is found by adding the products of the squared deviation-from-the-mean of each class multiplied by its frequency, dividing by the total number of variates, and extracting the square root of the quotient, thus:

$$\sigma = \sqrt{\frac{\text{sum of [(deviation of class from mean)}^2}{\text{x frequency of class]}}}$$

$$= \sqrt{\frac{\Sigma(x^2.f)}{n}}.$$

This measure is known as the standard deviation.

The probable error of the standard deviation is

$$\pm$$
 0.6745 $\frac{\text{standard deviation}}{\sqrt{2} \times \text{number of variates}} = \pm 0.6745 \frac{\sigma}{\sqrt{2n}}$.

Other Indices of Variation are the average deviation, or average departure, which is found thus:

$$A.D. = \frac{\text{sum of [deviations of class from mean} \times \text{frequency}]}{\text{number of variates}}.$$

The **probable error** is the distance from the mode of that ordinate which exactly bisects the half curve 0MX or $0MX^1$, Fig. 23; it is equal to $0.6745 \times \text{standard deviation} = 0.6745\sigma$. Neither of these last two indices of variation is as good as the standard deviation when n is rather small.

The standard deviation, like the other indices of variation, is a concrete number, being expressed in the same units as the magnitudes of the classes. The standard deviation of one lot of variates is consequently not comparable with the S. D. of variates measured in other units. It has been proposed to reduce the index of variation to a concrete number, independent of any particular unit, by dividing the index of variation of any variates by the mean; the quotient multiplied by 100 is called

the coefficient of variability. In a formula, $CV = \frac{\sigma}{M}$.

(Pearson, '96; Brewster, '97)

CHAPTER III.

THE CLASSES OF FREQUENCY POLYGONS.

The plotted curve may fall into one of the following classes:

A. Unimodal.

- I. Simple.
 - 1. Range unlimited in both directions:
 - a. Symmetrical. The normal curve.
 - b. Unsymmetrical (Pearson's Type IV).
 - 2. Range limited in one direction, together with skewness (Type III).
 - 3. Range limited in both directions:
 - a. Symmetrical, Type II.
 - b. Unsymmetrical, Type I.
- II. Complex.
- B. Multimodal.

The classification of any given curve is not always an easy task. Whether the curve is unimodal or multimodal can be told by inspection. Whether any unimodal curve is simple or complex cannot be told by any existing methods without great labor and uncertainty in the result.

Complex curves may be classified as follows:

- 1. Composed of two curves, whose modes are different but so near that the component curves blend into one; such curves are usually unsymmetrical.
- 2. The sum of two curves having the same mode but differing variability.
- 3. The difference of two curves having the same mode but differing variability.

If the material is believed to be homogeneous and the curve is unimodal it is probably simple and its classification may be carried further.

For classification the rule is as follows: Determine the mean of the magnitudes. Take a class near the mean (call it \mathcal{V}_m)

as a zero point; then the departure of all the other classes will be -1, -2, -3, etc., and +1, +2, +3, etc.

Add the products of all these departures multiplied by the frequency of the corresponding class and divide by n; call the quotient ν_1 .

Add the products of the squares of all the departures multiplied by the frequency of the corresponding class and divide by n; call the quotient ν_2 .

Add the products of the *cubes* of all the departures multiplied by the frequency of the corresponding class and divide by n; call the quotient ν_3 .

Add the products of the *fourth powers* of all the departures multiplied by the frequency of the corresponding class and divide by n; call the quotient ν_4 . Or,

$$u_1 = \frac{\sum (V - V_m)}{n} = \text{departure of } V_m \text{ from mean.} \quad V_m \text{ being known, } M \text{ may be found } [M = V_m + \nu_1]; *$$

$$\boldsymbol{\nu_2} = \frac{\sum (V - V_m)^2}{n};$$

$$\nu_{s} = \frac{\sum (V - V_{m})^{s}}{n};$$

$$\nu_{\bullet} = \frac{\Sigma (V - V_m)^4}{n}.$$

The values ν_1 , ν_2 , ν_3 , ν_4 , are called respectively the first, second, third, and fourth moments of the curve about V_m .

To get the moments of the curve about the mean, either of two methods (A or B) will be employed. Method A is used when integral variates are under consideration; method B when we deal with graduated variates.

(A) To find moments in case of integral variates:

$$\begin{array}{l} \mu_1 = 0; \\ \mu_2 = \nu_2 - \nu_1^2; \\ \mu_3 = \nu_3 - 3\nu_1\nu_2 + 2\nu_1^3; \\ \mu_4 = \nu_4 - 4\nu_1\nu_3 + 6\nu_1^2\nu_2 - 3\nu_1^4. \end{array}$$

(B) To find moments in case of graduated variates:

^{*} This is the short method of finding M referred to on page 14.

$$\begin{array}{l} \mu_1 = 0; \\ \mu_2 = \nu_2 - \nu_1^2 + \frac{1}{6}; \\ \mu_3 = \nu_3 - 3\nu_1\nu_2 + 2\nu_1^2; \\ \mu_4 = \nu_4 - 4\nu_1\nu_3 + 6\nu_1^2\nu_2 - 3\nu_1^4 + \nu_2 - \nu_1^2 + \frac{1}{15}. \end{array}$$
 Also,
$$\beta_1 = \frac{\mu_3^2}{\mu_2^3}, \ \beta_2 = \frac{\mu_4}{\mu_4^2}.$$

 $F = 6 + 3\beta_1 - 2\beta_2$ = the "critical function."

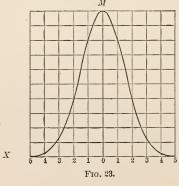
Now the classification of any empirical curve depends upon the value of its critical function, F.

When F is positive and $\begin{cases} \beta_1 > 0, \text{ curve is of Type I.} \\ \beta_1 = 0, \beta_2 < 3, \text{ curve is of Type II.} \end{cases}$ " F = 0 and $\begin{cases} \beta_1 > 0, \beta_2 > 3, \text{ curve is of Type III.} \\ \beta_1 = 0, \beta_2 = 3, \text{ curve is normal.} \end{cases}$

" F is negative and $\beta_1 > 0$, $\beta_2 > 3$, curve is of Type IV. An important relation to be referred to later is

$$s = \frac{6(\beta_2 - \beta_1 - 1)}{E},$$

in which s is an unknown, positive number.



The Normal Curve.

X

The **normal curve** is symmetrical about the mode; consequently the mode and the median and mean class coincide.

The mathematical formula of the normal curve, a formula which one does not have to understand in order to make use of it, is

$$y = \frac{\alpha}{\sigma \sqrt{2\pi}} \cdot \frac{1}{e^{x_2^2/\sigma^2}}.$$

This formula gives the value of any ordinate y (or any class) at any distance x (measured atong the base, X, X', of Fig. 23) from the mode. e is a constant number, 2.71828, the base of the Naperian system of logarithms. α is the total area of the curve or number of variates, and σ is the Standard Deviation, which is constant for any curve and measures the variability of the curve, or the steepness of its slope.

To compare any observed curve with the theoretical normal curve we can make use of tables. For the case of a polygon of integral variates the theoretical frequency of any class at a deviation $\frac{x}{\sigma}$ from the mean can be taken directly from Table III. Here x is the actual deviation from the mean expressed in the unit of the maximum, and σ is the standard deviation.

rectangles representing the relative frequency of the variates, Table IV gives the relation of the actual to the theoretical number of individuals occurring between the values $+\frac{x}{\sigma}$ and $-\frac{x}{\sigma}$. By looking up the given values of $\frac{x}{\sigma}$ the corresponding theoretical percentage of variates between the limits

For the case of a polygon of graduated variates built up of

 $+\frac{x}{\sigma}$ and $-\frac{x}{\sigma}$ will be found directly. The ratio $-\frac{x}{\sigma}$ may be called the *Index of Abmodality*.

The normal curve may preferably be employed even when β_1 is not exactly equal to 0, nor β_2 exactly equal to 3, nor F exactly equal to 0. Use the normal curve when

$$F \times \mu_2{}^3 < \pm 1$$
 and $\frac{3\nu_2{}^2-2\nu_1{}^4}{\nu_4}=1\,\pm\,.2$

To determine the closeness of fit of a theoretical polygon to the observed polygon. There are two methods according as the variates are (A) integral or (B) graduated.

(A) Find for each class the percentage which the difference between the theoretical value y and the observed frequency f is of the frequency, and find the average of these percentages, which is the index of closeness of fit sought.

(B) Subtract in order each theoretical value of y from the corresponding observed value, regarding signs. Call the difference δ_1 . Whenever in the successive values of δ_1 there is a change of sign, divide the product of these successive values of δ_1 , in pairs, by their sum. Call this value δ_2 ; make its sign always minus. Then the difference between the two polygons in per cent of one of them is given by the equation

$$\Delta\% = \frac{\Sigma \delta_1 + (-\delta_2)}{2n} 100,$$

where δ_1 is summated without regard to sign, and n equals the total number of variates. This is the method of Duncker, '98. It may be considered a sufficient agreement between

observation and calculation when $\Delta < \frac{100}{\sqrt{n}}$ %.

THE NORMAL CURVE OF FREQUENCY AS A BINOMIAL CURVE.

The normal curve may also be expressed by the binomial formula $(p+q)^l$, where $p=\frac{1}{2},q=\frac{1}{2}$, and l is the number of terms, less 1, in the expansion of the binomial; hence approximately the number of classes into which the magnitudes of the variates should fall. If the standard deviation be known, l may be found by the equation

$$l = 4 \times (\text{Standard Deviation})^2 = 4\sigma^2$$
.

Example of (nearly) normal curve. Number of spines in dorsal fin of Acerina cernua, L. (Duncker, '99, p. 177).

$$M = V_m + \nu_1 = 14 + 0.1568 = 14.1568.$$

$$\mu_2 = 0.3895 - 0.1568^2 = 0.3650.$$

 $\mu_3 = 0.2011 - 3 \times 0.1568 \times 0.3895 + 2 \times 0.1568^3 = 0.0257.$

 $\mu_4 = 0.5663 - 4 \times 0.1568 \times 0.2011 + 6 \times 0.1568^2 \times 0.3895 - 3 \times 0.1568^4 = 0.4929.$

$$\beta_1 = \frac{0.0257^2}{0.3650^3} = 0.01358; \quad \beta_2 = \frac{0.4929}{0.3650^2} = 3.6998.$$

$$F = 6 + .04074 - 7.3996 = -1.3589$$
, $F \cdot \mu_2^3 = 1.3589 \times 0.365^3 = .066$.

$$\frac{3\nu_2^2 - 2\nu_1^4}{\nu_4} = \frac{3 \times 0.3895^2 - 2 \times .1568^4}{0.5663} = .71. \qquad \sigma = \sqrt{\mu_2} = .6041.$$

Maximum frequency = $\frac{n}{\sigma \sqrt{2\pi}} = \frac{1900}{.6041 \times \sqrt{2\pi}} = 1255$.

Although somewhat more closely of Type IV (see page 18) than of the Normal Type, this example may be treated as Normal.

The difference between it and the normal is found below to be 1.39%.

To illustrate the method, and in accordance with Duncker's example, Δ is here, exceptionally, calculated by rule page 20.

$$\Delta = \frac{100(60.8 - 23.1)}{3800} = 0.99\%.$$

The values of y in the table above are calculated from the formula $y = y_0$. $e^{-x^2/2\sigma^2}$. The sum of the theoretical y values should equal the total number of variates.

OTHER UNIMODAL FREQUENCY POLYGONS.

The formulas of the remaining four types of unimodal simple frequency polygons have a family resemblance with the formula

$$y = y_{_0}e^{-\frac{x^2}{2\sigma^2}}$$

of the normal curve. They are as follows:

Curve of limited range on both sides:

Unsymmetrical,
$$y = y_0 \left(1 + \frac{x}{\alpha_1}\right)^{m_1} \left(1 - \frac{x}{\alpha_2}\right)^{m_2}$$
, Type I.

Symmetrical,
$$y = y_0 \left(1 - \frac{x^2}{a^2}\right)^m$$
, Type II.

Curve of range limited on one side:

Unsymmetrical,
$$y = y_0 \left(1 + \frac{x}{a}\right)^p e^{-x/d}$$
, Type III.

Curves of unlimited range on both sides:

Unsymmetrical, $y = y_0 \cos \theta^{2m} e^{-v\theta}$, where $\tan \theta = \frac{x}{a}$. Type IV.

[Symmetrical,
$$y = y_0 e^{-\frac{x^2}{2\sigma^2}}$$
, the normal curve.]

In these formulas:

 $y_0 = \text{modal ordinate}$, to be especially reckoned for each type.

y = the length of the ordinate (or area of rectangle) located at the distance x from y_0 .

a=a part of the abscissa-axis XX^{7} expressed in units of the classes.

e = the base of the Naperian system of logarithms, 2.71828.

Curves of limited range are theoretically different from the normal curve, which theoretically applies to cases where the classes have an infinite range above and below the mean. Such an infinite range is rare in biological statistics, although, as stated, the normal curve often fits observational curves very closely. The range in biological statistics may be limited at both extremes. Thus, the ratio of carapace length to total length of the lobster is limited between 0 and 1.

The range may be limited on one side only. Thus the ratio Antero-Post. Diam.

Dorso-Vent. Diam.

of a bivalve shell may conceivably range from 0 to

 ∞ . The forms of the molluscan genera Pinna (or Malleus) and Solen approach such extremes.

Asymmetry or skewness is found in Type I (of which Type II is the symmetrical limit), Type III and Type IV. In skew curves the mode and the mean are separated from each other by a certain distance, d. Asymmetry is measured by a factor

$$A = \frac{d}{\sigma} = \frac{1}{2} \sqrt{\beta_1} \frac{s \pm 2}{s \mp 2}$$
, where $s = \frac{6(\beta_2 - \beta_1 - 1)}{2\beta_2 - 3\beta_2 - 6}$;

the result has the same sign as µ3.

In Type I,
$$A = \frac{1}{2} \sqrt{\beta_1} \frac{s+2}{s-2}$$
.

" " III,
$$A = \frac{1}{2} \sqrt{\beta}$$
.

" " IV,
$$A = \frac{1}{2} \sqrt{\beta_1} \frac{s-2}{s+2}$$
.

To compare any observed frequency polygon of Type I with its corresponding theoretical curve.

$$y = y_0 \left(1 + \frac{x}{a_1}\right)^{m_1} \left(1 - \frac{x}{a_2}\right)^{m_2}$$

To find $a_1, a_2, m_1, m_2, !'_0$.

The total range, b, of the curve (along the abscissa axis) is found by the equation

$$b = \frac{\sigma}{2} \sqrt{\beta_1 (s+2)^2 + 16(s+1)} ;$$

 a_1 and a_2 are the ranges to the one side and the other of y_0 ;

$$\begin{aligned} a_1 &= \frac{1}{2}(b-ds); & d &= \sigma A = \sqrt[4]{\mu_2} \cdot A; \\ a_2 &= b - a_1; & \\ m_1 &= \frac{a_1}{b}(s-2); & m_1 + m_2 = s - 2; \\ y_0 &= \frac{\alpha}{b} \cdot \frac{m_1^{-m_1} \cdot m_2^{-m_2}}{(m_1 + m_2)^{m_1} + m_2} \cdot \frac{\Gamma(m_1 + m_2 + 2)}{\Gamma(m_1 + 1)(m_2 + 1)}. \end{aligned}$$

To solve this equation it will be necessary to determine the value of each parenthetical quantity following the Γ sign and find the corresponding value of Γ from Table V. It is, however, sometimes easier to calculate the value of y_0 from the following approximate formula:

$$y_0 = \frac{\alpha}{b} \cdot \frac{(m_1 + m_2 + 1)}{\sqrt{2\pi m_1 m_2}} \sqrt{\frac{1}{m_1 + m_2}} e^{\frac{1}{12} \left(\frac{1}{m_1 + m_2} - \frac{1}{m_1} - \frac{1}{m_2}\right)}.$$

With these data the theoretical curve of Type I may be drawn. Frequency polygons of Type I are found in biological measurements.

To compare any observed frequency polygon of Type II with its corresponding theoretical curve.

$$y = y_0 \left(1 - \frac{x^2}{a^2}\right)^m.$$

This equation is only a special form of the equation of Type I in which $a_1 = a_2$ and $m_1 = m_2$.

As from page 17, $\beta_1 = 0$ in Type II, $b = 2\sigma \sqrt{s+1}$; since the curve is symmetrical, d = 0, and

$$a = \frac{b}{2}; \quad m = \frac{1}{2}(s-2); \quad y_0 = \frac{\alpha}{a} \frac{\Gamma(m+1.5)}{\sqrt{\pi}\Gamma(m+1)}.$$

The I values will be found from Table V.

An approximate formula for y_0 is given by Duncker as follows:

$$y_0 = \frac{\alpha}{\sigma \sqrt{2\pi}} \frac{s-1}{\sqrt{(s+1)(s-2)}} e^{-\frac{1}{4(s-2)}}.$$

To compare any observed frequency curve of Type III with its corresponding theoretical curve.

$$y = y_0 \left(1 + \frac{x}{a} \right)^p e^{-x/d}.$$

The range at one side of the mode is infinite; at the other is found by the formula

$$a = \sigma \frac{4 - \beta_1}{2 \sqrt{\beta_1}} = \sigma \frac{1 - A^2}{A} \text{ (for Type III)}.$$

$$a = a - a \cdot c - \alpha - p^{p+1}$$

Also, $p = \frac{a}{d} = \frac{a}{\sigma A}; \quad y_0 = \frac{\alpha}{a} \cdot \frac{p^{p+1}}{e^p \Gamma(p+1)}.$

The value of Γ corresponding to p+1 can be got from Table V. Appendix.

To compare any observed frequency curve of Type IV with its corresponding theoretical curve.

This is the commonest type of biological skew curves.

$$y = y_0(\cos \theta)^{2m} \cdot e^{-v\theta}$$
.

 θ is a variable, dependent upon x as shown in the equation

$$x = a \tan \theta$$
.

The factor $(\cos \theta)^{2m}$ following y_0 indicates that the curve is not calculated from the mean ordinate (M), or the mode (M-d), but that the zero ordinate is at M-md; or at a distance $m \times d$ from the mean.

$$a = \frac{\sqrt{\mu_2}}{4} \sqrt{16(s-1) - \beta_1(s-\hat{z})^2}; \qquad m = \frac{1}{2}(s+2);$$

$$d = \frac{\sigma}{2} \sqrt{\beta_1} \frac{s-2}{s+2}; \qquad md = \frac{\sigma}{4} \sqrt{\beta}(s-2);$$

$$v = \frac{\sqrt{\mu_2} s(s-2) \sqrt{\beta_1}}{4\sigma}, \text{ with the opposite sign to } \mu_3;$$

$$\theta$$
 (arc of circle) = $\frac{\pi\theta^{\circ}}{180^{\circ}}$;

$$y_0 = \frac{\alpha}{a} \sqrt{\frac{s}{\frac{s}{2\pi}}} \frac{e^{\frac{(\cos\phi)^2}{3s} - \frac{1}{12s} - v\phi.*}}{(\cos\phi)^{s+1}}.$$

 $\phi = \text{angle whose tangent is } \frac{v}{s}.$

$$y_0 = \frac{\alpha}{a} \cdot \frac{e^{\frac{1}{2}v\pi}}{\int_0^{2\pi} (\sin\theta)^8 e^{v\theta} d\theta},$$

the formula for reducing which is to be gained from the integral calculus.

^{*}The foregoing value is approximate and is applicable when, as is usually the case, s is greater than 2. The exact value is given by Pearson as

Example of calculating the theoretical curve corresponding with observed data. (Fig. 24.)

Distribution of frequency of glands in the right fore leg of 2000 female swine (integral variates):

Number of glands 0 1 2 3 4 5 6 7 8 9 10 Frequency...... 15 209 365 482 414 277 134 72 22 8 2

Assume the axis yy' (Vm) to pass through ordinate 4, then:

$$\nu_1 = -998 \div 2000 = -.499.$$

$$\nu_2 = 6148 \div 2000 = 3.074.$$

$$\nu_8 = -3872 \div 2000 = -1.936$$
.

$$\nu_4 = 48568 \div 2000 = 24.284.$$

$$\mu_1 = M = 4 - .499 = 3.501.$$

$$\mu_2 = 3.074 - (-.499)^2 = 2.824999.$$

$$\mu_3 = -1.936 - 3(-.499 \times 3.074) + 2(-.499)^3 = 2.417278$$

$$\mu_4 = 24.284 - 4(-.499 \times -1.936) + 6(.249001 \times 3.074) - 3(-499)^4 = 24.826297$$

$$\beta_1 = \frac{(2.417278)^2}{(2.824999)^3} = \frac{5.843232929}{22.545241683} = 0.259178.$$

$$\beta_2 = \frac{24.826297}{(2.824999)^2} = \frac{24.826297}{7.98061935} = 3.110823.$$

$$F = 6 + 3 \times 0.259178 - 2 \times 3.110823 = +0.555888$$
 (Type I).

$$s = \frac{6(3.11082 - 0.25918 - 1)}{.55589} = 19.9857.$$

$$A = \frac{1}{2} \sqrt{.259178} \frac{21.9857}{17.9857} = .31115.$$

$$d = 1.680774 \times .3111 = .5230.$$

$$d.s = .5230 \times 19.9857 = 10.4519.$$

$$b = .840387 \sqrt{16 \times 20.9857 + 0.25918 \times (21.9857)^2} = 18.0448.$$

$$a_1 = \frac{18.0448 - 10.4519}{2} = 3.7965.$$

$$a_2 = 18.0448 - 3.7965 = 14.2483.$$

$$m_1 = \frac{3.7965 \times 17.9857}{18.0448} = 3.78401.$$

$$m_2 = \frac{14.2483 \times 17.9857}{18.0448} = 14.2006.$$

$$y_0 = \frac{2000}{18,0448} \frac{(18.9846) \sqrt{17.9846}}{\sqrt{2\pi \times 3.7840 \times 14.2006}} \times 2.171828$$
.0833(.0556 - .2643 - .0704)

= 475.24, the number of cases in the modal class.

The equation of the theoretical curve is thus

$$y = 475.24 \left(1 + \frac{x}{3.796}\right)^{3.784} \left(1 - \frac{x}{14.248}\right)^{14.201},$$

where x is the difference between the class magnitude and the $mode_i$ regarding signs.

Position of the mode, $y_0 = M - d = 3.501 - .523 = 2.978$.

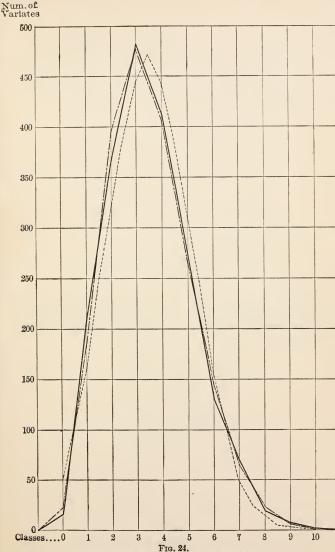
The mean percentage deviation of the theoretical ordinates from the observed ordinates is 11.4%* (Method A). This is calculated as follows:

V	f observed	y theoretical	δ	%
- 1	0	0.0	0.0	
0	15	. 21.1	- 6.1	40.7
1	209	185.8	+23.2	11.1
2	3 65	395.1	- 30.1	8.2
3	482	475.2	+ 6.8	1.4
4	414	405.6	+ 8.4	2.0
5	277	272.1	+ 4.9	1.8
6	134	147.6	- 13.6	10.2
7	72	65.9	+ 6.1	8.5
8	22	24.1	- 2.1	9.5
. 9	8	7.0	+ 1.0	12.5
10	2	1.6	+ 0.4	20.0
11	. 0	0.2		
12	0	0.0		11.4%

MULTIMODAL CURVES.

Multimodal curves are given when the frequency in the different classes exhibits more than one mode. False multimodal curves result from too few observations, or when the classes are made too numerous for the variates. By increasing the number of variates or by making the classes more inclusive some of the modes disappear.

^{*} The mean percentage deviation by Duncker's determination with method B using the same data is 1.73% of area.



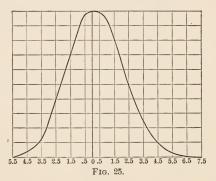
Distribution of frequency in glands of swine.

—, polygon of observed frequency.

—, polygon of theoretical frequency (Type I).

—, normal frequency polygon.

Multimodal curves differ in degree. The modes may be so close that only a single mode (usually in an asymmetrical curve) appears in the result; or one of the modes may appear as a hump on the other; or the two modes may even be far apart and separated by a deep sinus (Figs. 25 to 28).



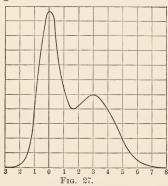
Pearson has offered a means of breaking up a compound curve with apparently only one mode into two curves having distinct modes; but this method is very tedious and rarely applicable.



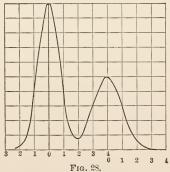
The index of divergence of two modes of a multimodal curve is the distance between the modes expressed in terms of the standard deviation of the more variable of the components.*

The index of isolation of two masses of variates grouped about adjacent modes is the ratio of the depression between the modes to the height of the shorter mode.

The meaning of multimodal curves is diverse. Sometimes



they indicate a polymorphic condition of the species, the modes representing the different type forms. This is the case with



the number of ray flowers of the white daisy which has modes at 8, 13, 21, 34, etc. Sometimes they indicate a splitting of a species into two or more varieties.

^{*} I have proposed (Science, VII, 685) to measure the divergence in a unit = $3 \times$ Standard Deviation, which has certain advantage in species study.

CHAPTER IV.

CORRELATED VARIABILITY.

Correlated variation is such a relation between the magnitudes of two or more characters that any abmodality of the one is accompained by a corresponding abmodality of the other or others.

The methods of measuring correlation depend upon the assumption that the variates of the characters compared are distributed normally about the mode. The method is approximately applicable to cases where the distribution of variates is slightly skew.

The principles upon which the measure of correlated variation rest are these. When we take individuals at random we find that the mean magnitude of any character is equal to the mean magnitude of this character in the whole population. Deviation from the mean of the whole population in any lot of individuals implies a selection. If we select individuals on the basis of one character (A, called the subject) we select also any closely correlated character (B, called the relative) (e.g. leglength and stature). If perfectly correlated, the index of abmodality of B will be as great as that of A or

$$\frac{\text{Index abmodality of relative}}{\text{Index abmodality of subject}} = 1.$$

If there is no correlation, then whatever the value of the index of modality of the subject, that of the relative will be zero and the coefficient of correlation will be

$$\frac{\text{Index of abmodality of relative}}{\text{Index of abmodality of subject}} = \frac{0}{m} = 0.$$

The coefficient of correlation is represented in formulas by the letter ρ . We cannot find the degree of correlation between two organs by measuring a single pair only; it is the correlation "in the long run" which we must consider. Hence we must deal with masses and with averages.

					-	-		-	-			-				
Classes	Classes of left leg.	0		os.	က	-j ı	ıo	9	<u>-</u>	20	5	10				
Deviations	Deviations of rel. class.	-3.54	-2.54	-1.54 -0.54	-0.54	0.46	1.46	2.46	3,46	4.46	5.46	6.46	Means left.		Deviat. Dev. Rel. Dev. Subj from M. S. D. rel. S.D. subj	Dev.Subj
Classes of right leg.	Deviation from mean.															
0	-3.547	∞	ro	c≀	:	:	:	:	:	:	:	:	009.0	-2.940	-1.70	-2.05
П	-2.547	4	151	28	6	က	:	:	:	:	:	:	1.360	-2.180	-1.26	-1.47
cs.	-1.547	e>	65	154	96	88	ž÷	-	:	:	:		3.306	-1.934	02.0-	0.90
ත	-0.547	:	14	88	173	128	88	9	:	:	:	:	3,197	-0.343	-0.20	-0.33
4	0.453	:	73	226	119	153	22	56	ಣ	-	:	:	3,888	0.348	0.30	98.0
ō	1,453	:		2-	5€	<u>26</u>	101	23	11	0	:	:	4.784	1.944	0.73	0.84
9	2.453		:	:	œ	16	82	48	16	ž-	0	cs.	5.510	1.970	1.14	1.42
¿~	3,453		:		П	œ	30	18	17	6	ro	:	6.141	2.601	1.50	3.00
œ	4.453		:		:		က	ت	က	es.	C\$:	6.500	2.90	1.71	2.57
6	5,453		:	:	:	:	-	හ	က	C5	C5	-	7.333	3.793	2.19	3.15
10	6.453		:	:	:	:	:	:			1		000.6	5.460	3.25	3,73
	Mean number of clonds right lea male = 3 547	phar of	olonde	rioht	leo. n	- ole	3 547		S.	tandar	d devi	ation.	Standard deviation relative 1 73	1.73		

Mean number of glands, right leg, male = 3.547left leg, male = 3.540

Standard deviation, relative, 1.73 subject, 1.73

In studying correlation one (either one) of the characters is regarded as subject and the other as relative. A correlation table is then arranged as in the example on page 29, which gives data for determining the correlation between the number of Müllerian glands on the right (subject) and left (relative) legs of male swine.

METHODS OF DETERMINING COEFFICIENT OF CORRELATION.

Galton's graphic method. On co-ordinate paper draw perpendicular axes X and Y; locate a series of points from the pairs of indices of abmodality of the relative and subject corresponding to each subject class. The indices of the subjects are laid off as abscissæ; the indices of the relatives as ordinates, regarding signs. Get another set of points by making a second correlation table, regarding character B as subject and character A as relative. Then draw a straight line through these points so as to divide the region occupied by them into halves. The tangent of the angle made by the last line with the horizontal axis XX (any distance yp, divided by xp) is the index of correlation.

A more precise method is given by Pearson as follows: Sum of products (deviation subj. class \times deviation each assoc. rel. class \times no. of cases in both)

total no. of indivs. × Stand. Dev. of subject × Stand. Dev. of relative;

or, expressed in a formula :

$$\rho = \frac{\sum (\text{dev. } x \times \text{dev. } y \times f)}{n\sigma_1\sigma_2}.$$

This method requires finding many products in the numerator, as many sets of products as there are entries in the body of the correlation table. A portion of the products to be found is indicated below:

$$\begin{array}{c} -3.547 \times \begin{cases} -3.540 \times 8 \\ -2.540 \times 5 \\ -1.540 \times 2 \end{cases} \\ -2.540 \times 4 \\ -2.540 \times 151 \\ -1.540 \times 58 \\ -0.540 \times 9 \\ -0.460 \times 3 \end{array}$$

A brief method of finding ρ is given by Duncker as follows:

$$ho$$
 is composed of two factors: $\dfrac{\varSigma(\mathrm{dev.}\ x\! imes\!\mathrm{dev.}\ y\! imes\!f)}{n}$ and $\dfrac{1}{\sigma_1\sigma_2}$

To find $\dfrac{\varSigma(\mathrm{dev.}\ x\! imes\!\mathrm{dev.}\ y\! imes\!f)}{n}$.

Separate the deviation from the mean of each class into its integral and its fractional parts; the fractional parts for all classes below the mean will be equal to the fractional part of the mean; of all classes above the mean, to the complement of that number. Designate the integral parts of the variants of the subject by $\pm X_1$; of the relatives by $\pm X_2$, and the fractional complement parts of the means of subject or relative by ξ_1, ξ_2 . Let f equal the frequency of any deviation in the combination X_1X_2 , as shown in the correlation table. Draw rectangular co-ordinates as shown on page 34 through the zeropoint of the correlation table. Number the N. W. quadrant, which should include negative deviations of both subject and relative variants, I; the N. E. quadrant, II; the S. W. quadrant containing solely positive deviations III; and the S. E. quadrant, IV. Then if $\Sigma_{\rm I}$, $\Sigma_{\rm II}$, etc., indicate a summation for the quadrant I, II, etc., and having regard to signs:

$$\frac{\sum_{1-IV}(fX_{1}X_{2})-\sum_{I}(fX_{1})-\sum_{I}(fX_{2})}{+\sum_{I}(f)-\sum_{I}(fX_{2})-\sum_{III}(fX_{1})}-\xi_{1}\xi_{2}.$$

The numerator of this fraction consists entirely of whole numbers; of them the following are on their own account

Rule: (1) Find products of integral parts of deviations of both subject and relative and the combination frequency, for all four quadrants, and take their sum.

(2) Subtract successively the sum of the products of the subject deviations in the first quadrant multiplied by the frequency, and the sum of the products of the relative deviations in the first quadrant multiplied by the frequency. Since these are negative values they will be actually added.

- (3) Add the sum of the numbers in the first quadrant; subtract the sum of the products of the integral parts of the relative deviations by the frequency in the second quadrant; subtract the sum of the products of the subject deviations of he third quadrant multiplied by their frequency.
- (4) Divide the algebraic sum of (1), (2), and (3) by the number of variates, and from the quotient subtract the product of the complement-fractional parts of the mean value of the subject and relative.

To get ρ , divide $\frac{\sum_{x_1x_2f}}{n}$ by the product of σ_1 and σ_2 .

The probable error of the determination of ρ is

$$P.E._{\rho} = \frac{0.6745(1-\rho^2)}{\sqrt{n(1+\rho)}}.$$

Example. Correlation in number of Müllerian glands on right and left legs of 2000 male swine.

Moon right log - 2 5165. Moon left le

111	ean, 1	пап	reg,	=	5.040	э;	Me	an, I	ert le	eg, =	= 3.8	5395
	σ_1			=	1.719	5;	(\mathcal{T}_2		=	= 1.	7304
	Righ	ıt leş	g, su	bjec	t:	I	eft l	eg, r	elativ	7e.		
X_{i}	2	- 3	- 2	- 1	0	0		2	3	4	5	6
Rel.	class	0	1	2	3	4	5	6	7	8	9	10
Sub	. class	s (I)										(II)
	X_1											
0	3	8	5	2								
1	- 2	4	151	58	9	3						
2	- 1	2	65	154	96	28	7	1				
3	0		14	88	173	128	28	6				
4	0		5	27	119	153	77	26	3	1		
5	1		1	7	24	92	101	52	11	9		
6	2				8	16	58	48	16	7		2
7	3				1	8	20	18	17	9	5	
8	4					1	3	5	3	2	2	
9	5						1	3	3	2	2	1
10	6 (III)									1	(IV)
												` ′

$$\begin{array}{l} \mathcal{Z}_{I-IT}(fX_1X_2) = 1142 - 9 - 9 + 1652 \\ -\mathcal{Z}_I(fX_1) - \mathcal{Z}(fX_2) + \mathcal{Z}_I(f) \\ = +806 + 814 + 829 \\ -\mathcal{Z}_{II}(fX_2) - \mathcal{Z}_{III}(fX_1) \\ = -49 - 51 \end{array} \right\} \div n = \frac{5125}{2000} = 2.5625 \\ -\xi_1\xi_2 = -4535 \times .4605 = \frac{-.2088}{2.3537}$$

$$\sigma_1 \sigma_2 = 1.7195 \times 1.7304 = 2.9754; \rho = \frac{2.3537}{2.9754} = .7919$$

$$P.E._{\rho} = \frac{.6745[1 - (.7919)^2]}{\sqrt{2000} \times 1.627} = \pm 0.0044$$

Spurious Correlation in Indices.

When two characters A and B are measured in each individual of a series of individuals, and each absolute magnitude is transformed into an index by dividing it by the magnitude of a third character C as found in the same individual, a spurious correlation will be found to exist between the indices of $\frac{A}{C}$ and $\frac{B}{C}$

Let
$$v_1$$
 = the coefficient of variation of A ;
 v_2 = " " " " B ;
 v_3 = " " " " C ;
 ρ_0 = " " spurious correlation.

$$\rho_0 = \frac{v_3^2}{\sqrt{v_1^2 + v_3^2} \sqrt{v_2^2 + v_3^2}}.$$

The precise method of using ρ_0 in modifying any determination of ρ is uncertain. Pearson recommends using $\rho - \rho_0$ as the true measure of "organic correlation" in the case of indices.

HEREDITY.

Heredity is a certain degree of correlation between the abmodality of parent and offspring. The statistical laws of heredity deal not with relations between one descendant and its parent or parents, but only with mean progeny of mean parents. Any group of selected parents is called a parentage, the progeny of a parentage is called a fraternity.

In uniparental inheritance, as in budding or asexual generation, heredity of any character is measured by the coefficient of correlation between the abmodality in a parentage and the abmodality of the corresponding fraternity. More strictly, since the variability of the character in the second generation, σ_2 , may (as a result of selection or of environmental change) be different from the variability of the character in the first generation, σ_1 , the index should be taken as

$$\rho \frac{\sigma_1}{\sigma_2}$$
.

The probable error of this determination is $\frac{.6745\,\sigma_1}{\sigma_2}\sqrt{\frac{1-\rho_{12}^2}{n}}$, in which ρ_{12} means the correlation coefficient between the filial character and that of the single parent

under consideration.

The variability of the fraternity is to variability of offspring in general as $\sqrt{1-\rho^2}$ is to 1.

In biparental inheritance, if there is no evidence of assortative mating, or correlation between the two parents in the character in question, the mean abmodality of any fraternity will be

$$h_1 = \rho_3 \frac{\sigma_1}{\sigma_2} h_2 + \rho_2 \frac{\sigma_1}{\sigma_3} h_3,$$

where $h_1 = \text{average abmodality of fraternity}$;

 h_2 = average abmodality of male parent;

 h_3 = average abmodality of female parent;

 $\rho_2 = \text{correlation coefficient between fraternity and }$ female parent;

 ρ_3 = correlation coefficient between fraternity and male parent;

 $\sigma_1 = \text{standard deviation of fraternity}$;

 $\sigma_2 = \text{standard deviation of male parent};$

 σ_3 = standard deviation of female parent.

When assortative mating occurs, as is usually case, the abmodality of a fraternity is given by

$$h_1 = rac{
ho_3 -
ho_1
ho_2}{1 -
ho_1^2} \cdot rac{\sigma_1}{\sigma_2} h_2 + rac{
ho_2 -
ho_1
ho_3}{1 -
ho_1^2} \cdot rac{\sigma_1}{\sigma_2} \cdot h_3,$$

where ρ_1 = correlation between male and female parents. The other letters have the same signification as before.

The strength of heredity in assortative mating is measured by the formula

$$\frac{\rho_3-\rho_1\rho_2}{1-\rho_1^2}\cdot\frac{\sigma_1}{\sigma_2}$$

Galton ('97) has shown that an individual inherits not only from his parents, but also from his grandparents, great-grandparents, and so on. The heritage from his 2 parents together is, on the average, 50% or $\frac{1}{2}$ of the whole; from the 4 grandparents 25% or $\frac{1}{4}$; from the 8 great-grandparents 12.5% or $\frac{1}{8}$; from the *n*th ancestral generation $\frac{1}{2^n}$ of the whole; the total

heritage adding up 100%. This law has been generalized by Pearson ('98) as follows:

$$h_1 = \frac{1}{2} \frac{\sigma_0}{\sigma_1} k_1 + \frac{1}{4} \frac{\sigma_0}{\sigma_2} k_2 + \frac{1}{8} \frac{\sigma_0}{\sigma_3} k_3 + \frac{1}{16} \frac{\sigma_0}{\sigma_4} k_4 + \dots$$

where h_1 = average abmodality of fraternity.

 $\sigma_0 = \text{standard deviation of fraternity.}$

 σ_1 , $\sigma_2 \dots \sigma_s = \text{standard deviation of mid-parent of}$ 1st, 2d . . . sth ancestral generation.

 $k_1 =$ abmodality of mid-parent of 1st ancestral generation.

 k_2 , k_3 ... k_s = abmodality of mid-parent of 2d, 3d ... sth ancestral generation.

The abmodality of the mid-parent of any degree of ancestry may be taken as the average abmodality of all the contributory ancestors of that generation.

CHAPTER V.

Some Applications of Statistical Biological Study.

The Laws of Variation. Darwin and others have formulated certain laws of variation, such as the law that specific characters are more variable than generic ones; that highly aberrant characters are more variable than more usual ones; that males are more variable than females. These laws can be established only by a determination of the Index or Coefficient of Variation in critical cases.

The causes of variation can be determined only by a quantitative study of the relation between specific change and environmental change, or a knowledge of the degree and frequency of sports.

The effect of **selection** in causing a greater death rate on one side of the mean than on the other side—the production of skewness—requires the quantitative method for its complete study. The change in the mode and in the index of skewness measures the progress of the effect of selection.

The **origin** of species through geographical segregation can be studied by the determination of place-modes; that is, the modal condition of specific characters of one and the same species in various localities. The progress of specific differentiation will be measured by the change in place-modes from decade to decade, or by the formation of a binomial curve in the place of a modal one; and by the gradual separation of the two modes of a binomial curve.

The definition of species may be improved by being rendered more quantitative. The relative importance of the various criteria used in separating species may be determined by finding that character in which there is least intergrading between the modal condition characteristic of the two races. Thus if for two species or varieties of birds both total length and form of bill show two modes, the better criterion is that in which the modes are farthest apart or in which the intergrades are fewest.

A basis for an arbitrary distinction between species and varieties may be gained by determining a degree of divergence and of isolation which shall be used to distinguish the two. A degree of divergence of thrice the standard deviation has been suggested as a convenient line between species and varieties.

Quantitative studies in correlation will give us new criteria for homology by telling us the relative morphoge-

netic kinship of the parts of the body.

Quantitative studies in heredity will give definitive information on **prepotency** of sex or race. By examining hybrids quantitatively and comparing them with their parents we shall unravel the laws of inheritance in cross-breeding and the principles of mixing characters in biparental inheritance.

In a word, by the use of the quantitative method biology will pass from the field of the speculative sciences to that of

the exact sciences.

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EXPLANATION OF TABLES.

- I. Formulas. In this table the principal formulas used in the calculation of curves are brought together for convenient reference. The meanings of the letters are explained in the text.
- II. Certain constants and their logarithms. This table includes the constants most frequently employed in the calculations of this book.
- III. Table of ordinates of normal curve. This table is for comparison of a normal frequency polygon consisting of weighted ordinates with the theoretical curve.

Example: M=14.157; $\sigma=0.604$; $1y_0=1255$. (See page 19.)

IV. Table of values of probability integral. This table is for comparison of a normal frequency polygon consisting of rectangles with the theoretical curve.

Example: M. 5.24; $\sigma = 0.987$. (See page 12).

f	%	Class limits	$\begin{array}{c} \text{Deviation} \\ \text{from} \\ M = x \end{array}$	$\frac{x}{\sigma}$	$\Sigma_0^{x+\sigma}$
1	4	3.0	-2.24	-2.27	48.8
1	4	3.5	-1.74	-1.76	46.1
3	12	4.0	-1.24	-1.26	39.6
3	12	4.5	-0.74	-0.75	27.3 ····· The oret ical fre quency
7	28	5.0	-0.24	-0.25	9.9 20.5 55.2 79.6 92.4 97.7
5	20	5.5	0.26	0.27	10.6 28 60 84 92 100 Ob serv ed fre quency
3	12	6.0	0.76	0.77	27.9 da 110 quency
1	4	6.5	1.26	1.28	40.0
1	4	7.0	1.76	1.78	46.3
25	100	7.5	2.26	2.29	48.9

In the example, the curve of which is shown in Fig. 22, the frequency between the limits is given in column f; the frequency reduced to percents in column headed %. The $\frac{x}{\sigma}$ of the limit is found and the entries in Table IV corresponding to the quotient are taken. These are added in pairs as indicated, one above and one below the mean, and the sum is compared with the sum of the observed cases within those limits (in italic figures). The closeness of agreement indicates the closeness with which the observed frequency follows the normal frequency.

V. Table of $\log \Gamma$ functions of q. This table will enable one to solve the equations for y_0 given on page 23. The table gives the logarithms of the values of Γ functions only within the range p=1 to 2. As all values of the function within these limits are less than 1, the mantissa of the logarithms is -1; but it is given in the table as 10-1=9, as is usually done in logarithmic tables.

Supposing the quantity of which we wish to find the value reduced to the form $\Gamma(4.273)$. The value cannot be found directly because the value of p is larger than the numbers in the table (1 to 2). The solution is made by aid of the equation $\Gamma(p+1) = p\Gamma(p)$, thus:

$$\log \Gamma(1.273) = 9.955185$$

$$\log 1.273 = 0.104828$$

$$\log \Gamma(2.273) = 0.060013$$

$$\log 2.273 = 0.356599$$

$$\log \Gamma(3.273) = 0.416612$$

$$\log 3.273 = 0.514946$$

$$\log \Gamma(4.273) = 0.931558$$
or, more briefly,
$$\log \Gamma(1.273) = 9.955185$$

$$\log 1.273 = .104828$$

$$\log 2.273 = .356599$$

$$\log 3.273 = .514946$$

$$\log \Gamma(4.273) = 0.931558 = \log 8.542$$

- VI. Table of reduction from the common to the metric system. This is given first for whole inches from 1 to 99 excepting even tens, which may be got from the first line of figures by shifting the decimal point one place to the right. The table may be used for hundredths of an inch by shifting the decimal point two places to the left. Other fractions than decimals are given in the lower tables.
- VII. First to sixth powers of integers from 1 to 30. This table is useful in calculating moments.
- VIII. Squares, cubes, square roots, and reciprocals of numbers from 1 to 1054. The use of this table can be extended by using the principle that if any number be multiplied by n, its square is multiplied by n^2 , its cube by n^3 , and its reciprocal by $\frac{1}{n}$.
- IX. Logarithms of numbers to six places. The following explanation of the use of the logarithmic tables is taken from Searles' Field Engineering, pp. 257-263 [ed. 1887].

APPENDIX IX.—The logarithm of a number consists of two parts, a whole number called the *characteristic*, and a decimal called the *mantissa*. All numbers which consist of the same figures standing in the same order have the same mantissa, regardless of the position of the decimal point in the number, or of the number of ciphers which precede or follow the significant figures of the number. The value of the characteristic depends entirely on the position of the decimal point in the number, It is always one less than the number of figures in the number to the left of the decimal point. The value is therefore diminished by one every time the decimal point of the number is removed one place to the left, and vice versa. Thus

Number.	Logarithm,
13840.	4.141136
1384.0	3.141136
138.40	2.141136
13.84	1.141136
1.384	0.141136
.1384	-1.141136
.01384	-2.141136
.001384	-3.141136
etc.	etc.

The mantissa is always positive even when the characteristic is negative. We may avoid the use of a negative characteristic by arbitrarily adding 10, which may be neglected at the close of the calculation. By this rule we have

Number.	Logarithm.
1.384	0.141136
.1384	9.141136
.01384	8.141136
.001384	7.141136
etc.	etc.

No confusion need arise from this method in finding a number from its logarithm; for although the logarithm 6.141136 represents either the number 1,384,000, or the decimal .0001384, yet these are so diverse in their values that we can never be uncertain in a given problem which to adopt.

The table IX. contains the mantissas of logarithms, carried to six places of decimals, for numbers between 1 and 9999, inclusive. The first three figures of a number are given in the first column, the fourth at the top of the other columns. The first two figures of the mantissa are given only in the second column, but these are understood to apply to the remaining four figures in either column following, which are comprised between the same horizontal lines with the two.

If a number (after cutting off the ciphers at either end) consists of not more than four figures, the mantissa may be taken direct from the table; but by interpolation the logarithm of a number having six figures may be obtained. The last column contains the average difference of consecutive logarithms on the same line, but for a given case the difference needs to be verified by actual subtraction, at least so far as the last figure is concerned. The lower part of the page contains a complete list of differences, with their multiples divided by 10.

To find the logarithm of a number having six figures:—Take out the mantissa for the four superior places directly from the table, and find the difference between this mantissa and the next greater in the table. Add to the mantissa taken out the quantity found in the table of proportional parts, opposite the difference, and in the column headed by the fifth figure of the number; also add $\frac{1}{10}$ the quantity in the column headed by the sixth figure. The sum is the mantissa required, to which must be prefixed a decimal point and the proper characteristic.

Example.—Find the log of 23.4275.

For 2342 mantissa is 369587 '' diff. 185 col. 7 129.5 '' '' '' 5 9.2

Ans. For 23.4275 log is 1.369726

The decimals of the corrections are added together to determine the nearest value of the sixth figure of the mantissa.

To find the number corresponding to a given logarithm.—If the given mantissa is not in the table find the one next less, and take out the four figures corresponding to it; divide the difference between the two mantissas by the tabular difference in that part of the table, and annex the figures of the quotient to the four figures already taken out. Finally, place the decimal point according to the rule for characteristics, prefixing or annexing ciphers if necessary. The division required is facilitated by the table of proportional parts, which furnishes by inspection the figures of the quotient.

First 4 figures 1836 from 263873Tabular diff. = 236 ... 5th fig. = 2 47.26th fig. = 3 7.08

Ans. No. = .0183623 or 183,623,000.

The number derived from a six-place logarithm is not reliable beyond the sixth figure.

At the end of table XXIV. is a small table of logarithms of numbers from 1 to 100, with the characteristic prefixed, for easy reference when the given number does not exceed two digits. But the same mantissas may be found in the larger table.

APPENDIX X.—The logarithmic sine, tangent, etc. of an arc is the logarithm of the natural sine, tangent, etc. of the same arc, but with 10 added to the characteristic to avoid negatives. This table gives log sines, tangents, cosines, and cotangents for every minute of the quadrant. With the number of degrees at the left side of the page are to be read the minutes in the left-hand column; with the degrees on

the right-hand side are to be read the minutes in the right-hand column. When the degrees appear at the top of the page the top headings must be observed, when at the bottom those at the bottom. Since the values found for arcs in the first quadrant are duplicated in the second, the degrees are given from 0° to 180°. The differences in the logarithms due to a change of one second in the arc are given in adjoining columns.

To find the log.sin, cos, tan, or cot of a given arc.: Take out from the proper column of the table the logarithm corresponding to the given number of degrees and minutes. If there be any seconds multiply them by the adjoining tabular difference, and apply their product as a correction to the logarithm already taken out. The correction is to be added if the logarithms of the table are increasing with the angle, or subtracted if they are decreasing as the angle increases. In the first quadrant the log sines and tangents increase, and the log cosines and cotangents decrease as the angle increases.

Example.—Find the log sin of 9° 28' 20".

 $\begin{array}{ll} \text{Log sin of 9° 28' is} & 9.216097 \\ \text{Add correction } 20 \times 12.62 & 252 \end{array}$

Ans. 9.216349

Example.—Find the log cot of 9° 28′ 20″.

Log cotan of 9° 28' is 10.777948 Subtract correction 20×12.97 259

Ans. 10.777689

To find the angle or arc corresponding to a given logarithmic sine, tangent, cosine, or cotangent.—If the given logarithm is found in the proper column take out the degrees and minutes directly; if not, find the two consecutive logarithms between which the given logarithm would fall, and adopt that one which corresponds to the least number of minutes; which minutes take out with the degrees, and divide the difference between this logarithm and the given one by the adjoining tabular difference for a quotient, which will be the required number of seconds.

With logarithms to six places of decimals the quotient is not reliable beyond the tenth of a second.

Example. -9.383781 is the log tan of what angle?

Next less 9.383682 gives

13° 36′

Diff. $49.00 \div 9.20 = 05''.3$ Ans. 13° 36′ 05''.3

Example. -9.249348 is the log cos of what angle?

Next greater 583 gives 79° 46′

Diff. $235 \div 11.67 = 20''.1$ Ans. $79^{\circ} 46' 20''.1$

The above rules do not apply to the first two pages of this table (except for the column headed cosine at top) because here the differences vary so rapidly that interpolation made by them in the usual way will not give exact results.

On the first two pages, the first column contains the number of seconds for every minute from 1' to 2°; the minutes are given in the second, the log. sin. in the third, and in the fourth are the last three figures of a logarithm which is the difference between the log sin and the logarithm of the number of seconds in the first column. The first three figures and the characteristic of this logarithm are placed, once for all, at the head of the column.

To find the log sin of an arc less than 2° given to seconds.—Reduce the given arc to seconds, and take the logarithm of the number of seconds from the table of logarithms, and add to this the logarithm from the fourth column opposite the same number of seconds. The sum is the log sin required.

The logarithm in the fourth column may need a slight interpolation of the last figure, to make it correspond closely to the given number of seconds.

Example.—Find the log sin of 1° 39′ 14″.4.

1° 39′ 14″.4 = 5954″.4 log 3.774838 add (q-l) 4.685515

Ans. log sin 8.460353

Log tangents of small arcs are found in the same way, only taking the last four figures of (q-l) from the fifth column.

Example.—Find the log tan of 0° 52′ 35″.

52' 35" = (3120" + 35") = 3155" $\log 3.498999$ add (q - b) 4.685609

Ans. log tan 8.184608

To find the log cotangent of an angle less than 2° given to seconds.—Take from the column headed (q+l) the logarithm corresponding to the given angle, interpolating for the last figure if necessary, and from this *subtract* the logarithm of the number of seconds in the given angle.

Example.—Find the log cotan of 1° 44′ 22″.5.

$$6240'' + 22''.5 = 6262.5$$

$$q + l 15.314292$$

$$\log 3.796748$$

$$Ans. 11.517544$$

These two pages may be used in the same way when the given angle lies between 88° and 92° , or between 178° and 180° ; but if the number of degrees be found at the bottom of the page, the title of each column will be found there also; and if the number of degrees be found on the right hand side of the page, the number of minutes must be found in the right hand column, and since here the minutes increase upward, the number of seconds on the same line in the first column must be diminished by the odd seconds in the given angle to obtain the number whose logarithm is to be used with $(q \pm l)$ taken from the table.

Example.—Find the log cos of 88° 41′ 12″.5

$$4740'' - 12''.5 = 4727.5$$
 $(q - l) 4.685537$ $\log 3.674631$

Ans. 8.360168

Example.—Find the log tan of 90° 30′ 50″.

$$1800" + 50" = 1850"$$
 $\begin{array}{c} q + l \ 15.314413 \\ \log \ 3.267172 \\ Ans. \ 12.047241 \end{array}$

To find the arc corresponding to a given log sin, cos, tan, or cotan which falls within the limits of the first two pages of Table X.

Find in the proper column two consecutive logarithms between which the given logarithm falls. If the title of the given function is found at the top of that column read the degrees from the top of the page; if at the bottom read from the bottom.

Find the value of (q-l) or (q+l), as the case may require, corresponding to the given log (interpolating for the last figure if necessary). Then if q =given log and l =log of number of seconds, n, in the required arc, we have at once l = q - (q - l) or l = (q + l) - q, whence n is easily found.

Find in the first column two consecutive quantities between which the number n falls, and if the degrees are read from the left hand side of the page, adopt the less, take out the minutes from the second column, and take for the seconds the difference between the quantity adopted and the number n. But if the degrees are read from the right hand side of the page, adopt the greater quantity, take out the minutes on the same line from the right-hand column, and for the seconds take the difference between the number adopted and the number n.

```
Example.—11.734268 is the log cot of what arc?
  q + l
                                               15.314376
                                               11.734268
    q
                  3802.8
                                                3.580108
                           giving 03'
  For 1° adopt
                 3780.
  Difference
                    22".8
Ans. 1° 03′ 22″.8 or 178° 56′ 37″.2.
Example.—8.201795 is the log cos of what arc?
  q-l
                                                4.685556
    q
                                                8.201795
                   3282".8
                                                3,516239
  For 89° adopt 3300.
                           giving 05'
  Difference
                     17".2
Ans. 89° 05′ 17″.2 or 90° 54′ 42″.8.
```

I.-FORMULAS.

$$\begin{split} M &= \frac{\Sigma(V,f)}{n} = V_m - \nu_1, \qquad P.E._M = \pm 0.6745 \frac{\sigma}{\sqrt{n}}, \qquad x = V - M, \\ \sigma &= \sqrt{\frac{\Sigma(x^2,f)}{n}} = \sqrt{\nu_2 - \nu_1^2} = \sqrt{\mu_2}, \quad P.E._\sigma = 0.6745 \frac{\sigma}{\sqrt{2n}}, \\ AD &= \frac{\Sigma(x,f)}{n} = 0.7979\sigma, \qquad P.E. = q = 0.6745\sigma, \\ \nu_1 &= \frac{\Sigma(V - V_m)}{n} = M - V_m, \qquad \qquad \nu_2 = \frac{\Sigma(V - V_m)^2}{n}, \\ \nu_3 &= \frac{\Sigma(V - V_m)^3}{n}, \qquad \qquad \nu_4 = \frac{\Sigma(V - V_m)^4}{n}, \\ \mu_2 &= \nu_2 - \nu_1^2(+\frac{1}{6}) = \frac{\Sigma(x^2,f)}{n}(+\frac{1}{6}), \\ \mu_3 &= \nu_3 - 3\nu_1\nu_2 + 2\nu_1^3 = \frac{\Sigma(x^3,f)}{n}, \\ \mu &= \nu_4 - 4\nu_1\nu_3 + 6\nu_1^2\nu_2 - 3\nu_1^4(+\nu_2 - \nu_1^2 + \frac{\tau_5}{15}) = \frac{\Sigma(x^4,f)}{n}\left(+\frac{\Sigma(x^2,f)}{n} + \frac{1}{15}\right), \\ \beta_1 &= \frac{\mu_3^2}{n^2}, \qquad \qquad \beta_2 = \frac{\mu_4}{n^2}. \end{split}$$

$$F = 6 + 3\beta_1 - 2\beta_2.$$

$$s = \frac{6(\beta_2 - \beta_1 - 1)}{E}.$$

$$A = \frac{1}{2} \sqrt{\beta_1} \frac{s \pm 2}{s \mp 2}. \qquad d = \sigma. A$$

 $\Delta \% \, (\text{for graduated variates}) = \frac{\Sigma \delta_1 + \Sigma (- \, \delta_2)}{2n} \, . \, 100 \%.$

 Δ % (for integral variates) = $\Sigma \frac{\delta}{f \cdot k}$. 100%, where k equals the number of classes.

$$\rho = \frac{\Sigma(\text{dev. } x . \text{dev. } y . f)}{n\sigma_1\sigma_2} = \frac{\Sigma X_1 X_2 f}{n\sigma_1\sigma_2}.$$

$$\frac{\Sigma_f X_1 X_2}{n} = \frac{\Sigma_{I-IV}(fX_1 X_2) - \Sigma_I(fX_1) - \Sigma_I(fX_2) + \Sigma_I(f) - \Sigma_{II}(fX_2) - \Sigma_{III}(fX_1)}{n} - \xi_1 \xi_2$$

$$0.6745(1 - o^2)$$

$$P.E._{\rho} = \frac{0.6745(1-\rho^2)}{\sqrt{n(1+\rho)}}.$$

 $\rho_0 \text{ (spurious correlation)} = \frac{v_3^2}{\sqrt{v_1^2 + v_3^2} \sqrt{v_2^2 + v_3^2}}.$

h (index of heredity, uniparental inheritance) = $\rho \frac{\sigma_1}{\sigma_2}$.

$$P.E._h = \frac{.6745\sigma_1}{\sigma_2} \sqrt{\frac{1 - \rho_{12}^2}{n}}.$$

 $h_1 = \rho_3 \frac{\sigma_1}{\sigma_2} h_2 + \rho_2 \frac{\sigma_1}{\sigma_3} h_3$ [biparental inheritance; unassortative mating].

 $h_1 = \frac{\rho_2 - \rho_1 \rho_2}{1 - \rho_1^2} \cdot \frac{\sigma_1}{\sigma_2} h_2 + \frac{\rho_2 - \rho_1 \rho_2}{1 - \rho_1^2} \cdot \frac{\sigma_1}{\sigma_2} \cdot h_3 \quad \text{[biparental inheritance; assortative mating]}.$

II.—CERTAIN CONSTANTS AND THEIR LOGARITHMS.

Title.	Symbol	Number.	Log.
Ratio of circumference to diameter	π	3.1415927	0.4971499
Reciprocal of same	$\frac{1}{\pi}$	0.3183099	9.5028501
Square root of same	$\sqrt{\pi}$	1.7724538	0.2485749
Reciprocal of square root of same	$\frac{1}{\sqrt{\pi}}$	0.5641896	9.7514251
Square root of 2π	$\sqrt[4]{2\pi}$	2.506628	0.399090
Reciprocal of same	$\frac{1}{\sqrt{2\pi}}$	0.3989422	9.6009100
Base of hyperbolic logarithms	€	2.7182818	0.4342945
Modulus of common system of logs = log ϵ	nι	0.4342945	9.6377843
Reciprocal of same = hyp. log 10	$\frac{1}{m}$	2.3025851	0.3622157
Com. $\log x = m \times \text{hyp. } \log x, \text{ or}$			
Com.log(com.log(x) = 9.6377843 + com.log(hyp.log(x))			
Hyp. $\log x = \text{com. } \log x \times \frac{1}{m}$, or			
Com.log(hyp.log x) = com.log(com.log x) + 0.3622157			
Circumference of circle =	$2\pi r$		
Area of circle	πr^2		
Area of sector (length of arc = l)	½lr		
Area of sector (angle of arc = a°)	$\frac{a}{360}\pi r^2$		
Eccentricity of an ellipse, $\epsilon = \sqrt{\frac{a^2 - b^2}{a^2}}$, where a	ı=semi-n	najor axis	b=semi-
4-		axis of el	

III.—TABLE OF ORDINATES OF NORMAL CURVE, OR VALUES_OF $\frac{y}{y_0}$ CORRESPONDING TO VALUES OF $\frac{x}{\sigma}$.

x =deviation from mean. y =frequency.

 $\sigma={
m standard\ deviation}, \qquad y_0=rac{a}{\sigma\ V^{2\pi}}={
m maximum\ frequency}.$

x/σ	y/y_0	<i>x/σ</i>	y/y_0	<i>x</i> /σ	y/y_0	x/σ	y/y_0
0 0.1 0.2 0.3 0.4 0.5 0.6 0.7	1. .9950 .9802 .9560 .9231 .8825 .8353 .7827	0.8 0.9 1.0 1.1 1.2 1.3 1.4 1.5	.7262 .6670 .6065 .5467 .4868 .4286 .3753 .3246	1.6 1.7 1.8 1.9 2.0 2.2 2.4 2.6	.2780 .2357 .1979 .1645 .1353 .0889 .0561	2.8 3.0 3.2 3.4 3.6 3.8 4.0 5.0	.0198 .0111 .0060 .0031 .0015 .0007 .0003

IV.—TABLE OF VALUES OF THE NORMAL PROBABILITY INTEGRAL CORRESPONDING TO VALUES OF $\frac{x}{\sigma}$; OR THE FRACTION OF THE AREA OF THE CURVE BETWEEN THE LIMITS 0 AND $+\frac{x}{\sigma}$ OR 0 AND $-\frac{x}{\sigma}$.

Total area of curve assumed to be 10000.

x = deviation from mean. $\sigma =$ standard deviation.

<u>π</u> σ	0	1	2	3	4	5	6	7	8	9	Δ
0.0	0000	0040	0080	0120	0160	0200	0239	0279	0319	0359	40
0.1	0399	0438	0478	0517	0557	0597	0636	0676	0715	0754	40
0.2	0793	0832	0871	0910	0948	0987	1026	1064	1103	1141	39
0.3	1179	1217	1255	1293	1330	1368	1406	1443	1480	1517	38
0.4	1554	1591	1628	1664	1700	1737	1773	1808	1844	1879	36
0.5	1915	1950	1985	2020	2054	2089	2124	2157	2191	2225	34
0.6	2258	2291	2324	2357	2389	2422	2454	2486	2518	2549	32
0.7	2581	2612	2643	2672	2704	2734	2764	2794	2823	2853	30
0.8	2882	2910	2939	2967	2995	3023	3051	3078	3106	3133	28
0.9	3160	3186	3212	3238	3264	3290	3315	3340	3365	3389	26
1.0	3414	3438	3461	3485	3509	3532	3555	3577	3600	3622	23
1.1	3644	3665	3686	3708	3729	3750	3770	3791	3811	3830	21
1.2	3850	3869	3888	3906	3925	3944	3962	3980	3997	4015	19
1.3	4032	4049	4066	4083	4099	4115	4132	4147	4162	4178	17
1.4	4193	4208	4222	4237	4251	4265	4279	4292	4306	4319	14
1.5	4332	4345	4358	4370	4383	4395	4406	4418	4429	4441	12
1.6	4452	4463	4174	4485	4496	4506	4516	4526	4536	4545	10
1.7	4554	4564	4573	4582	4591	4600	4608	4617	4625	4633	9
1.8	4641	4648	4656	4664	4671	4678	4686	4693	4700	4706	7
1.9	4713	4720	4726	4732	4738	4744	4750	4756	4762	4767	6
2.0	4773	4778	4783	4788	4794	4799	4804	4808	4813	4817	5
2.1	4822	4826	4830	4834	4838	4842	4846	4850	4854	4858	4
2.2	4861	4865	4868	4872	4875	4878	4881	4884	4887	4890	3
2.3	4893	4896	4899	4901	4904	4906	4909	4911	4914	4916	3
2.4	4918	4921	4923	4925	4927	4929	4931	4933	4935	4936	2
2.5 2.6 2.7 2.8 2.9	4938 4953 4966 4975 4982	4940 4955 4967 4975 4982	4942 4956 4968 4976 4983	4943 4958 4969 4977 4983	4945 4959 4970 4978 4984	4946 4960 4970 4978 4984	4947 4961 4971 4979 4985	4949 4962 4972 4980 4985	4951 4964 4973 4981 4986	4952 4965 4974 4981 4986	2 1 0.5 0.5
3 ∞	4987 5000	4991	4993	4995	4997	4998	4999	4999	4999	5000	

V.—TABLE OF LOG Γ FUNCTIONS OF p.

p	0	1	2	3	4	5	6	7	8	9
1.00 1.01 1.02 1.03 1.04	9.997529 5128 2796 0533	9750 7285 4892 2567 0311	9500 7043 4656 2328 0089	9251 6801 4421 2110 9868	9003 6560 4187 1883 9647	8755 6320 3953 1656 6427	8509 6080 3721 1430 9208	8263 5841 3489 1205 8989	8017 5602 3257 0981 8772	7773 536 5 3026 0775 8554
1.05	9.988338	8122	7907	7692	7478	7265	7052	6841	6629	6419
1.06	6209	6000	5791	5583	5378	5169	4963	4758	4553	4349
1.07	4145	3943	3741	3539	3338	3138	2939	2740	2541	2344
1.08	2147	1951	1755	1560	1365	1172	0978	0786	0594	0403
1.09	0212	0022	6833	9644	9456	6269	6082	8900	8710	8525
1.10	9.978341	8157	7974	7791	7610	7428	7248	7068	6888	6709
1.11	6531	6354	6177	6000	5825	5650	5475	5301	5128	4955
1.12	4783	4612	4441	4271	4101	3932	3764	3596	3429	3262
1.13	3096	2931	2766	2602	2438	2275	2113	1951	1790	1629
1.14	1469	1309	1150	0992	0835	0677	0521	0365	0210	0055
1.15	9.969901	9747	9594	9442	9290	9139	8988	8838	8688	8539
1.16	8390	8243	8096	7949	7803	7658	7513	7369	7225	7082
1.17	6939	6797	6655	6514	6374	6234	6095	5957	5818	5681
1.18	5544	5408	5272	5137	5002	4868	4734	4601	4469	4337
1.19	4205	4075	3944	3815	3686	3557	3429	3302	3175	3048
1.20	2922	2797	2672	2548	2425	2302	2179	2057	1936	1815
1.21	1695	1575	1456	1337	1219	1101	0984	0867	0751	0636
1.22	0521	0407	0293	0180	0067	9955	8843	9732	9621	9511
1.23	9.959401	9292	9184	9076	8968	8861	8755	8649	8544	8439
1.24	8335	8231	8128	8025	7923	7821	7720	7620	7520	7420
1.25	7321	7223	7125	7027	6930	6834	6738	6642	6547	6453
1.26	6359	6267	6173	6081	5989	5898	5807	5716	5627	5537
1.27	5449	5360	5273	5185	5099	5013	4927	4842	4757	4673
1.28	4589	4506	4423	4341	4259	4178	4097	4017	3938	3858
1.29	3780	3702	3624	3547	3470	3394	3318	3243	3168	3094
1.30	3020	2947	2874	2802	2730	2659	2588	2518	2448	2379
1.31	2310	2242	2174	2106	2040	1973	1907	1842	1777	1712
1.32	1648	1585	1522	1459	1397	1336	1275	1214	1154	1094
1.33	1035	0977	0918	0861	0803	0747	0690	0634	0579	0524
1.34	0470	0416	0362	0309	0257	0205	0153	0102	0051	0001
1.35	9. 949951	9902	9853	9805	9757	9710	9663	9617	9571	9525
1.36	9480	9435	9391	9348	9304	9262	9219	9178	9136	9095
1.37	9054	9015	8975	8936	8898	8859	8822	8785	8748	8711
1.38	8676	8640	8605	8571	8537	8503	8470	8437	8405	8373
1.39	8342	8311	8280	8250	8221	8192	8163	8135	8107	8080
1.40	8053	8026	8000	7975	7950	7925	7901	7877	7854	7831
1.41	7808	7786	7765	7744	7723	7703	7683	7664	7645	7626
1.42	7608	7590	7573	7556	7540	7524	7509	7494	7479	7465
1.43	7451	7438	7425	7413	7401	7389	7378	7368	7358	7348
1.44	7338	7329	7321	7312	7305	7298	7291	7284	7278	7273
1.45	7268	7263	7259	7255	7251	7248	7246	7244	7242	7241
1.46	7240	7239	7239	7240	7241	7242	7243	7245	7248	7251
1.47	7254	7258	7262	7266	7271	7277	7282	7289	7295	7302
1.48	7310	7317	7326	7334	7343	7353	7363	7373	7384	7395
1.49	7407	7419	7431	7444	7457	7471	7485	7499	7515	7529

TABLE OF LOG Γ FUNCTIONS.

V.—TABLE OF LOG I FUNCTIONS OF p.

p	0	1	2	3	4	5	6	7	s	9
1.50	9.947545	7561	7577	7594	7612	7629	7647	7666	76°5	7704
1.51	7724	7744	7764	7785	7806	7828	7850	7873	7896	7919
1.52	7943	7967	7991	8016	8041	8067	8093	8120	8146	8174
1.53	8201	8929	8258	8287	8316	8346	8376	8406	8437	8468
1.54	8500	8532	8564	8597	8630	8664	8698	8732	8767	8802
1.55	8837	8873	8910	8946	8983	9021	9059	9097	9135	9174
1.56	9214	9254	9294	9334	9375	9417	9458	9500	9543	9586
1.57	9629	9672	9716	9761	9806	9851	9896	9942	9989	6035
1.58	9.950082	0130	0177	0225	0274	0323	0372	0422	0472	0599
1.59	0573	0624	0676	0728	0780	0833	0886	0939	0993	1047
1.60	1102	1157	1212	1268	1324	1380	1437	1494	1552	1610
1.61	1668	1727	1786	1845	1905	1965	2025	2086	2147	2209
1.62	2271	2333	2396	2459	2522	2586	2650	2715	2780	2845
1.63	2911	2977	3043	3110	3177	3244	3312	3380	3449	3517
1.64	3587	3656	3726	3797	3867	3938	4010	4081	4154	4226
1.65	4299	4372	4446	4519	4594	4668	4743	4819	4894	4970
1.66	5047	5124	5201	5278	5356	5434	5513	5592	5671	5740
1.67	5830	5911	5991	6072	6154	6235	6317	6400	6482	6566
1.68	6649	6733	6817	6901	6986	7072	7157	7243	7322	7416
1.69	7503	7590	7678	7766	7854	7943	8032	8122	8211	8301
1.70	8391	8482	8573	8664	8756	8848	8941	9034	9127	9220
1.71	9314	9409	9502	9598	9693	9788	9884	9980	6077	6174
1.72	9.960271	0369	0467	0565	0664	0763	0862	0961	1061	1162
1.73	1262	1363	1464	1566	1668	1770	1873	1976	2079	2183
1.74	2287	2391	2496	2601	2706	2812	2918	3024	3131	3238
1.75	3345	3453	3561	3669	3778	3887	3996	4105	4215	4326
1.76	4436	4547	4659	4770	4882	4994	5107	5220	533 3	5447
1.77	5561	5675	5789	5904	6019	6135	6251	6367	6484	6600
1.78	6718	6835	6953	7071	7189	7308	7427	7547	7666	7787
1.79	7907	8023	8149	8270	8392	8514	8636	8759	8882	9005
1.80	9129	9253	9377	9501	9626	9751	9877	6008	6129	6255
1.81	9.970383	0509	0637	0765	0893	1021	1150	1279	1408	1538
1.82	1668	1798	1929	2060	2191	2322	2454	2586	2719	2852
1.83	2985	3118	3252	3386	3520	3655	3790	3025	4061	4197
1.84	4333	4470	4606	4744	4881	5019	5157	5295	5434	5573
1.85	5712	5852	5992	6132	6273	6414	6555	6697	6838	6980
1.86	7123	7266	7408	7552	7696	7840	7984	8128	8273	8419
1.87	8564	8710	8856	9002	9149	9296	9443	9591	9739	9887
1.88	9.980036	0184	03 3 3	0483	0633	0783	0933	1084	1234	1386
1.89	1537	1689	1841	1994	2147	2299	2453	2607	2761	2915
1.90	3069	3224	3379	3535	3690	3846	4003	4159	4316	4474
1.91	4631	4789	4947	5105	5264	5423	5582	5742	5902	6062
1.92	6223	6383	6544	6706	6867	7029	7192	7354	7517	7680
1.93	7844	8007	8171	8336	8500	8665	8830	8996	9161	9327
1.94	9494	9660	9827	9995	6162	6330	6498	6666	6835	1004
1.95	9.991173	1343	1512	1683	1853	2024	2195	2366	2537	2709
1.96	2881	3054	3227	3399	3573	3746	3920	4094	4269	4443
1.97	4618	4794	4969	5145	5321	5498	5674	5851	6029	6206
1.98	6384	6562	6740	6919	7078	7277	7457	7637	7817	7997
1.99	8178	8359	8540	8722	8903	9085	9268	9450	9633	9816

VI.—TABLE OF REDUCTION FROM COMMON TO METRIC SYSTEM.

	Inches to Millimeters.								
	1	2	3	4	5	6	7	8	9
10 20 30 40 50 60 70 80 90	25.40 279.40 533.39 787.39 1041.4 1295.4 1549.4 1803.4 2057.4 2311.4	50.80 304.80 558.79 812.79 1066.8 1320.8 1574.8 1828.8 2082.8 2336.8	76.20 330.19 584.19 838.19 1092.2 1346.2 1600.2 1854.2 2108.2 2362.2	355.59 609.59	127.00 380.99 634.99 888.99 1143.0 1397.0 1651.0 1905.0 2159.0 2413.0	152.40 406.39 660.39 914.39 1168.4 1422.4 1676.4 1930.4 2184.4 2438.4	177.80 431.79 685.79 939.78 1193.8 1447.8 1701.8 1955.8 2209.8 2463.8	203.20 457 19 711.19 965.18 1219.2 1473.2 1727.2 1981.2 2235.2 2489.2	228.60 482.59 736.59 990.58 1244.6 1498.6 1752.6 2006.6 2260.6 2514.6
-	Twel	fths.				Sixteen	nths.		
1/12 2/12 3/12 4/12 5/12 6/12	4.23 6.35 8.47 10.58	8/12 1 9/12 1 10/12 2 11/12 2	$ \begin{array}{c c} 6.93 & 1 \\ 9.05 & 3 \end{array} $	/16 1.59 /8 3.17 /16 4.76 /4 6.35	3/8 7/16	7.94 9.52 11.11 12.70	5/8 15 11/16 17	13/1 1.87 1.46 1.05	$8 \mid 22.22 \mid$

TABLE VII.—FIRST TO SIXTH POWERS OF INTEGERS FROM 1 TO 30.

	Powers,						
First.	Second.	Third.	Fourth.	Fifth.	Sixth.		
1	1	1	1	1	1		
2	4	8	16	32	64		
3	9	27	81	243	729		
4	16	64	256	1024	4096		
5	25	125	625	3125	15625		
6	36	216	1296	7776	46656		
7	49	343	2401	16807	117649		
8	64	512	4096	32768	262144		
9	81	729	6561	59049	531441		
10	100	1000	10000	100000	1000000		
11	121	1331	14641	161051	1771561		
12	144	1728	20736	248832	2985984		
13	169	2197	28561	371293	4826809		
14	196	2744	38416	537824	7529536		
15	225	3375	50625	759375	11390625		
16	256	4096	65536	1048576	16777216		
17	289	4913	83521	1419857	24137569		
18	324	5832	104976	1889568	34012224		
19	361	6859	130321	2476099	47045881		
20	400	8000	160000	3200000	64000000		
21	441	9261	194481	4084101	85766121		
22	484	10648	234256	5153632	113379904		
23	529	12167	279841	6436343	148035889		
24	576	13824	331776	7962624	191102976		
25	625	15625	390625	9765625	244140625		
26	676	17576	456976	11881376	308915776		
27	729	19683	531441	14348907	387420489		
28	784	21952	614656	17210368	481890304		
29	841	24389	707281	20511149	594823321		
30	900	27000	810000	24300000	729000000		

TABLE VIII.—SQUARES, CUBES, SQUARE ROOTS.

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
1 2 3 4 5 6 7 8 9	1 4 9 16 25 36 49 64 81	1 8 27 64 125 216 343 512 729	1.0000000 1.4142136 1.7320508 2.0000000 2.2360680 2.4494897 2.6457513 2.8284271 3.0000000	1.0000000 1.2599210 1.4422496 1.5874011 1.7099759 1.8171206 1.9129312 2.0000000 2.0800837	1.000000000 .50000000 .33333333 .250000000 .20000000 .16666667 .142857143 .125000000
10 11 12 13 14 15 16 17 18	100 121 144 169 196 225 256 289 324 361	1000 1331 1728 2197 2744 3375 4096 4913 5832 6859	3.1692777 3.3166248 3.4641016 3.6055513 3.7416574 3.8729833 4.0000000 4.1231056 4.2426407 4.3585989	2.1544347 2.2239801 2.2894286 2.3513347 2.4101422 2.4662121 2.5712816 2.6207414 2.6684016	.10000000 .090909091 .08333333 .076923077 .071428571 .066666667 .06250000 .058823529 .05555556
20 21 22 23 24 25 26 27 28 29	400 441 484 529 576 625 676 729 784 841	8000 9261 10648 12167 13824 15625 17576 19683 21952 24389	4,4721360 4,5825757 4,6904158 4,7958315 4,8989795 5,0000000 5,0990195 5,1961524 5,2915026 5,3851648	2.7144177 2.7589243 2.8020393 2.8438670 2.8844991 2.9240177 2.9624960 3.0000000 3.0365889 3.0723168	.05000000 .047619048 .045454545 .043478261 .041666667 .04000000 .038461538 .037037037 .035714286 .034482759
30 31 32 33 34 35 36 37 38 39	900 961 1024 1089 1156 1225 1296 1369 1444 1521	27000 29791 32768 35937 39304 42875 46656 50653 54872 59319	5.4772256 5.5677644 5.6568542 5.7445626 5.8309519 5.9160798 6.0000000 6.0827625 6.1644140 6.2449980	3.1072325 3.1413806 3.1748021 3.2075243 3.2075243 3.2376118 3.2710663 3.3019272 3.3322218 3.3619754 3.3912114	.03333333 .032258065 .031250000 .03030303 .029411765 .028571429 .027777778 .027027027 .026315789 .025641026
40 41 42 43 44 45 46 47 48 49	1600 1681 1764 1849 1936 • 2025 2116 2209 2304 2401	64000 68921 74088 79507 85184 91125 97336 103823 110592 117649	6.3245553 6.4031242 6.4807407 6.5574385 6.6332496 6.7082039 6.7823300 6.8556546 6.9282032 7.0000000	3.4199519 3.4482172 3.4760266 3.5033981 3.5303483 3.5568933 3.5830479 3.6088261 3.6342411 3.6593057	.025000000 .024390244 .023809524 .023255814 .022727273 .02222222 .021739130 .021276000 .020833333 .020408163
50 51 52 53 54 55 56 57 58 59	2500 2601 2704 2809 2916 3025 3136 3249 3364 3481	125000 132651 140608 148877 157464 166375 175616 185193 195112 205379	7.0710678 7.1414284 7.2111026 7.2801099 7.3484692 7.4161985 7.4833148 7.5498344 7.6157731 7.6811457	3.6840314 3.7084298 3.7325111 3.7562858 3.7797631 3.8029525 3.8258624 3.8485011 3.8708766 3.8929965	.020000000 .019607843 .019230769 .018867925 .018518519 .018181818 .017857143 .017543860 .017241879 .016949153
60 61 62	3600 3721 3844	216000 226981 238328	7.7459667 7.8102497 7.8740079	3.914867 6 3.936497 2 3.9578915	.016666667 .016393443 .016129032

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
63	3969	250047	7.9372539	3.9790571	.015873016
64	4096	262144	8.0000000	4.0000000	.015625000
65	4225	274625	8.0622577	4.0207256	.015384615
66	4356	287496	8.1240384	4.0412401	.015151515
67	4489	300763	8.1853523	4.0615480	.014925373
68	4624	314432	8.2462113	4.0816551	.014705882
69	4761	328509	8.3066239	4.1015661	.014492754
70 71 72 73 73 74 75 75 75 75 75 75 75 75 75 75 75 75 75	4900 5041 5184 5329 5476 5625 5776 5929 6084 6241	343000 357911 373248 389017 405224 421875 438976 456533 474552 493039	8.3666003 8.4261498 8.4852814 8.5440037 8.6023253 8.6602540 8.7177979 8.7749644 8.8317609 8.8881944	4.1212853 4.1408178 4.1601676 4.1793390 4.1983364 4.2171633 4.23582310 4.2543210 4.2726586 4.2908404	.014985714 .014084507 .013888889 .013698630 .013513514 .013333333 .013157895 .012987013 .012820513 .012658228
80	6400	512000	8.9442719	4.3088695	.012500000
81	6561	531441	9.0000000	4.3267487	.012345679
82	6724	551368	9.0553851	4.3444815	.012195122
83	6889	571787	9.1104336	4.3620707	.612048193
84	7056	592704	9.1651514	4.3795191	.011904762
85	7225	614125	9.2195445	4.3968296	.011764706
86	7396	636056	9.2736185	4.4140049	.011627907
87	7569	658503	9.3273791	4.4310476	.011494253
88	7744	681472	9.3808315	4.4479602	.011863636
89	7921	704969	9.4339811	4.4647451	.011235955
90	8100	729000	9.4868330	4.4814047	.01111111
91	8281	753571	9.5393920	4.4979414	.010989011
92	8464	778688	9.5916630	4.5143574	.010899565
93	8649	804357	9.6436508	4.5306549	.010752688
94	8836	830584	9.6953597	4.5468359	.010638298
95	9025	857375	9.7467943	4.5629026	.010526316
96	9216	884736	9.7979590	4.5788570	.010416667
96	9409	912673	9.8488578	4.5947009	.010309278
97	9604	941192	9.8994949	4.6104363	.010204082
98	9801	970299	9.9498744	4.0260650	.010101010
100	10000	1000000	10,0000000	4.6415888	.01000000
101	10201	1030301	10,0498756	4.6570095	.009000990
102	10404	1061208	10,0995049	4.6733287	.009009990
103	10609	1092727	10,1488916	4.6875482	.00971538
104	10816	1124864	10,1980300	4.7026694	.00961535
105	11025	1157625	10,2469508	4.7176940	.009523810
106	11236	1191016	10,2956301	4.7326235	.009433962
107	11449	1225043	10,3440804	4.7474594	.009345794
108	11664	1259712	10,3923048	4.7622032	.00 .259259
109	11881	1295029	10,4403065	4.7768562	.009174312
110 111 112 113 114 115 116 117 118	19100 12321 12544 12769 12996 13225 13456 13689 13924 14161	1331000 1367631 1404928 1442897 1441897 150875 1560896 1601613 1643032 1685159	10.4880865 10.5356538 10.5830052 10.6301458 10.770783 10.7238053 10.7703296 10.8166538 10.8627805 10.9087121	4.7914199 4.8058955 4.8202845 4.8345881 4.8488076 4.8629442 4.8769990 4.8909732 4.9048681 4.9186847	.009090909 .009090009 .0089285.1 .008819558 .008771930 .008695652 .008620690 .008547009 .008474576 .008403361
120	14400	1728000	10.9544512	4.9324242	.008333333
121	14641	1771561	11.00J0000	4.9460874	.008264463
122	14884	1815848	11.0453610	4.9596757	.008196721
123	15129	1860867	11.0905365	4.9731898	.008130081
124	15376	1906624	11.1355287	4.9866310	.008064516

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
125 126 127 128 129	15625 15876 16129 16384 16641	1953125 2000376 2048383 2097152 2146689	11.1803399 11.2249722 11.2694277 11.3137085 11.3578167	5.0000000 5.0132979 5.0265257 5.0396842 5.0527743	.008000000 .007936508 .007874016 .007812500 .007751938
130 131 132 133 134 135 136 137 138	16900 17161 17424 17689 17956 18225 18496 18769 19044 19321	2197000 2248091 2299968 2352637 2406104 2460375 2515456 2571353 2628072 2685619	11.4017543 11.4455231 11.4891253 11.5325626 11.5738369 11.6189500 11.6619038 11.7046999 11.7473401 11.788261	5.0657970 5.0787531 5.0916434 5.1044687 5.1173299 5.1299278 5.1425632 5.1551367 5.1676493 5.1801015	.007692308 .007633588 .007575758 .007518797 .007462687 .007407407 .007352941 .007299270 .007246377 .007194245
140 141 142 143 144 145 146 147 148 149	19600 19881 20164 20449 20736 21025 21316 21609 21904 22201	2744000 2803221 2863288 2924207 2985984 3048625 3112136 3176523 3241792 3307949	11.8321596 11.8743421 11.9163753 11.9582607 12.0000000 12.0415946 12.0830460 12.1243557 12.1655251 12.2065556	5.1924941 5.2048279 5.2171034 5.2298215 5.2414828 5.2535879 5.2656374 5.2776321 5.2895725 5.3014592	.007142857 .007092199 .007042254 .006993007 .006944444 .006896552 .006849315 .006802721 .006756757 .006711409
150 151 152 153 154 155 156 157 158 159	22500 22801 23104 23409 23716 24025 24336 24649 24964 25281	3375000 3442951 3511808 3581577 3652264 3723875 3796416 3869893 3944312 4019679	12.2474487 12.2882057 12.3288280 12.3693169 12.4096736 12.4498996 12.489960 12.5299641 12.5698051 12.6095202	5.3132928 5.3250740 5.3368033 5.3484812 5.3601084 5.3716854 5.3832126 5.3946907 5.4061202 5.4175015	.006666667 .006622517 .006578947 .006578947 .006535948 .006493506 .006451613 .006410256 .006369427 .006329114 .006289308
160 161 162 163 164 165 166 167 168 169	25600 25921 26244 26569 26896 27225 27556 27556 27889 28224 28561	4096000 4173281 4251528 4330747 4410944 4492125 4574296 4657463 4741632 4826809	12.6491106 12.6855775 12.727921 12.7671458 12.8062485 12.8452326 12.8840987 12.9228480 12.9614814 13.0000000	5,4288352 5,4401218 5,4513618 5,4625556 5,4737037 5,4848066 5,4958647 5,5068784 5,5178484 5,5287748	.006250000 .006211180 .006172840 .006134969 .006097561 .006060606 .0069824096 .005985024 .005952381 .005917160
170 171 172 173 174 175 176 177 178 179	28900 29241 29584 29929 30276 30625 30976 31329 31684 32041	4913000 5000211 5088448 5177717 5268024 5359375 5451776 5545233 5689752 5735339	13.03\$4048 13.0766968 13.1148770 13.1529464 13.1909060 13.2287566 13.2664992 13.3041347 13.3416641 13.3790882	5.5396583 5.5504991 5.5612978 5.5720546 5.5827702 5.5934447 5.6040787 5.6146724 5.6252363 5.6357408	.005882353 .005847953 .005817953 .005813953 .005747126 .005714286 .00561818 .005647718 .005617978 .005586592
180 181 182 183 184 185 186	32400 32761 33124 33489 33856 34225 34596	5832000 5929741 6028568 6128487 6229504 6331625 6434856	13.4164079 13.4536240 13.4907376 13.5277493 13.5646600 13.6014705 13.6381817	5.6462162 5.6566528 5.6670511 5.6774114 5.6877340 5.6980192 5.7082675	.00555556 .005524862 .005494505 .005464481 .005434783 .005405405 .005376344

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
187	34969	6539203	13.6747943	5.7184791	.005347594
188	35344	6644672	13.7113092	5.7286543	.005319149
189	35721	6751269	13.7477271	5.7387936	.005291005
190	36100	6859000	13.7840488	5.7488971	.005263158
191	36481	6967871	13.8202750	5.7589652	.005235602
192	36864	7077888	13.8564065	5.7689982	.005208333
193	37249	7189057	13.8924440	5.7789966	.005181347
194	37636	7301384	13.9283883	5.7889604	.005154639
195	38025	7414875	13.9642400	5.7988900	.005128205
196	38416	7529536	14.0000000	5.8087857	.005102041
197	38809	7645373	14.0356688	5.8186479	.005076142
198	39204	7762392	14.0712473	5.8284767	.0050750505
199	39601	7880599	14.1067360	5.8282725	.005025126
200	40000	8000000	14.1421356	5.8480355	.005000000
201	40401	8120601	14.1774469	5.8577660	.004975124
202	40804	8242408	14.2126704	5.8674643	.004950495
203	41209	8365427	14.2478068	5.8771307	.004926108
204	41616	8489664	14.2828569	5.8867653	.004901961
205	42025	8615125	14.3178211	5.8963685	.004878049
206	42436	8741816	14.3527001	5.9059406	.004854369
207	42849	8869743	14.3874946	5.9154817	.004830918
208	43264	8998912	14.4222051	5.9249921	.004807692
209	43681	9129829	14.4568323	5.9344721	.004784689
210 211 212 213 214 215 216 217 218 219	44100 44521 44944 45369 45796 46225 46656 47089 47524 47961	9361000 9393931 9528128 9663597 9800344 9938875 10077696 10218313 10360232 10503459	14.4913767 14.5258390 14.5602198 14.5945195 14.6287388 14.6969385 14.7309199 14.7648231 14.7986486	5.9439220 5.9533418 5.9627320 5.9720926 5.9814240 5.9907264 6.000000 6.0092450 6.0184617 6.0276502	.004761905 .004739336 .004716981 .004694836 .004678897 .004651163 .004629630 .00468295 .004587156
220	48400	10648000	14.8323970	6.0368107	.004545455
221	48841	10793861	14.8660687	6.0459435	.004524887
222	49284	10941048	14.8996644	6.0550489	.004504505
223	49729	11089567	14.9331845	6.0641270	.00448430 5
224	50176	11239424	14.9666295	6.0731779	.004464286
225	50625	11390625	15.0000000	6.0822020	.00444444
226	51076	11543176	15.0332964	6.0911994	.004424779
227	51529	11697083	15.0665192	6.1001702	.004405286
228	51984	11852352	15.0996689	6.1091147	.004385965
229	52441	12008989	15.1327460	6.1180332	.004366812
230	52900	12167000	15.1657509	6.1269257	.004347826
231	53361	12326391	15.1986842	6.1357924	.004329004
232	53824	12487168	15.2315462	6.1446337	.004310345
233	54289	12649337	15.2643375	6.1534495	.004291845
234	54756	12812904	15.2970585	6.1622401	.004273504
235	55225	12977875	15.3297097	6.1710058	.004255319
236	55696	13144256	15.3622915	6.1797466	.004237288
237	56169	13312053	15.3948043	6.1884628	.004219409
238	56644	13481272	15.4272486	6.1971544	.004201681
239	57121	13651919	15.456248	6.2058218	.004184100
240	57600	13824000	15.4919334	6.2144650	.004166667
241	58081	13997521	15.5841747	6.2230843	.004149378
242	58564	14172488	15.5563492	6.2316797	.004132331
243	59049	14348907	15.5884573	6.2402515	.004115226
244	59536	14526784	15.6204994	6.2487998	.004098361
245	60025	14706125	15.6524758	6.2573248	.004081633
246	60516	14886936	15.6843871	6.2658266	.004065041
247	61009	15009223	15.7162336	6.2748054	.004048583
248	61504	15252992	15.7480157	6.2827613	.004032258

TABLE VIII.—SQUARES, CUBES, SQUARE ROOTS.

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
249	62001	15438249	15.7797338	6.2911946	.004016064
1	00=00	15625000	15.8113883	6.2996053	.004000000
250	62500 63001	15813251	15.8429795	6.3079935	.003984064
251	63504	16003008	15.8745079	6.3163596	.003968254
252 253	64009	16194277	15.9059737	6.3247035	.003952569
254	64516	16387064	15.9373775	6.3330256	.003937008
255	65025	16581375	15.9687194	6.3413257	.003921569
256	65536	16777216	16.0000000	6.3496042	.003906250
257	66049	16974593	16.0312195	6.3578611	.003891051
258	66564	17173512	16.0623784	6.3660968	.003875969
259	67081	17373979	16.0934769	6.3743111	.003861004
260	67600	17576000	16.1245155	6.3825043	.003846154
261	68121	17779581	16.1554944	6.3906765	.003831418
262	68644	17984723	16.1864141	6.3988279	.003816794
263	69169	18191447	16.2172747	6.4069585	.003802281
264	69696	18399744	16.2480768	6.4150687	.003787879
265	70225	18609625	16.2788206	6.4231583	.003773585
266	70756	18821096	16.3095064	6.4312276	.003759398
267	71289	19034163	16.3401346	6.4392767	.003745318
268	71824	19248832	16.3707055	6.4473057	.003731343
269	72361	19465109	16.4012195	6.4553148	.003717472
270	72900	19683000	16.4316767	6.4633041	.003703704
271	73441	19902511	16.4620776	6.4712736	.003690037
272	73984	20123648	16.4924225	6.4792236	.003676471
273	7452)	20346417	16.5227116	6.4871541	.003663004
274	75076	20570824	16.5529454 16.5831240	6.4950653	.003649635
275 276	75625	20796875 21024576	16.6132477	6.5029572 6.5108300	.003623188
277	76176 76729	21253933 .	16.6433170	6.5186839	.003610108
278	77284	21484952	16.6733320	6.5265189	.003597122
279	77841	21717639	16,7032931	6.5343351	.003584229
280	78400	21952000	16,7332005	6.5421326	.003571429
281	78961	22188041	16.7630546	6.5499116	.003558719
282	79524	22425768	16,7928556	6.5576722	.003546099
283	80089	22665187	16.8226038	6.5654144	.003533569
284	80656	22906304	16.8522995	6.5731385	.003521127
285	81225	23149125	16.8819430	6.5808443	.003508772
286	81796	23393656	16.9115345	6.5885323	.003496503
287	82369	23639903	16.9410743	6.5962023 6.6038545	.003484321
288 289	82944 83521	23887872 24137569	16.9705627 17.0000000	6.6114890	.003472222
290	84100	24389000	17.0293864 17.0587221	6.6191060 6.6267054	.003448276
291 292	84681 85264	24642171 24897088	17.0880075	6.6342874	.003436426
293	85849	25153757	17.1172428	6.6418522	.003412969
294	86436	25412184	17.1464282	6.6493998	.003401361
295	87025	25672375	17.1755640	6.6569302	.003389831
296	87616	25934336	17.2046505	6.6644437	.003378378
297	88209	26198073	17.2336879	6.6719403	.003367003
298	88804	26463593	17.2626765	6.6794200	.003355705
299	89401	26730899	17.2916165	6.6868831	.003344482
300	90000	27000000	17.3205081	6.6943295	.003333333
301	90601	27270901	17.3493516	6.7017593	.003322259
302	91204	27543608	17.3781472	6.7091729	.003311258
303	91809 92416	27818127 28094464	17.4068952 17.4355958	6.7165700 6.7239508	.003300330
305	93025	28372625	17.4642492	6.7313155	.003278689
306	93636	28652616	17.4928557	6.7386641	.003267974
307	94249	28934443	17.5214155	6.7459967	.003257329
308	94864	29218112	17.5499288	6.7533134	.003246753
309	95481	29503629	17.5783958	6.7606143	.003236246
310	96100	29791000	17.6068169	6.7678995	.003225806

CUBE ROOTS, AND RECIPROCALS.

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
311 312 313 314 315 316 317 318 319	96721 97344 97969 98596 99225 99856 100489 101124 101761	30080231 30371328 30664297 30959144 31255875 31554496 31855013 32157432 32461759	17.6351921 17.6635217 17.6918060 17.7200451 17.7482393 17.7763888 17.8044938 17.8605711	6.7751690 6.7824329 6.7896613 6.7968844 6.8040921 6.8112847 6.8184620 6.8256242 6.8327714	.003215434 .003205128 .003194888 .003194713 .003164557 .003164557 .003154574 .003144654 .003134796
320 321 322 323 324 324 325 326 327 328 329	102400 103041 103684 104329 104976 105625 106276 106929 107584 108241	32768000 33076161 33386248 33698267 34013224 34328125 34645976 34965783 35287552 35611289	17.885438 17.9164729 17.9443584 17.9722008 18.0000000 18.0277564 18.0554701 18.0831413 18.1107703 18.1383571	6.8399037 6.8470213 6.8541240 6.8612120 6.8682855 6.8753443 6.8823888 6.8894188 6.8964345 6.9934359	.003125000 .003115265 .003105590 .003095975 .003086420 .003076923 .003067485 .003058104 .003048780 .003039514
330 331 332 333 334 335 336 337 338 339	108900 109561 110224 110889 111556 112225 112896 113569 114244 114921	35937000 36264691 36594368 36.026037 37259704 37595375 37933056 38272753 38614472 38958219	18.1659021 18.1934054 18.2208672 18.2482876 18.2756669 18.3030052 18.3330328 18.3575598 18.3847763 18.4119526	6.9104232 6.9173964 6.9243556 6.9313008 6.9382321 6.9451496 6.9520533 6.9589434 6.9658198 6.9726826	.003030303 .003021148 .003012048 .003003003 .002994012 .002985075 .002976190 .002967359 .002949853
340 341 342 343 344 345 346 347 348 349	115600 116281 116964 117649 118336 119025 119716 120409 121104 121801	39304000 39651821 40001688 40055607 40707584 41063625 41421736 41781923 42144193 42308549	18.4390889 18.4661853 18.4932420 18.5202592 18.5472370 18.5741756 18.6010752 18.6279360 18.6547581 18.66815417	6.9795321 6.9863681 6.9931906 7.0000000 7.0067962 7.0135791 7.0203490 7.0271058 7.0338497 7.0405806	.002941176 .002932551 .002923977 .002915452 .002906977 .002898551 .00289173 .002881844 .002873563 .002865330
350 351 352 353 354 355 356 357 358 359	122500 123201 123904 124609 125316 126025 126736 127449 128164 128881	42875000 43243551 43614208 43986977 44361864 44738875 45118016 45499293 45882712 46268279	18, 7082869 18, 7349940 18, 7616630 18, 7882942 18, 8148877 18, 8414437 18, 8974436 18, 89208879 18, 9472953	7.0472987 7.0540041 7.0606967 7.0673767 7.0740440 7.0806988 7.0873411 7.0939709 7.1005885 7.1071937	.002857143 .002849003 .002840909 .002832861 .002824859 .002816901 .002808989 .002801120 .002793296 .002785515
360 361 362 363 364 365 366 367 368 369	129600 130321 131044 131769 132496 133225 133936 134689 135424 136161	46656000 47045881 47137928 47832147 482285144 48627125 49027896 49430863 49636032 50243409	18.9736660 19.0000000 19.0362976 19.0525589 19.0787840 19.1049732 19.1311265 19.1572441 19.1883261 19.2093727	7.1137866 7.1203674 7.1203660 7.1334925 7.1400370 7.1465695 7.1530901 7.1595988 7.1660957 7.1725809	.002777778 .002770683 .002762481 .002754821 .002747253 .002739726 .002732240 .0027324796 .002717391 .002710027
370 371 372	136900 137641 138384	50653000 51064811 51478848	19.2353841 19.2613603 19.2873015	7.1790544 7.1855162 7.1919663	.002702703 .002695418 .002688172

No.	Squares.	Cubes.	Square Roots,	Cube Roots.	Reciprocals.
373 374 375 376 377 378 379	139129 139876 140625 141376 142129 142884 143641	51895117 52313624 52734375 53157376 53582633 54010152 54439939	19.3132079 19.3390796 19.3649167 19.3907194 19.4164878 19.4422221 19.4679223	7.1984050 7.2048322 7.2112479 7.2176522 7.2240450 7.2304268 7.2367972	.002680965 .002673797 .002666667 .002659574 .002652520 .002645503 .002638522
380 381 382 383 384 385 386 387 388 389	144400 145161 145924 146689 147456 148225 148996 149769 150544 151321	54872000 55306341 55742968 56181887 56623104 57066625 57512456 57960603 58411072 5863869	19.4935887 19.5192213 19.5448203 19.5703858 19.5595179 19.6214169 19.6468827 19.6723156 19.6977156 19.7230829	7.2431565 7.2495045 7.2558415 7.2621675 7.2621675 7.264884 7.2747864 7.2810794 7.2873617 7.2936330 7.2998936	.002631579 .002624672 .002617801 .002610966 .002604167 .002597403 .002590674 .002583979 .002577320
390 391 392 393 394 395 396 397 398 399	152100 152881 153664 154449 155236 156025 156816 157609 158404 159201	59319000 59776471 60236288 60698457 61162984 61629875 62099136 62570773 63044792 63521199	19.7484177 19.7737199 19.7989899 19.8242276 19.8194332 19.8746069 19.8997487 19.9248588 19.9499373 19.9749844	7, 3061436 7, 3123828 7, 3186114 7, 3248295 7, 3310369 7, 3372339 7, 3434205 7, 3495966 7, 3557624 7, 3619178	.002564103 .002557545 .002551020 .002544529 .002538071 .002531646 .002525253 .002518892 .002512563
400 401 402 403 404 405 406 407 408 409	160000 160801 161604 162409 163216 164025 164836 165649 166464 167281	6400000 64481201 64964808 65450827 65939264 66430125 66923416 67419143 67917312 68417929	20.000000 20.0249844 20.0499377 20.0748599 20.0997512 20.1246118 20.1494417 20.1742410 20.1990099 20.2287484	7.3680630 7.3741979 7.3803227 7.3864373 7.3925418 7.3986363 7.4047206 7.4107950 7.4168595 7.4229142	.002500000 .002493766 .002487562 .002481390 .002475248 .002469136 .002457002 .00245980 .002444988
410 411 412 413 414 415 416 416 417 418 419	168100 168921 169744 170569 171396 172225 173056 173889 174724 175561	68921000 69426531 69934528 70444997 70957944 71473375 71991296 72511713 73034632 73560059	20.2484567 20.2731349 20.2977831 20.3224014 20.3469899 20.3715488 20.3960781 20.4205779 20.4450483 20.4694895	7.4289589 7.4349938 7.4410189 7.4470342 7.4530399 7.4650223 7.4769694 7.4829242	.002439024 .002433090 .002427184 .002421308 .002415459 .002409639 .002403846 .002398082 .002392344
420 421 422 423 424 425 426 427 428 429	176400 177341 178084 178929 179776 180625 181476 182329 183184 184041	74088000 74618461 75151448 75686967 6225024 76765625 77308776 77854483 78402752 78953589	20.4939015 20.5182845 20.5426386 20.5669638 20.5912603 20.6155281 20.6397674 20.6639783 20.6881609 20.7123152	7.4888724 7.4948113 7.5007406 7.5066607 7.5125715 7.5184730 7.5243652 7.5361221 7.5361221 7.5419867	.002380952 .002375297 .002369668 .002364066 .002352941 .002352941 .002347418 .002347418 .002340449
430 431 432 433 434	184900 185761 186624 187489 188356	79507000 80062991 80621568 81182737 81746504	20.7364414 20.7605395 20.7846097 20.8086520 20.8326667	7.5478423 7.5536888 7.5595263 7.5653548 7.5711743	.002325581 .002320186 .002314815 .002309469 .002304147

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
435	189225	82312875	20.8566536	7.5769849	.002298851
436	190096	82881856	20.8806130	7.5827865	.002293578
437	190969	83453453	20.9045450	7.5885793	.002268330
438	191844	84027672	20.9284495	7.5943633	.002283105
439	192721	84604519	20.9523268	7.6001385	.002277904
440	193600	85184000	20.9761770	7.6059049	.002272727
441	194481	85766121	21.0000000	7.6116626	.002267574
442	195364	86350888	21.0237960	7.6174116	.002262443
443	196249	86938307	21.0475652	7.6231519	.002257336
414	197136	87528384	21.0713075	7.6288837	.002252252
445	198025	88121125	21.0950231	7.6346067	.002247191
446	198916	88716536	21.1187121	7.6403213	.002242152
447	199809	89314623	21.1423745	7.6460272	.002237136
448	200704	89915392	21.1660105	7.6517247	.002232143
449	201601	90518849	21.1896201	7.6574133	.002227171
450	202500	91125000	21,2132034	7.6630943 7.6687665 7.6744303 7.6800857 7.6857328 7.6913717 7.6970023 7.7026246 7.7082388 7.7138448	.00222222
451	203401	91733851	21,2307606		.002217295
452	204304	92345408	21,2602916		.002217295
453	205209	92359677	21,2837967		.002207506
454	206116	93576664	21,3072758		.002207506
455	207025	94196375	21,3307290		.002197802
456	207936	94818816	21,3541565		.00219802
457	208849	95443993	21,3775583		.002188184
458	209764	96071912	21,4009346		.002188406
459	210681	96702579	21,4242853		.002178649
460 461 462 463 464 465 466 467 468 469	211600 212521 213444 214369 215296 216225 217156 218089 219024 219961	97336000 97972181 98611128 99252847 99897344 100544625 101194696 101847563 102503232 103161709	21.4476106 21.4709106 21.4941853 21.5174348 21.5406592 21.5638587 21.5670331 21.6101828 21.6354078	7.7194426 7.7250325 7.7306141 7.7361877 7.7417532 7.7473109 7.7528006 7.7584023 7.7030361 7.7094620	.002173913 .002169197 .002164502 .002159827 .002155172 .002150538 .002145923 .002141328 .002136752 .002132196
470	220900	103823000	21.6794834	7.7749801	.002127660
471	221841	104487111	21.7025344	7.7804904	.002123142
472	222784	105154048	21.7255610	7.7859928	.002118644
473	223729	105823817	21.7455632	7.7914875	.002114165
474	224676	106496424	21.7715411	7.7969745	.002109705
475	225625	107171875	21.7794947	7.8024538	.002105263
476	226576	107850176	21.8174242	7.8079254	.002100840
477	227529	108531333	21.8403297	7.8138892	.002096436
478	228484	109215352	21.8632111	7.8188456	.002096436
479	229441	109902239	21.8860686	7.8242942	.002087683
480 481 482 483 484 485 486 486 487 488 489	230400 231361 232324 233289 234256 235225 236196 237169 238144 239121	110592000 111284641 111980168 112678587 113379904 114084125 114791256 115501303 116214272 116930169	21.9089023 21.9317123 21.9317123 21.9544984 21.9772610 22.0000000 22.0227155 22.0454077 22.0680705 22.0907220 22.1133444	7.8297353 7.8351688 7.8405949 7.8460134 7.8514244 7.8568281 7.8622242 7.8676130 7.8729944 7.8729844	.002088333 .002079002 .002074689 .002070393 .002066116 .002057613 .002053388 .002049180
490	240100	117649000	22.1359436	7.8837352	.002040816
491	241081	118370771	22.1585198	7.8890946	.002036660
492	242064	119095488	22.1810730	7.8914468	.002032520
493	243049	119823157	22.2036033	7.8997917	.002032520
494	244036	120553784	22.2261108	7.9051294	.002024291
495	245025	121287375	22.2485955	7.9104599	.002020202
496	246016	122023936	22.2710575	7.9157832	.002016129

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
497 498 499	247009 248004 249001	122763473 123505992 124251499	22,2934968 22,3159136 22,3383079	7.9210994 7.9264085 7.9317104	.002012072 .002008032 .002004008
500 501 502 503 504 505 506 507 508 509	250000 251001 252:04 253009 254016 255025 256036 257049 258064 259081	12500000 125751501 126506008 127263527 128024064 128787625 129554216 130323843 131096512 131872229	22.3606798 22.3830293 22.4053565 22.4976615 22.4499443 22.4792051 22.4944438 22.5166605 22.5388553 22.5610283	7.9370053 7.9422931 7.9475739 7.9528477 7.9581144 7.9633743 7.9638271 7.9738731 7.9791122 7.9843444	.002000000 .001996008 .001992032 .001988072 .001984127 .001980198 .001976285 .001973387 .001964637
510 511 512 513 514 515 516 517 518 519	260100 261121 262144 263169 264196 265225 266256 267289 268324 269361	13265209 132651000 133432831 134217728 135005697 135796744 1365590875 137388096 138188413 138991832 139798359	22.5831796 22.6053091 22.6053091 22.6495083 22.6715681 22.6936114 22.7156334 22.7376340 22.7596134 22.7815715	7.9895697 7.9947883 8.0000000 8.0052049 8.0104032 8.0155946 8.0207794 8.0259574 8.0311287 8.0362935	.001904657 .001960784 .001956947 .001953125 .001949318 .001941525 .001941748 .001937984 .001934236 .001936502 .001936782
520 521 522 523 524 525 526 527 528 529	270400 271441 272484 273529 274576 275625 276676 277729 278784 279841	140608000 141420761 142236648 143055667 143877824 144703125 145521576 146303183 147197952 148035889	22.8035085 22.8254244 22.8473193 22.8691933 22.8910463 22.9128785 22.9346899 22.9564806 22.9782506 23.0000000	8.0414515 8.0466030 8.0517479 8.0568862 8.0620180 8.0671432 8.0722620 8.0773743 8.0824800 8.08575794	.001923077 .001919386 .001915709 .001912046 .001908307 .001904762 .001901141 .001897533 .001893399 .001890359
530 531 532 533 534 535 536 537 538 539	280900 281961 283024 284089 285156 286225 287296 288369 289444 290521	148877000 149721291 150568768 151419437 152273304 153130375 153990656 154854153 155720872 156590819	23.0217289 23.0434372 23.0651252 23.0867928 23.1084400 23.1516738 23.1732605 23.1948270 23.2163735	8.0926723 8.0977589 8.1028390 8.1079128 8.1129803 8.1180414 8.1230962 8.1281447 8.1331870 8.1382230	.001886792 .001883239 .001879699 .001876173 .001872659 .001865672 .001863197 .00185236 .0018538736
540 541 542 543 544 545 546 547 548 549	291600 292681 293764 294849 295936 297025 298116 299209 300304 301401	157464000 158340421 159220088 167103007 160989184 161878625 162771336 163667323 164566592 165469149	23.2379001 23.2594067 23.2808935 23.3023604 23.3238076 23.3452351 23.3666429 23.3880311 23.4003998 23.4307490	8.1432529 8.1482765 8.1532939 8.1583051 8.1683102 8.1683092 8.1733020 8.1782888 8.1832695 8.1882441	.001851852 .001848429 .001845018 .001841621 .001838235 .001834862 .001831502 .00182154 .001824518
550 551 552 553 554 555 556 557 558	302500 303601 304704 305809 306916 308025 309136 310249 311364	166375000 167284151 168196608 169112377 170031464 170953875 171879616 172808693 173741112	23.4520788 23.4733802 23.4946802 23.5150520 23.5372046 23.5584380 23.5796522 23.6008474 23.6220236	8.1932127 8.1981752 8.2031319 8.2090825 8.2130271 8.2179657 8.2228985 8.2278254 8.2327463	.001818182 .001814882 .001811594 .001805318 .001805054 .001801802 .001798561 .001795332 .001792115

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
559	312481	174676879	23.6431808	8.2376614	001788909
560 561 562 563 564 565 566 567 568 569	313600 314721 315844 316969 318096 319225 320356 321489 322624 323761	175616000 176558481 177504328 178453547 179406144 180362125 181321496 182284263 183250432 184220000	23.6648191 23.6854386 23.7065392 23.7276210 23.7486842 23.7697286 23.7907545 23.8117618 23.8327506 25.8537209	8.2425706 8.2471740 8.2523715 8.2572633 8.2621492 8.2670294 8.2719039 8.2767726 8.2816355 8.2864928	.001785714 .001782531 .001779359 .001776199 .001773050 .001769912 .00176368 .001760563 .001757469
570 571 572 573 574 575 576 577 578 579	324900 326041 327184 328329 329476 330625 331776 332929 324084 335241	185193000 186169411 187149248 188132517 189119224 190109375 191102976 192100033 193100552 194104539	23.8746728 23.8956063 23.9165215 23.9374184 23.9582971 23.9791576 24.000000 24.0208243 24.0416306 24.0624188	8.2913444 8.2961903 8.3010304 8.3058651 8.3106941 8.3155175 8.3203353 8.3251475 8.3299542 8.3347553	.001754886 .001751313 .001748252 .001745201 .001742160 .001739130 .001736111 .001733102 .001730104
580 581 582 583 584 585 586 587 588 588	336400 337561 338724 339889 341056 342225 343396 344569 345744 346921	195112000 196122941 197137368 198155287 199176704 200201625 201230056 202262003 203297472 204336469	24.0831891 24.1039416 24.1246762 24.1453929 24.1660919 24.1867732 24.2074369 24.2280829 24.2487113 24.2693222	8.3395509 8.3443410 8.3491256 8.3539047 8.3586784 8.3634466 8.3682095 8.3729668 8.3777188 8.3824653	.001724138 .001721170 .001718213 .001715266 .001712329 .001709402 .001709402 .001703578 .001700680 .001697793
590 591 592 593 594 595 596 597 598 599	349100 349281 350464 351649 352836 354025 355216 356409 357604 358801	205379000 206425071 207474688 206527857 209584584 210644875 211708736 212776173 213847192 214921799	24.2899156 24.3104916 24.3510501 24.3515913 24.3721152 24.3926218 24.4131112 24.4335834 24.4540385 24.4744765	8.3872065 8.3919423 8.3966729 8.4013981 8.4061180 8.4108326 8.4155419 8.4202460 8.4219448 8.4296383	.001694915 .001692047 .001689189 .001686341 .001683502 .001677852 .001675042 .001672241 .001669449
600 601 602 603 604 605 606 607 608 609	360000 361201 362404 363609 364816 366025 367236 368449 369664 370881	216000000 217081801 218167203 219256227 220348864 221445125 222545016 223648543 224755712 225866529	24.4948974 24.5153013 24.5356888 24.5560583 24.5764115 24.5967478 24.6170673 24.6373700 24.6576560 24.6779254	8.4343267 8.4390098 8.4436877 8.4483605 8.4530281 8.4576906 8.4623479 8.4670601 8.4716471 8.4762892	.001666667 .00166894 .00165130 .001658375 .001655629 .001652893 .001650165 .001647446 .001644737 .001642036
610 611 612 613 614 615 616 617 618 619 620	372100 373321 374544 375769 376996 378225 379456 380689 381924 383161 384400	226981000 228099131 2299220928 230346397 231475544 232608375 233744896 234885113 236029032 237176659 238328000	24. 6981781 24. 7184142 24. 7386338 24. 7588368 24. 7790234 24. 7991935 24. 8193473 24. 8394847 24. 8596058 24. 8797106 24. 8997992	8.4809261 8.4855579 8.4901848 8.4948065 8.4994233 8.5040350 8.5086417 8.5132435 8.5178403 8.524321 8.5224321	.001639344 .001636661 .001633987 .001631321 .001628664 .001626016 .00162746 .001618123 .001615509 .001612903

No.	Squares	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
621 622 623 624 625 626 627 628 629	385641 386884 386129 389376 390625 391876 393129 394384 395641	239483061 240641848 241804867 242970624 244140625 245314376 246491883 247673152 248858189	24.9198716 24.9399278 24.9599679 24.9799920 25.0000000 25.0199920 25.0399681 25.0599282 25.0798724	8.5816009 8.5361780 8.5407501 8.5453173 8.5498797 8.5544372 8.5589899 8.5685377 8.5680807	.001610306 .001607717 .001605136 .001602564 .001600000 .001597444 .001594896 .001592357
630 631 632 633 634 635 636 637 638 639	396900 398161 399424 400689 401956 403225 404496 405769 407044 408321	250047000 251239591 252435668 253636137 254840104 256047875 257259456 258474853 250694072 260917119	25.0998008 25.1197134 25.1396102 25.1594913 25.1793566 25.1992063 25.2190404 25.2388589 25.2586619 25.2784493	8.5726189 8.5771523 8.5816809 8.5862047 8.5907238 8.5952380 8.5997476 8.6042525 8.6087526 8.1132480	.001587302 .001584786 .001582278 .001579779 .001577287 .001574803 .001574803 .001569859 .001567398
640 641 642 643 644 645 646 647 648 649	409600 410881 412164 413449 414736 416025 417316 418609 419904 421201	262144000 263374721 264603288 265847707 26708984 268336125 269586136 270840023 272097792 273359449	25, 2982213 25, 3179778 25, 3377189 25, 3574447 25, 3771551 25, 3968502 25, 4165301 25, 4361947 25, 4558441 25, 4754784	8.6177388 8.6222248 8.6267063 8.6311830 8.6356551 8.6401226 8.6445855 8.6490437 8.6534974 8.6579465	.001562500 .001560062 .001557632 .00155210 .001552795 .001550388 .00154595 .00154595 .001548320
650 651 652 653 654 655 656 657 658 659	422500 423801 425104 426409 427716 429025 430336 431649 432964 434281	274625000 275894451 277167808 278445077 279726264 281011375 282300416 283593393 284890312 286191179	25.4950976 25.5147016 25.5342907 25.5538647 25.5734237 25.5929679 25.6320112 25.6320112 25.6515107 25.6709953	8.6623911 8.6668310 8.6712665 8.6756974 8.6801237 8.6845456 8.6889630 8.6933759 8.6977843 8.7021882	.001538462 .001536098 .001533742 .001531394 .001529052 .001526718 .001524300 .001522070 .00151757
660 661 662 663 664 665 666 667 668 669	435600 436921 438244 439569 440896 442225 443556 444889 446224 447561	287496000 288804781 290117528 291434247 292754944 294079625 295408296 296740963 298077632 299418309	25.6904652 25.7099203 25.7293607 25.7487864 25.7681975 25.7875939 25.8069758 25.8263431 25.8456960 25.8456943	8.705877 8.7109827 8.7159734 8.715756 8.7241414 8.7285187 8.7328918 8.7372604 8.7416246 8.7459846	.001515152 .001512859 .001510574 .001508296 .001508296 .001506024 .001503759 .001501502 .001499250 .001497006 .001494768
670 671 672 673 674 675 676 677 678 679	448900 450241 451584 452929 454276 455625 456976 458329 459684 461041	300763000 302111711 303464448 304821217 306182024 307546875 308915776 310288733 311665752 313046839	25, 8843582 25, 9036677 25, 9229628 25, 9422485 25, 9615100 25, 9807621 26, 000000 26, 0192287 26, 0384331 26, 0576284	8.7503401 8.7546913 8.7590383 8.7633809 8.7677192 8.7720532 8.7763830 8.7807084 8.7850296 8.7893466	.001492537 .001490313 .001485095 .001485384 .001485380 .001481481 .001479290 .001477105 .0014774926 .00147754
680 681 682	462400 463761 465124	314432000 315821241 317214568	26.0768096 26.0959767 26.1151297	8.7936593 8.7979679 8.8022721	.001470588 .001468429 .001466276

CUBE ROOTS, AND RECIPROCALS.

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
683 684 685 686 687 688 689	466489 467856 469225 470596 471969 473344 474721	318611987 320013504 321419125 322828856 324242703 325660672 327082769	26.1342687 26.1533937 26.1725047 26.1916047 26.2106848 26.2297541 26.2488095	8.8065722 8.8108681 8.8151598 8.8194474 8.8237307 8.8280099 8.8322850	.001464129 .001461988 .001459854 .001457726 .001455604 .001453488 .001451379
690 691 692 693 694 695 696 697 698	476100 477481 478864 480249 481636 483025 484416 485809 487204	328509000 329939371 331373888 332812557 334255384 335702375 337153536 338608873 340068392	26.2678511 26.2868789 26.3058929 26.3248932 26.3438797 26.3628527 26.3818119 26.4007576 26.4196896	8.8365559 8.8408227 8.8450854 8.8450854 8.8535985 8.8535985 8.8620952 8.8663375 8.8705757	.001449275 .001447178 .001445087 .001443001 .001440923 .001438849 .001436782 .001434720 .001432665
699 700 701 702 703 704 705 706 707 708	488601 490000 491401 492804 494209 495616 497025 498436 499849 501264	341532099 343000000 344472101 345948408 347428927 348913664 350402625 351895816 353939243 354894912	26.4386081 26.4575131 26.4764046 26.4952826 26.5141472 26.5329983 26.5518361 26.5706605 26.5894716 26.6082694	8.8748099 8.8790400 8.8832661 8.8874882 8.8917063 8.8959204 8.9001304 8.9043366 8.9085387 8.9127369	.001430615 .001428571 .001426534 .001424501 .001422475 .001420455 .001418440 .001416431 .001414427 .001412429
709 710 711 712 713 714 715 716 717 718 719	502681 504100 505521 506944 508369 509796 511225 512656 514089 515524 516961	356400829 357911000 359425431 360944128 362467097 363994344 365525875 367061696 368601813 370146232 371694959	26 6270539 26 6458252 26 6645833 26 6833281 26 7020598 26 7304839 26 7381763 26 7768557 26 7955220 26 8141754	8.9169311 8.9211214 8.9253078 8.9294902 8.9336687 8.9378433 8.9420140 8.9461809 8.9503438 8.9545029 8.9586581	.001410437 .001408451 .001406470 .001404494 .001402525 .001400560 .001396648 .001394700 .001392758 .001390821
720 721 722 723 724 725 726 727 728 729	516961 518400 519841 521284 522729 524176 525625 527076 528529 529984 531441	373248000 374805361 376867048 377933067 379503424 381078125 382657176 384240583 385828352 387420489	26.8328157 26.8328157 26.8700577 26.8886593 26.9072481 26.9258240 26.9443872 26.9629375 26.9814751 27.0000000	8.9628095 8.9669570 8.9711007 8.9752406 8.9793766 8.9835089 8.9876373 8.9917620 8.9958829 9.0000000	.001399821 .001385983 .001385963 .001385042 .001383126 .001379310 .001377410 .001375516 .001373626 .001371742
730 731 732 733 734 735 736 736 737 738 739	532900 534361 535824 537289 538756 540225 541696 543169 544644 546121	389017000 390617891 392223168 3938532837 395446904 397065375 398688256 400315553 401947272 403583419	27.0185122 27.0370117 27.0554985 27.0739727 27.0924344 27.1108834 27.1293199 27.1477439 27.1661554 27.1845544	9.0041134 9.0082229 9.0123288 9.0164309 9.0205293 9.0246239 9.0287149 9.0328021 9.0368857 9.0409655	.001369863 .001367989 .001366120 .001364256 .001362398 .001360544 .001358696 .001356852 .001355014
740 741 742 743 744	547600 549081 550564 552049 553536	405224000 406869021 408518488 410172407 411830784	27, 2029410 27, 2213152 27, 2396769 27, 2580263 27, 2763634	9.0450419 9.0491142 9.0531831 9.0572482 9.0613098	.001351351 .001349528 .001347709 .001345895 .001344086

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
745 746 747 748 749	555025 556516 558009 559504 561001	413493625 • 415160936 416832723 418508992 420189749	27.2946881 27.3130006 27.3313007 27.3495887 27.3678644	9.0653677 9.0694220 9.0734726 9.0775197 9.0815631	.001342282 .001340483 .001338688 .001336898 .001335113
750 751 752 753 754 755 756 757 758 759	562500 564001 565504 567009 568516 570025 571536 573049 574564 576081	421875000 423564751 425259008 426957777 428661064 430368875 432081216 433798093 435519512 437245479	27.3861279 27.4043792 27.4226184 27.4408455 27.4590604 27.4772632 27.5136330 27.5317998 27.5499546	9.0856030 9.0896392 9.0936719 9.0977010 9.1017265 9.1057485 9.1097669 9.1137818 9.1177931 9.1218010	.00133333 .001331558 .001329787 .001328021 .001326260 .001324503 .001322751 .001321004 .001319261 .001317523
760 761 762 763 764 765 766 767 768 769	577600 579121 580644 582169 583696 585225 586756 588289 589824 591361	438976000 440711081 442450728 444194947 445943744 447697125 449455096 451217663 452984832 454756609	27.5680975 27.5862284 27.6043475 27.62:4546 27.6405499 27.6586334 27.6767050 27.6947648 27.7128129 27.7308492	9.1258053 9.1298061 9.1338084 9.1377971 9.1417874 9.1457742 9.1497576 9.1557375 9.1577139 9.1616869	.001315789 .001314060 .001312336 .001310616 .001308901 .001307190 .001303781 .001302083 .001300390
770 771 772 773 774 775 776 777 778 779	592900 594441 595984 597529 599076 600625 602176 603729 605284 606841	456533000 458314011 460090648 461889917 463684824 465484375 467288576 469097433 470910952 472729139	27.7488739 27.7668868 27.7848880 27.8028775 27.8308755 27.8388218 27.8567766 27.8747197 27.8926514 27.9105715	9.1656565 9.1696225 9.1735852 9.1775445 9.1815003 9.1854527 9.1894018 9.1933474 9.1972897 9.2012286	.001298701 .001297017 .001295337 .001293661 .001291990 .001290323 .001288660 .001287001 .001285347 .001283697
780 781 782 783 784 785 786 787 788 789	608400 609961 611524 613089 614656 616225 617796 619369 620944 622521	474552000 476379541 478211768 480048687 481890304 483736625 485587656 487443403 489303872 491169069	27.9284801 27.9463772 27.9642629 27.9821372 28.0000000 28.0178515 28.0356915 28.0535203 28.0713377 28.0891438	9.2051641 9.2090962 9.2130250 9.2169505 9.2206726 9.2247914 9.2287068 9.2326189 9.2365277 9.2404333	.001282051 .001280410 .001278772 .001277139 .001275510 .001273885 .00127265 .001270648 .001269036 .001267427
790 791 792 793 794 795 796 797 798 799	624100 625681 627264 628849 630436 632025 633616 635209 636804 638401	493039000 494913671 490793088 498677257 500566184 502459875 504358336 506261573 508169592 510082399	28.1069386 28.1247222 28.1424946 28.1602557 28.1780056 28.1957444 28.231884 28.2488938 28.2665881	9.2443355 9.2482344 9.2521300 9.2560224 9.2599114 9.2637973 9.2676798 9.2715592 9.2754352 9.2793081	.001265823 .001264223 .001262626 .001261034 .001259446 .001257862 .001256281 .001254705 .001253133 .001251564
800 801 802 803 804 805 806	640000 641601 643204 644809 646416 648025 649636	512000000 512922401 515849608 517781627 519718464 521660125 523606616	28.2842712 28.3019434 28.3196045 28.3372546 28.3548938 28.3725219 28.3901391	9.2831777 9.2870440 9.2909072 9.2947671 9.2986239 9.3024775 9.3063278	.001250000 .001248439 .001246883 .001245330 .001243781 .001242236 .001240695

No.	Squares.	Cubes.	Square Roots,	Cube Roots.	Reciprocals.
807 808 809	651249 652864 654481	525557948 527514112 529475129	28.4077454 28.4253408 28.4429253	9.3101750 9.3140190 9.3178599	.001239157 .001237624 .001236094
810 811 812 813 814 815 816 817 818 819	656100 657721 659344 660969 662596 664225 665856 667489 669124 670761	531441000 533411731 535387328 5373677797 539353144 541343375 543338496 545338513 547343432 549353259	28.4604989 28.4780617 28.4956137 28.5131549 28.5306852 28.5482048 28.5657137 28.5832119 28.6006993 28.6181760	9.3216975 9.3255320 9.3293634 9.3331916 9.3370167 9.3408386 9.3446575 9.3484731 9.3522857 9.3560952	.001234568 .001233046 .001231527 .001230012 .001225501 .001225490 .001225490 .001223490 .001222494
820 821 822 823 824 825 826 827 828 829	672400 674041 675684 677329 678976 680625 682276 683929 685584 687241	551368000 553387661 555412248 557441767 559476224 561515625 563559976 565609283 567763552 569722789	28.6356421 28.6350976 28.6705424 28.6879766 28.7054002 28.7228132 28.7402157 28.7749891 28.7728001	9.3599016 9.3637049 9.3675051 9.3713022 9.375963 9.3758873 9.3826752 9.3864600 9.3902419 9.3940206	.001219512 .001218027 .001216545 .001215067 .001213592 .001212121 .001210654 .001209190 .001207729 .001206273
830 831 832 833 834 835 836 837 838 839	688900 690561 692224 693889 695556 697225 698896 700569 702244 703921	571787000 573856191 575930368 578009537 580093704 582182875 584277056 586376253 588480472 590589719	28,8097206 28,8270706 28,8414102 28,8617394 28,8790582 28,8963666 28,9136646 28,9309523 28,9482297 28,9654967	9.3977964 9.4015691 9.4053387 9.4091054 9.4128690 9.4166297 9.4203873 9.4241420 9.4278936 9.4316423	.001204819 .001203369 .001201923 .001200480 .001199041 .001197605 .001196172 .001194743 .001193317 .001191895
840 841 842 843 844 845 846 847 848 849	705600 707281 708964 710649 712336 714025 715716 717409 719104 720801	592704000 594823321 596947688 599077107 601211584 603351125 605495736 607645423 609800192 611960049	28.9827535 29.0000000 29.0172363 29.0344623 29.0516781 29.0688837 29.0860791 29.1032644 29.1204396 29.1376046	9.4353880 9.4391307 9.4428704 9.4466072 9.4503410 9.4540719 9.4577999 9.4615249 9.4652470 9.4689661	.001190476 .001189061 .001187648 .001186240 .001184834 .001183432 .001182033 .001180638 .001177856
850 851 852 853 854 855 856 857 858 859	722500 724201 725904 727609 729316 731025 732736 734449 736164 737881	614125000 616295051 618470208 620650477 622835864 625026375 627222016 629422793 631628712 633839779	29.1547595 29.1719043 29.1890390 29.2061637 29.2232784 29.2403830 29.2574777 29.2745623 29.2916370 29.3087018	9.4726824 9.4763957 9.4801061 9.4838136 9.4875182 9.4912200 9.4949188 9.4986147 9.5023078 9.5059980	.001176471 .001175088 .001173709 .001172333 .001170960 .001169591 .001168224 .001166861 .001164144
860 861 862 863 864 865 866 867 868	789600 741321 743044 744769 746496 748225 749956 751689 758424	636056000 638277381 640503928 642735647 6449723464 647214625 649461896 651714363 653972032	29.3257566 29.3428015 29.3598365 29.3768616 29.3938769 29.4108823 29.4278779 29.4448637 29.4618397	9,5096854 9,5133699 9,5170515 9,5207303 9,5244063 9,5280794 9,5317497 9,5354172 9,5390818	.001162791 .001161440 .001160093 .001158749 .001157407 .001156069 .001154734 .001153403 .001153074

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
869	755161	656234909	29.4788059	9.5427437	.001150748
			29.4957624	9.5464027	.001149425
870	756900 758641	658503000 660776311	29.5127091	9.5500589	.001148106
871 872	760384	663054848	29.5296461	9.5537123	.001146789
873	762129	665338617	29.5465734	9.5573630	.001145475
874	763876	667627624	29.5634910	9.5610108	.001144165
875	765625	669921875	29.5803989	9.5646559	.001142857
876	767376	672221376	29.5972972	9.5682982	.001141553
877	769129	674526133	29.6141858	9.5719377	.001140251
878	770884	676836152	29.6310648	9.5755745	.001138952
879	772641	679151439	29.6479342	9.5792085	.001137656
880	774400	681472000	29.6647939	9.5828397	.001136364
881	776161	683797841	29.6816442	9.5864682	.001135074
882	777924	686128968	29.6984848	9.5900939	.001133787
883	779689	688465387	29.7153159	9.5937169	.001132503
884	781456	690807104	29.7321375	9.5973373	.001131222
885	783225	693154125	29.7489496 29.7657521	9.6009548 9.6045696	.001129944
886	784996	695506456 697864103	29.7657521	9.6081817	.001127396
887 888	786769 788544	700227072	29.7993289	9.6117911	.001126126
889	790321	702595369	29.8161030	9.6153977	.001124859
			29.8328678	9.6190017	.001123596
890	792100	704969000	29.8496231	9.6190017	.001123390
891 892	793881 795664	707347971 709732288	29.8663690	9.6262016	.001121076
893	797449	712121957	29.8831056	9.6297975	.001119821
894	799236	714516984	29.8998328	9.6333907	.001118568
895	801025	716917375	29.9165506	9.6369812	.001117318
896	802816	719323136	29.9332591	9.6405690	.001116071
897	804609	721734273	29.9499583	9.6441542	.001114827
898	806404	724150792	29.9666481	9.6477367	.001113586
899	808201	726572699	29.9833287	9.6513166	.001112347
900	810000	729000000	30.0000000	9.6548938	.001111111
901	811801	731432701	30.0166620	9.6584684	.001109878
902	813604	733870808	30.0333148	9.6620403	.001108647
903	815409	736314327	30.0499584 30.0665928	9.6656096	.001107420
904 905	817216 819025	738763264 741217625	30.0832179	9.6691762 9.6727403	.001104972
906	820836	743677416	30.0998339	9.6763017	.001103753
907	822649	746142643	30.1164407	9.6798604	.001102536
908	824464	748613312	30.1330383	9.6834166	.001101322
909	826281	751089429	30.1496269	9.6869701	.001100110
910	828100	753571000	30.1662063	9.6905211	.001098901
911	829921	756058031	30.1827765	9.6940694	.001097695
912	831744	758550528	30.1993377	9.6976151	.001096491
913	833569	761048497	30.2158899	9.7011583	,001095290
914	835396	763551944	30.2324329	9.7046989	.001094092
915	837225	766060875	30.2489669	9.7082369	.001092896
916	839056	768575296	30.2654919 30.2820079	9.7117723 9.7153051	.001091703
917 918	840889 842724	771095213 773620632	30.2985148	9.7188354	.001089325
918	844561	776151559	30.3150128	9.7223631	.001088139
			30.3315018	9.7258883	.001086957
920 921	846400 848241	778688000 781229961	30.3313018	9.7294109	.001085576
921	850084	783777448	30.3644529	9.7329309	.001084599
923	851929	786330467	30.3809151	9.7364484	.001083423
924	853776	788889024	30.3973683	9.7399634	.001082251
925	855625	791453125	30.4138127	9.7434758	.001081081
926	857476	794022776	30.4302481	9.7469857	.001079914
927	859329	796597983	30.4466747	9.7504930	.001078749
928	861184	799178752 801765089	30.4630924 30.4795013	9.7539979 9.7575002	.001077586
929	863041	801765089 804357000	30.4795013	9.7610002	.001075269
930	864900	004667000	1 00.4959014	9.7010001	.001010600

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
931 932 933 934 935 936 937 938 \$39	866761 868624 870489 872356 874225 876096 877969 879844 881721	806954491 809557568 812166237 814780364 817400375 820025856 822656953 825293672 827986019	30.5122926 30.5286750 30.5450487 30.5614136 30.5777697 30.5941171 30.6104557 30.6267857 30.6431069	9.7644974 9.7679922 9.7714845 9.7749743 9.7784616 9.7819466 9.7854288 9.7889087 9.7923861	.001074114 .001072961 .001071811 .001070664 .001069519 .001068376 .001067236 .001064963
940 941 942 943 944 945 946 947 948 949	883600 885481 887364 889249 891136 893025 894916 896809 898704 900601	830584000 833237621 835896888 838561807 841232384 843908625 846590536 849278123 851971393 854670349	30.6594194 30.6757233 30.6920185 30.7083051 50.7083051 50.7345830 30.7408523 30.7571130 30.7733651 30.7896086 30.8058436	9.7958611 9.7993336 9.8028036 9.8062711 9.8097362 9.8131989 9.8166591 9.820169 9.8235723 9.823723	.001063830 .001062699 .001061571 .001060445 .001059322 .001058201 .001057082 .001055966 .001054852 .001053741
950 951 952 953 954 955 956 957 958 959	902500 904401 906304 908209 910116 912025 913936 915849 917764 919681	857375000 860085351 862801408 865523177 868250664 870983875 873722816 876467493 879217912 881974079	30,8220700 30,8382879 30,8544972 30,876981 30,8868904 30,9030743 30,9192497 30,9354166 30,93547551 30,9677251	9.8304757 9.8339238 9.8373695 9.8408127 9.8442536 9.8476920 9.8511280 9.8545617 9.8579929 9.8614218	.001052632 .001051525 .001050420 .001049318 .001048218 .001047120 .001046025 .001044932 .001043841 .001042753
960 961 962 963 964 965 966 967 968 969	921600 923521 925444 927369 929296 931225 933156 935089 937024 938961	884736000 887503681 890277128 893056347 895841344 898632125 901428696 904231063 907039232 909853209	30.9838668 31.0000000 31.0161248 31.0322413 31.0483494 31.0805405 31.0966236 31.1126984 31.1287648	9.8648483 9.8682724 9.87716941 9.8751135 9.8765305 9.8819451 9.8853574 9.8857673 9.8921749 9.8955801	.001041667 .001040583 .001039501 .001038422 .001037344 .001036269 .001035197 .001084126 .001033058 .001031992
970 971 972 973 974 975 976 977 978 979	940900 942841 944784 946729 948676 950625 952576 954529 956484 958441	912673000 915498611 918830048 921167317 924010424 926859375 929714176 932574833 935441352 938313739	31.1448230 31.1608729 31.1769145 31.1929479 31.2089731 31.2249900 31.2409987 31.2569992 31.2729915 31.2889757	9.8989830 9.9023825 9.9057817 9.9091776 9.9125712 9.9159624 9.9193513 9.9227379 9.9261222 9.9295042	.001030928 .001029866 .00102807 .00102807 .001026694 .001026694 .001023541 .001023541 .001023495 .001021450
980 981 982 983 984 985 986 987 988 989	960400 962361 964324 966289 966286 970225 972196 974169 976144 978121	941192000 944076141 946966168 949862087 952763904 955671625 95855256 961504803 964430272 967361669	31.3049517 31.3209195 31.3368792 31.3528308 31.3687743 31.4006369 31.4165561 31.4324673 31.4483704	9.9328839 9.9362613 9.9396363 9.9430092 9.9463797 9.9457118 9.9564775 9.9598889 9.9631981	.001020408 .001019368 .001018330 .001017294 .001016260 .001015228 .001014199 .001013171 .001012146 .001011122
990 991 992	980100 982081 984064	970299000 973242271 976191488	31.4642654 31.4801525 31.4960315	9.9665549 9.9699095 9.9732619	.001010101 .001009082 .001008065

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
000	000040	070110657	31.5119025	9.9766120	.001007049
993	986049	979146657	31.5277655	9.9799599	.001007049
994	988036	982107784 985074875	31,5436206	9.9833055	.001005035
995	990025	988047936	31.5594677	9.9866488	.001003023
996	992016 994009	991026973	31.5753068	9.9899900	.001003009
997	996004	994011992	31,5911380	9,9933289	.001003003
998	998001	997002999	31.6069613	9,9966656	.001002004
999		1000000000	31.6227766	10.0000000	.001000000
1000	1000000				
1001	1002001	1003003001	31.6385840	10.0033322	.0009990010
1002	1004004	1006012008	31.6543836	10.0066622	.0009980040
1003	1006009	1009027027	31.6701752	10.0099899	.0009970090
1004	1008016	1012.48064	31.6859590	10.0133155	.0009960159
1005	1010025	1015075125	31.7017349	10.0166389	.0009950249
1006	1012036	1018108216	31.7175030	10.0199601	.0009940358
1007	1014049	1021147343	31.7332633	10.0232791	.0009930487
1008	1016064	1024192512	31.7490157	10.0265958	.0009920635
1009	1018081	1027243729	31.7647603	10.0299104	.0009910803
1010	1020100	1030301000	31.7804972	10.0332228	,0009900990
1011	1022121	1033364331	31.7962262	10.0365330	.0009891197
1012	1024144	1036433728	31.8119474	10.0398410	.0009881423
1013	1026169	1039509197	31.8276609	10.0431469	.0009871668
1014	1028196	1042590744	31.8433666	10.0464506	.0009861933
1015	1030225	1045678375	31.8590646	10.0497521	.0009852217
1016	1032256	1048772096	31.8747549	10.0530514	.0009842520
1017	1034289	1051871913	31.8904374	10.0563485	.0009832842
1018	1036324	1054977832	31.9061123 .	10.0596435	.0009823183
1019	1038361	1058089859	31.9217794	10.0629364	.0009813543
1020	1040400	1061208000	31.9374388	10.0662271	.0009803922
1021	1042441	1064332261	31,9530906	10.0695156	.0009794319
1022	1044484	1067462648	31.9687347	10.0728020	.0009784736
1023	1046529	1070599167	31.9843712	10.0760863	.0009775171
1024	1048576	1073741824	32.0000000	10.0793684	.0009765625
1025	1050625	1076890625	32.0156212	10.0826484	.0009756098
1026	1052676	1080045576	32.0312348	10.0859262	.0009746589
1027	1054729	1083206683	32.0468407	10.0892019	.0009737098
1028	1056784	1086373952	32.0624391	10.0924755	.0009727626
1029	1058841	1089547389	32.0780298	10.0957469	.0009718173
1030	1060900	1092727000	32.0936131	10.0990163	.0009708738
1031	1062961	1095912791	32.1091887	10.1022835	.0009699321
1032	1065024	1099104768	32.1247568	10.1055487	.0009689922
1033	1067089	1102302937	32.1403173	10.1088117	.0009680542
1034	1069156	1105507304	32.1558704	10.1120726	.0009671180
1035	1071225	1108717875	32.1714159	10.1153314	.0009661836
1036	1073296	1111934656	32.1869539	10.1185882	.0009652510
1037	1075369	1115157653	32.2024844	10.1218428	.0009643202
1038	1077444	1118386872	32.2180074	10.1250953	.0009633911
1039	1079521	1121622319	32.2335229	10.1283457	.0009624639
1040	1081600	1124864000	32.2490310	10.1315941	
1041	1083681	1128111921	32.2645316	10.1348403	.0009606148
1042	1085764	1131366088	32.2800248	10.1380845	.0009596929
1043	1087849	1134626507	32.2955105	10.1413266	.0009587738
1044	1089936	1137893184	32.3109888	10.1445667	.0009578544
1045	1092025	1141166125	32.3264598	10.1478047	.0009569378
1046	1094116	1144145336	32.3419233	10.1510406	.0009500229
1047	1096209	1147730823	32.3573794 32.3728281	10.1542744 10.1575062	.0009531098
1048	1098304	1151022592	32.3882695	10.1607359	.0009532888
1049 1050	1100401 1102500	1154320649 1157625000	32.4037035	10.1639636	.0009523810
1	1		1	1	
1051	1104601	1160935651	32.4191301	10.1671893	.0009514748
1052	1106704	1164252608	32.4345495	10.1704129	.0009496676
1053	1108809	1167575877	32.4499615	10.1736344 10.1768539	.0009496676
1054	1110916	1170905464	32.4653662	10.1100359	1 .0009-01000

No.	100 L. 00	0.]				_No. 109 L. 0 4					
N.	0	1	2	8	4	5	6	7	8	9	Diff.
100	000000 4321 8600	0434 4751 9026	0868 5181 9451	1301 5609 9876	1734 6038	2166 6466	2598 6894	3029 7321	3461 7748	3891 8174	432 438
3 4	012837 7033	3259 7451	3680 7868	4100 8284	0300 4521 8700	0724 4940 9116	1147 5360 9532	1570 5779 9947	1993 6197	2415 6616	424 420
5 6 7	021189 5306 9384	1603 5715 9789	2016 6125	2428 6533	2841 6942	3252 7350	3664 7757	4075 8164	0361 4486 8571	0775 4896 8978	418 418 408
8 9	033424 7426	3826 7825	0195 4227 8223	0600 4628 8620	1004 5029 9017	1408 5430 9414	1812 5830 9811	2216 6230	2619 6629	3021 7028	404 400
	04		}					0207	0602	0998	39

Diff.	1	2	3	4	5	6	7	8	9
434 433 432 431 430	43.4 43.3 43.2 43.1 43.0	86.8 86.6 86.4 86.2 86.0	130.2 129.9 129.6 129.3 129.0	173.6 173.2 172.8 172.4 172.0	217.0 216.5 216.0 215.5 215.0	260.4 259.8 259.2 258.6 258.0	303.8 303.1 302.4 301.7 301.0	347.2 346.4 345.6 344.8 344.0	390.6 389.7 388.8 387.9 387.0
429 428 427 426 425	42.9 42.8 42.7 42.6 42.5	85.8 85.6 85.4 85.2 85.0	128.7 128.4 128.1 127.8 127.5	171.6 171.2 170.8 170.4 170.0	214.5 214.0 213.5 213.0 212.5	257.4 256.8 256.2 255.6 255.0	300.3 299.6 298.9 298.2 297.5	343.2 342.4 341.6 340.8 340.0	386.1 385.2 384.3 383.4 382.5
424 423 422 421 420 419 418 417 416	42.4 42.3 42.2 42.1 42.0 41.9 41.8 41.7	84.8 84.6 84.4 84.2 84.0 83.8 83.6 83.4 83.2	127.2 126.9 126.6 126.3 126.0 125.7 125.4 125.1 124.8	169.6 169.2 168.8 168.4 168.0 167.6 167.2 166.8	212.0 211.5 211.0 210.5 210.0 209.5 209.0 208.5 208.0	254.4 253.8 253.2 252.6 252.0 251.4 250.8 250.2 249.6	296.8 296.1 295.4 294.7 294.0 293.3 292.6 291.9	339.2 338.4 337.6 336.8 336.0 335.2 334.4 333.6 332.8	381.6 380.7 379.8 378.9 378.0 377.1 376.2 375.3 374.4
415 414 413 412 411 410 409 408 407 406 405	41.5 41.4 41.3 41.2 41.1 41.0 40.9 40.8 40.7 40.6 40.5	83.0 82.8 82.6 82.4 82.2 82.0 81.8 81.6 81.4 81.2 81.0	124.5 124.2 123.9 123.6 123.3 123.0 122.7 122.4 122.1 121.8 121.5	166.0 165.6 165.2 164.8 164.4 163.6 163.2 162.8 162.4	207.5 207.0 206.5 206.0 205.5 205.0 204.5 204.0 203.5 203.0 202.5	249.0 248.4 247.8 247.2 246.6 246.0 245.4 244.8 244.8 243.6 243.0	290.5 289.8 289.1 288.4 287.7 287.0 286.3 285.6 284.9 284.2 283.5	332.0 331.2 330.4 329.6 328.8 328.0 327.2 326.4 325.6 324.8 324.0	373.5 372.6 371.7 370.8 369.9 369.0 368.1 367.2 366.3 365.4 364.5
404 403 402 401 400 399 398 397 396 395	40.4 40.3 40.2 40.1 40.0 39.9 39.8 39.7 39.6 39.5	80.8 80.6 80.4 80.2 80.0 79.8 79.6 79.4 79.2 79.0	121.2 120.9 120.6 120.3 120.0 119.7 119.4 119.1 118.8 118.5	161.6 161.2 160.8 160.4 160.0 159.6 159.2 158.8 158.4 158.0	202.0 201.5 201.0 200.5 200.0 199.5 199.0 198.5 198.0 197.5	242.4 241.8 241.2 240.0 239.4 238.8 238.2 237.6 237.0	282.8 282.1 281.4 280.7 280.0 279.3 278.6 277.9 277.2 276.5	323.2 322.4 321.6 320.8 320.0 319.2 318.4 317.6 316.8 316.0	363.6 362.7 361.8 360.9 360.0 359.1 358.2 357.3 356.4 355.5

N.	0	1	2	3	4	5	6	7	8	9	Diff
	U	•		o o	7		U				ыш
10	041393	1787	2182	2576	2969	3362	3755	4148	4540	4932	39
1	5323	5714	6105	6495	6885	7275	7664	8053	8112	8830	39
2	9218	9606	9993	0000	0800	1150		1001		0001	000
3	053078	3463	3846	0380 4230	0766 4613	1153 4996	1538 5378	1924 5760	2309 6142	2694 6524	38 38
4	6905	7286	7666	8046	8426	8805	9185	9563	9942	0024	90
		_	_							0320	37
5	060698	1075	1452	1829	2206	2582	2958	3333	3709	4083	37
6	4458 8186	4832 8557	5206 8928	5580 9298	5953 9668	6326	6699	7071	7443	7815	37
1	0100	0001	0920	9296	9000	0038	0407	0776	1145	1514	37
8	071882	2250	2617	2985	3352	3718	4085	4451	4816	5182	36
9	5547	5912	6276	6640	7004	7368	7731	8094	8457	8819	36

Diff.	1	2	3	4	5	6	7	8	9	
395 394 393 392 391 390 389 388 387 386 385	39.5 39.4 39.3 39.2 39.1 39.0 38.9 38.8 38.7 38.6 38.5	79.0 78.8 78.6 78.4 78.2 78.0 77.8 77.6 77.4 77.2 77.0	118.5 118.2 117.9 117.6 117.3 117.0 116.7 116.4 116.1 115.8 115.5	158.0 157.6 157.2 156.8 156.4 156.0 155.6 155.2 154.8 154.4 154.0	197.5 197.0 196.5 196.0 195.5 195.0 194.5 194.0 193.5 193.0 192.5	237.0 236.4 235.8 235.2 234.6 234.0 233.4 232.8 231.6 231.0	276.5 275.8 275.1 274.4 273.7 273.0 272.3 271.6 270.9 270.2 269.5	316.0 315.2 314.4 313.6 312.8 312.0 311.2 310.4 309.6 308.8 308.0	355.5 354.6 353.7 352.8 351.9 351.0 350.1 349.2 348.3 347.4 346.5	
384	38.4	76.8	115.2	153.6	192.0	230.4	268.8	307.2	345.6	
383	38.3	76.6	114.9	153.2	191.5	229.8	268.1	306.4	344.7	
382	38.2	76.4	114.6	152.8	191.0	229.2	267.4	305.6	343.8	
381	38.1	76.2	114.3	152.4	190.5	228.6	266.7	304.8	342.9	
380	38.0	76.0	114.0	152.0	190.0	228.0	266.0	304.0	342.0	
379	37.9	75.8	113.7	151.6	189.5	227.4	265.3	303.2	341.1	
378	37.8	75.6	113.4	151.2	189.0	226.8	264.6	302.4	340.2	
377	37.7	75.4	113.1	150.8	188.5	226.2	263.9	301.6	339.3	
376	37.6	75.2	112.8	150.4	188.0	225.6	263.2	300.8	338.4	
375	37.5	75.0	112.5	150.0	187.5	225.0	262.5	300.0	337.5	
374	37.4	74.8	112.2	149.6	187.0	224.4	261.8	299.2	336.6	
373	37.3	74.6	111.9	149.2	186.5	223.8	261.1	298.4	335.7	
372	37.2	74.4	111.6	148.8	186.0	223.2	260.4	297.6	334.8	
371	37.1	74.2	111.3	148.4	185.5	222.6	259.7	296.8	333.9	
370	37.0	74.0	111.0	148.0	185.0	222.0	259.0	296.0	333.0	
369	36.9	73.8	110.7	147.6	184.5	221.4	258.3	295.2	332.1	
368	36.8	73.6	110.4	147.2	184.0	220.8	257.6	294.4	331.2	
367	36.7	73.4	110.1	146.8	183.5	220.2	256.9	293.6	330.3	
366	36.6	73.2	109.8	146.4	183.0	219.6	256.2	292.8	329.4	
565	36.5	73.0	109.5	146.0	182.5	219.0	255.7	292.0	328.5	
364	36.4	72.8	109.2	145.6	182.0	218.4	254.8	291.2	327.6	
363	36.3	72.6	108.9	145.2	181.5	217.8	254.1	290.4	326.7	
362	36.2	72.4	108.6	144.8	181.0	217.2	253.4	289.6	325.8	
361	36.1	72.2	108.3	144.4	180.5	216.6	252.7	288.8	324.9	
360	36.0	72.0	108.0	144.0	180.0	216.0	252.0	288.0	324.0	
359	35.9	71.8	107.7	143.6	179.5	215.4	251.3	287.2	323.1	
358	35.8	71.6	107.4	143.2	179.0	214.8	250.6	286.4	322.2	
357	35.7	71.4	107.1	142.8	178.5	214.2	249.9	285.6	321.3	
356	35.6	71.2	106.8	142.4	178.0	213.6	249.2	284.8	320.4	

LOCADITUMS OF NUMBERS

		TABL	EIX	.—L	OGA1	RI	THMS	SOF	7	UM	BE	RS.		
No.	120 L. 0	79.]										[No	. 134	L. 130.
N.	0	1	2	3	4		5	6		7	8	3	9	Diff.
120	079181	9543	9904	-										
1	082785	3144	3503	0266 3861	4219		0987 4576	1347 4934	i	707 291	206 564	i	2426 6004	360
2 3	6360	6716	7071	7426	7781		8136	8490		845	919		9552	355
4	093422	0258 3772	$0611 \\ 4122$	0963 4471	1315 4820		1667 5169	2018 5518	5	370 866	272 621	5	$3071 \\ 6562$	352 349
5	6910	7257	7604	7951	8298	-1	8644	8990		335	968	_	0026	346
6 7 8	100371 3804 7210	0715 4146 7549	1059 4487 7888	1403 4828 8227	1747 5169 8565		2091 5510 8903	2434 5851 9241	6	777 191 579	311 653 991	1	3462 6871	343 341
9	110590	0926	1963	1599	1934		2270	2605		940	327	_	0253 3609	338 335
130 1	3943 7271	4277 7603	$\frac{4611}{7934}$	4944 8265	5278 8595		5611 8926	5943 9256		276 586	660 991		6940	333
2	120574	0903	1231	1560 4830	1888		2216	2544	2	871	319	8	0245 3525	330 328
3 4	3852 7105 1 3	4178 7429	4504 7753	8076	5156 8399		5481 8722	5806 9045	9:	131 368	645 969	0 -	6781 0012	325 323
		<u>'</u>			_								0012	020
				Pro	PORTI	ON	AL PA	RTS.						
Diff.	1	2	3		4		5	6		,	7		8	9
355 354 353 352 351 350 349 348 347 346	35.5 35.4 35.3 35.2 35.1 35.0 34.9 34.8 34.7 34.6	71.0 70.8 70.6 70.4 70.2 70.0 69.8 69.6 69.4 69.2	106 106 105 105 105 105 104 104 104 104	5.2 5.9 5.6 5.3 5.0 1.7 1.4	142.0 141.6 141.2 140.8 140.4 140.0 139.6 139.2 138.8 138.4		177.5 177.0 176.5 176.0 175.5 175.0 174.5 174.0 173.5 173.0	213. 212. 211. 211. 210. 210. 209. 208. 208. 207.	4 8 2 6 0 4 8 2	24 24 24 24 24 24 24 24	8.5 7.8 7.1 6.4 5.7 5.0 4.3 3.6 2.9 2.2	25 25 25 25 27 27 27 27 27	\$4.0 \$3.2 \$2.4 \$1.6 \$0.8 \$0.0 79.2 78.4 77.6 76.8	319.5 318.6 317.7 316.8 315.9 315.0 314.1 313.2 312.3 311.4
345 344 343 342 341 340 339 338 337 336	34.5 34.4 34.3 34.2 34.1 34.0 33.9 33.8 33.7	69.0 68.8 68.6 68.4 68.2 68.0 67.8 67.6 67.4 67.2	103 103 103 103 103 103 101 101 101	3.5 3.2 2.9 2.6 2.3 2.0 1.7	138.0 137.6 137.2 136.8 136.4 136.0 135.6 135.2 134.8 134.4		172.5 172.0 171.5 171.0 170.5 170.0 169.5 169.0 168.5 168.0	207. 206. 205. 205. 204. 204. 203. 202. 202.	0 4 8 2 6 0 4 8 2	24 24 24 23 23 23 23 23 23 23 23	1.5 0.8 0.1 9.4 8.7 8.0 7.3 6.6 5.9	21 21 21 21 21 21 21 21	76.0 75.2 74.4 73.6 72.8 72.0 71.2 70.4 39.6 38.8	310.5 309.6 308.7 307.8 306.9 306.0 305.1 304.2 303.3 302.4
335 334 333 332 331 330 329 328 327 326	23.5 33.4 33.3 33.2 33.1 33.0 32.9 32.8 32.7 32.6	67.0 66.8 66.6 66.4 66.2 66.0 65.8 65.6 65.4	100 100 99 99 99 98 98 98	0.5 0.2 0.9 0.6 0.3 0.0 3.7 3.4 3.1	134.0 133.6 133.2 132.8 132.4 132.0 131.6 131.2 130.8 130.4		167.5 167.0 166.5 166.0 165.5 165.0 164.5 164.0 163.5 163.0	201. 200. 199. 199. 198. 198. 197. 196. 196.	0 4 8 2 6 0 4 8 2	23 23 23 23 23 23 23 23 23 22 22 22	4.5 3.8 3.1 2.4 1.7 1.0 0.3 9.6 8.9 8.2	26 26 26 26 26 26 26 26	38.0 37.2 36.4 35.6 34.8 34.0 33.2 32.4 31.6 30.8	301.5 300.6 299.7 298.8 297.9 297.0 296.1 295.2 294.3 293.4

162.5

162.0

161.5 161.0

195.0

194.4

193.8

193.2

 $\frac{227.5}{226.8}$

226.1

225.4

260.0

259.2 258.4 257.6

292.5

 $\frac{291.6}{290.7}$

289.8

130.0

129.6

129.2

128.8

97.5 97.2 96.9 96.6

65.0

64.8

64.6 64.4

325 324 323

322

32.5 32.4 32.3 32.2

No. 1	35 L. 13	60.]							[1	No. 149	L. 175.
N.	0	1	2	3	4	5	6	7	8	9	Diff.
135 6 7 8	130334 3539 6721	0655 3858 7037	0977 4177 7354	1298 4496 7671	1619 4814 7987	1939 5133 8303	2260 5451 8618	2580 5769 8934	2900 6086 9249	6403	321 318 316
9 140	9879 143015 6128	0194 3327 6438	0508 3639 6748	0822 3951 7058	4263	1450 4574 7676	1763 4885 7985	2076 5196 8294		5818	314 311 309
2 3 4	9219 152288 5336 8362	9527 2594 5640 8664	9835 2900 5943 8965	0142 3205 6246 9266	3510 6549	0756 3815 6852 9868	1063 4120 7154	1370 4424 7457	4728	5032	307 305 303
5 6 7	161368 4353 7317	1667 4650 7613	1967 4947 7908	2266 5244 8203	2564 5541	2863 5838 8792	0168 3161 6134 9086	0469 3460 6430 9380	3758 6726	3 4055 7022	301 299 297 295
8 9	170262 3186	0555 3478	0848 3769	1141 4060	1434 4351	1726 4641	2019 4932	2311 5222		2895	293 291
				PR.	PORTIC	ONAL PA	RTS.				
Diff	. 1	2	1	3	4	5	6		7	8	9
321 320 319 318 317 316 315 314 313 312	32.1 32.0 31.9 31.8 31.7 31.6 31.5 31.4 31.3 31.2	64.2 64.0 63.8 63.6 63.4 63.2 63.0 62.8 62.6 62.4	96 96 95 95 95 94 94 94 93	.0 .7 .4 .1 .8 .5 .2	128.4 128.0 127.6 127.2 126.8 126.4 126.0 125.6 125.2 124.8	160.5 160.0 159.5 159.0 158.5 158.0 157.5 157.0 156.5 156.0	192 192 191 190 190 189 188 187 187	.0 .4 .8 .2 .6 .0 .4 .8	224.7 224.0 223.3 222.6 221.9 221.2 220.5 219.8 219.1 218.4	256.8 256.0 255.2 254.4 253.6 252.8 252.0 251.2 250.4 249.6	288.9 288.0 287.1 286.2 285.3 284.4 283.5 282.6 281.7 280.8
311 310 309 308 307 306 305 304 303 302	31.1 31.0 30.9 30.8 30.7 30.6 30.5 30.4 30.3 30.2	62.2 62.0 61.8 61.6 61.4 61.2 61.0 60.8 60.6 60.4	93 93 92 92 92 91 91 91 90	.0 .7 .4 .1 .8 .5 .2	124.4 124.0 123.6 123.2 122.8 122.4 122.0 121.6 121.2 120.8	155.5 155.0 154.5 154.0 153.5 153.0 152.5 152.0 151.5	186 186 185 184 184 183 183 183 182 181	.0 .4 .8 .2 .6 .0 .4	217.7 217.0 216.3 215.6 214.9 214.2 213.5 212.8 212.1 211.4	248.8 248.0 247.2 246.4 245.6 244.8 244.0 243.2 242.4 241.6	279.9 279.0 278.1 277.2 276.3 275.4 274.5 273.6 272.7 271.8
301 300 299 298 297 296 295 294 293 292	30.1 30.0 29.9 29.8 29.7 29.6 29.5 29.4 29.3 29.2	60.2 60.0 59.8 59.6 59.4 59.2 59.0 58.8 58.6	90 90 89 89 89 88 88 88	.3 .0 .7 .4	120.4 120.0 119.6 119.2 118.8 118.4 118.0 117.6 117.2 116.8	150.5 150.0 149.5 149.0 148.0 147.5 147.0 146.5	180 180 179 178 178 177 177 176 175 175	.6 .0 .4 .8 .2 .6 .0 .4 .8	210.7 210.0 209.3 208.6 207.9 207.2 206.5 205.8 205.1 204.4	240.8 240.0 239.2 238.4 237.6 236.8 236.0 235.2 234.4 233.6	270.9 270.0 269.1 268.2 267.3 266.4 265.5 264.6 263.7 262.8
291 290 289 288 287 286	29.1 29.0 28.9 28.8 28.7 28.6	58.2 58.0 57.8 57.6 57.4 57.2	87 87 86 86	.3 .0 .7 .4	116.4 116.0 115.6 115.2 114.8 114.4	145.5 145.0 144.5 144.0 143.5 143.0	174 174 173 172 172	.6 .0 .4 .8	203.7 203.0 202.3 201.6 200.9 200.2	232.8 232.0 231.2 230.4 229.6 228.8	261.9 261.0 260.1 259.2 258.3 257.4

NO. 1	150 L. 17	0.]	1		1 1	1 1			I I	Vo. 169 J	Li, 230,
N.	0	1	2	3	4	5	6	7	8	9	Diff.
50	176091 8977	6381 9264	6670 9552	6959 9839	7248	7536	7825	8113	8401	8689	289
2	181844	2129	2415	2700	0126 2985	0413 3270	0699 3555	0986 3839	1272 4123	1558 4407	287 285
3	4691 7521	4975 7803	5259 8084	5542 8366	5825 8647	6108 8928	6391 9209	6674 9490	6956 9771	7239	283
5	190332	0612	0892	1171	1451	1730	2010	2289	2567	- 0051 2846	281 279
6 7	3125 5900	3403 6176	3681 6453	3959 6729	4237 7005	4514 7281	4792 7556	5069 7832	5346 8107	5623 8382	278 276
8 9	8657 201397	8932	9206	9481	9755 2488	0029 2761	0303 3033	0577 3305	0850 3577	1124 3848	274 272
.60	4120	4391	4663	4934	5204	5475	5746	6016	6286	6556	271
1 2	6826 9515	7096 9783	7365	7634	7904	8173	8441	8710	8979	9247	269
3	212188	2454	0051 2720	0319 2986	0586 3252	0853 3518	1121 3783	1388 4049	1654 4314	4579	267 266
5	4844 7484	5109 7747	5373 8010	5638 8273	5902 8536	6166 8798	6430 9060	6694 9323	6957 9585	7221 9846	264 262
6 7	220108	0370	0631	0892	1153	1414	1675	1936 4533	2196 4792	2456 5051	261 259
8 9	2716 5309 7887	2976 5568 8144	3236 5826 8400	3496 6084 8657	3755 6342 8913	4015 6600 9170	4274 6858 9426	7115 9682	7372 9938	7630	258
١	23	0111	0100				<u> </u>	0000	1000	0193	256
	T			Pro	PORTIC	NAL PA	ARTS.				1
Diff	. 1	2	;	3	4	5	6		7	8	9
285	28.5	57.0	85	.5	114.0	142.5	171		99.5	228.0	256.
284 283	28.4 28.3	56.8 56.6	84	.9	113.6 113.2	142.0 141.5	170 169	.8 1	98.8 98.1	227.2 226.4	255 254
$\frac{282}{281}$	28.2 28.1	56.4	84	.6	112.8 112 4	141.0 140.5	169 168	.6 1	97.4 96.7	225.6 224.8	253. 252.
$\frac{280}{279}$	28.0 27.9	56.0 55.8	84	.0	112.0 111.6	140.0 139.5	168 167	.0 1	96.0 95.3	224.0 223.2	252 . 251 .
278	27.8	55.€	83	.4	111.2	139.0	166	.8 1	94.6	222.4	250.
$\begin{array}{c} 277 \\ 276 \end{array}$	27.8 27.7 27.6	55.4 55.2	83	.8	110.8 110.4	138.5 138.0	· 166	$.2 \mid 1$	93.9 93.2	$\frac{221.6}{220.8}$	249 248
275 274	27.5 27.4	55.0 54.8	82	2.5	110.0 109.6	137.5 137.0	165 164		92.5 91.8	$220.0 \\ 219.2$	247 246
273	27.3	54.6	81	.9	109.2	136.5	163	.8 1	91.1	218.4	245
272 271	27.2 27.1	54.4 54.2		.6	108.8 108.4	136.0 135.5	163 162	$\begin{array}{c c} .2 & 1 \\ 6 & 1 \end{array}$	90.4	217.6 216.8	244 243
270	27.0	54.0	81	.0	108.0	135.0	162	.0 1	89.0	216.0	243.
269 268	26.9 26.8	53.8 53.6		0.7	107.6 107.2	134.5 134.0	161 160		88.3 87.6	215.2 214.4	242 241
267	26.7	53.4	1 80	0.1	106.8	133.5	160	.2 1	86.9	213.6	240.
266 265	26.6 26.5	53.2	79	8.9	106.4	133.0	159 159	1	86.2	212.8 212.0	239
264	26.4	52.8	79	0.5	105.6	132.5 132.0	158	.4 1	84.8	211.2	237
263 262	26.3 26.2	52.6 52.4	5 78	3.9	105.2 104.8	131.5 131.0	157 157		84.1 83.4	$210.4 \\ 209.6$	236 235
261	26.1	52.2	2 78	3.3	104.4	130.5	156	.6 1	82.7	208.8	234
260 259	26.0 25.9	52.0 51.8		3.0	104.0 103.6	130.0 129.5	156 155		82.0 81.3	208.0	234 233
258	25.8	51.6	3 77	7.4	103.2	129.0	154	.8 1	80.6	206.4	232.
257 256	25.7 25.6	51.4 51.5		5.8	102.8 102.4	128.5 128.0	154 153	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	79.9 79.2	$205.6 \\ 204.8$	231
255	25.5	51.0	76	5.5	102.0	127.5	153	.0 1	78.5	204.0	229

No.	170 L. 28	30.]							[N	To. 189	L. 278.
N.	0	1	2	3	4	5	6	7	8	9	Diff.
170 1 2 3	230449 2996 5528	0704 3250 5781	0960 3504 6033	1215 3757 6285	1470 4011 6537	1724 4264 6789	1979 4517 7041	2234 4770 7292	2488 5023 7544	2742 5276 7795	255 253 252
4 5 6	8046 240549 3038 5513	8297 0799 3286 5759	1048 3534 6006	1297 3782 6252	9049 1546 4030° 6499	9299 1795 4277 6745	9550 2044 4525 6991	9800 2293 4772 7237	0050 2541 5019 7482	0300 2790 5266 7728	250 249 248 246
8 9	7973 250420 2853	8219 0664 3096	8464 0908 3338	8709 1151 3580	8954 1395 3822	9198 1638 4064	9443 1881 4306	9687 2125 4548	9932 2368 4790	0176 2610 5031	245 243 242
180	5273 7679	5514 7918	5755 8158	5996 8398	6237 8637	6477 8877	6718 9116	6958 9355	7198 9594	7439 9833	241 239
2 3 4 5 6	260071 2451 4818 7172 9513	0310 2688 5054 7406 9746	0548 2925 5290 7641 9980	0787 3162 5525 7875	1025 3399 5761 8110	1263 3636 5996 8344	1501 3873 6232 8578	1739 4109 6467 8812	1976 4346 6702 9046	2214 4582 6937 9279	238 237 235 234
7 8 9	271842 4158 6462	2074 4389 6692	2306 4620 6921	0213 2538 4850 7151	0446 2770 5081 7380	0679 3001 5311 7609	0912 3233 5542 7838	1144 3464 5772 8067	1377 3696 6002 8296	1609 3927 6232 8525	233 232 230 220

1									
Diff.	1	2	3	4	5	6	7	8	9
255 254 253 253 252 251 250 249 248 247 246	25.5 25.4 25.3 25.2 25.1 25.0 24.9 24.8 24.7 24.6 24.5	51.0 50.8 50.6 50.4 50.2 50.0 49.8 49.6 49.4 49.2 49.0	76.5 76.2 75.9 75.6 75.3 75.0 74.7 74.4 74.1 73.8 73.5	102.0 101.6 101.2 100.8 100.4 100.0 99.6 99.2 98.8 98.4	127.5 127.0 126.5 126.0 125.5 125.0 124.5 124.0 123.5 123.0 122.5	153.0 152.4 151.8 151.2 150.6 150.0 149.4 148.8 148.2 147.0	178.5 177.8 177.1 176.4 175.7 175.0 174.3 173.6 172.9 172.2 171.5	204.0 203.2 202.4 201.6 200.8 200.0 199.2 198.4 197.6 196.8	229.5 228.6 227.7 226.8 225.9 225.0 224.1 223.2 222.3 221.4 220.5
245 244 243 242 241 240 239 238 237 236 235	24.5 24.4 24.3 24.2 24.1 24.0 23.9 23.8 23.7 23.6 23.5	49.0 48.8 48.6 48.4 48.2 48.0 47.8 47.6 47.4 47.2 47.0	73.2 72.9 72.6 72.3 72.0 71.7 71.4 71.1 70.8 70.5	97.6 97.2 96.8 96.4 96.0 95.6 95.2 94.8 94.4	122.0 121.5 121.0 120.5 120.0 119.5 119.0 118.5 118.0 117.5	147.0 146.4 145.8 145.2 144.6 144.0 143.4 142.8 142.2 141.6 141.0	171.5 170.8 170.1 169.4 168.7 168.0 167.3 166.6 165.9 165.2 164.5	195.0 195.2 194.4 193.6 192.8 192.0 191.2 190.4 189.6 188.8 188.0	220.5 219.6 218.7 217.8 216.9 216.0 215.1 214.2 213.3 212.4 211.5
234 233 232 231 230 229 228 227 226	23.4 23.3 23.2 23.1 23.0 22.9 22.8 22.7 22.6	46.8 46.6 46.4 46.2 46.0 45.8 45.6 45.4 45.2	70.2 69.9 69.6 69.3 69.0 68.7 68.4 68.1 67.8	93.6 93.2 92.8 92.4 92.0 91.6 91.2 90.8 90.4	117.0 116.5 116.0 115.5 115.0 114.5 114.0 113.5	140.4 139.8 139.2 138.6 138.0 137.4 136.8 136.2 135.6	163.8 163.1 162.4 161.7 161.0 160.3 159.6 158.9 158.2	187.2 186.4 185.6 184.8 184.0 183.2 182.4 181.6 180.8	210.6 209.7 208.8 207.9 207.0 206.1 205.2 204.3 203.4

No.	190 L. 27	78.]								[]	No. 214	L. 332.
N.	0	- 1	2	3		4	5	6	7	8	9	Diff.
190	278754	8982	9211	948	39	9667	9895					
1 2 3 4	281033 3301 5557 7802	1261 3527 5782 8026	1488 3753 6007 8249	171 397 623 847	32	1942 4205 6456 8696	2169 4431 6681 8920	0123 2596 4656 6905 9143	0351 2622 4882 7130 9366	0578 2849 5107 7354 9589	0806 3075 5332 7578 9812	228 227 226 225 223
5 6 7 8 9	290035 2256 4466 6665 8853	0257 2478 4687 6884 9071	0480 2699 4907 7104 9289	070 29: 512 73: 950	20 27 23	0925 3141 5347 7542 9725	1147 3363 5567 7761 9943	1369 3584 5787 7979	1591 3804 6007 8198	1813 4025 6226 8416	4246 6446	222 221 220 219
200 1 2 3 4	301030 3196 5351 7496 9630	1247 3412 5566 7710 9843	1464 3628 5781 7924	168 38- 599 813	81 14 96	1898 4059 6211 8351	2114 4275 6425 8564	0161 2331 4491 6639 8778	0378 2547 4706 6854 8991	0595 2764 4921 7068 9204	2980 5136 7282	218 217 216 215 213
5 6 7 8	311754 3867 5970 8063	1966 4078 6180 8272	0056 2177 4289 6390 8481	026 238 449 659 868)9)9	0481 2600 4710 6809 8898	0693 2812 4920 7018 9106	0906 3023 5130 7227 9314	1118 3234 5340 7436 9522	1330 3445 5551 7646 9730	3656 5760 7854	212 211 210 209 208
9 210 1 2 3	320146 2219 4282 6336 8380	0354 2426 4488 6541 8583	0562 2633 4694 6745 8787	076 285 480 695 899	39 99 50	0977 3046 5105 7155 9194	1184 3252 5310 7359 9398	1391 3458 5516 7563 9601	1598 3665 5721 7767 9805	1805 3871 5926 7972	4077 6131	207 206 205 204
4	330414	0617	0819	10:		1225	1427	1630	1832	0008 2034		203 202
					Pr	OPORT	MONAL ?	Parts.				
Diff	. 1	2	;	3		4	5	6		ĩ	8	9
225 224 223 222 221 220 219 218	22.5 22.4 22.3 22.2 22.1 22.0 21.9 21.8	45.0 44.8 44.6 44.4 44.2 44.0 43.8 43.6	67 67 66 66 66 66 65 65	.2 .9 .6 .3 .0 .7		90.0 89.6 89.2 88.8 88.4 88.0 87.6 87.2	112.5 112.0 111.5 111.0 110.5 110.0 109.5 109.0	135 134 133 133 132 132 131 130	.4 1 .8 1 .2 1 .6 1 .0 1	57.5 56.8 56.1 55.4 54.7 54.0 53.3 52.6	180.0 179.2 178.4 177.6 176.8 176.0 175.2 174.4	202.5 201.6 200.7 199.8 198.9 198.0 197.1 196.2
217 216 215 214 213 212 211 210	21.7 21.6 21.5 21.4 21.3 21.2 21.1 21.0	43.4 43.2 43.0 42.8 42.6 42.4 42.2 42.0	65 64 64 64 63 63 63 63	.8 .5 .9 .6 .3		86.8 86.4 86.0 85.6 85.2 84.8 84.4 84.0	108.5 108.0 107.5 107.0 106.5 106.0 105.5 105.0	130 129 129 128 127 127 126 126	.6 1	51.9 51.2 50.5 49.8 49.1 48.4 47.7 47.0	173.6 172.8 172.0 171.2 170.4 169.6 168.8 168.0	195.3 194.4 193.5 192.6 191.7 190.8 189.9 189.0
209 208 207 206 205 204 203 202	20.9 20.8 20.7 20.6 20.5 20.4 20.3 20.2	41.8 41.6 41.4 41.2 43.0 40.8 40.6 40.4	62 61 61 61 60	.4		83.6 83.2 82.8 82.4 82.0 81.6 81.2 00.8	104.5 104.0 103.5 103.0 102.5 102.0 101.5 101.0	125 124 124 123 123 123 121 121	.4 1 .8 1 .2 1 .6 1 .0 1 .4 1	46.3 45.6 44.9 44.2 43.5 42.8 42.1 41.4	167.2 166 4 165.6 164.8 164.0 163.2 162.4 161.6	188.1 187.2 186.3 185.4 184.5 183.6 182.7 181.8

No.	215 L. 33	2.]							[]	No. 239	L. 380.
N.	0	1	2	3	4	5	6	7	8	9	Diff.
215 6 7 8	332438 4454 6460 8456	2640 4655 6660 8656	2842 4856 6860 8 855	3044 50£7 7060 9054	5257 7260	3447 5458 7459 9451	3649 5658 7659 9650	3850 5859 7858 9849	4051 6059 8058	4253 6260 8257	202 201 200
9	340444	0642	0841	1039	1237	1435	1632	1830	0047 2028	0246 2225	199 198
220 1 2 3	2423 4392 6353 8305	2620 4589 6549 8500	2817 4785 6744 8694	3014 4981 6939 8889	5178 7135	3409 5374 7330 9278	3606 5570 7525 9472	3802 5766 7720 9666	3999 5962 7915 9860	4196 6157 8110	197 196 195
4 5 6 7 8	350248 2183 4108 6026 7935 9835	0442 2375 4301 6217 8125	0636 2568 4493 6408 8316	0829 2761 4685 6599 8506	2954 4876 6790	1216 3147 5068 6981 8886	1410 3339 5260 7172 9076	1603 3532 5452 7363 9266	1796 3724 5643 7554 9456	0054 1989 3916 5834 7744 9646	194 193 193 192 191 190
		0025	0215	0404		0783	0972	1161	1350	1539	189
230 1 2 3 4	361728 3612 5488 7356 9216	1917 3800 5675 7542 9401	2105 3988 5862 7729 9587	2294 4176 6049 7915 9772	4363 6236 8101	2671 4551 6423 8287	2859 4739 6610 8473	3048 4926 6796 8659	3236 5113 6983 8845	3424 5301 7169 9030	188 188 187 186
5 6 7 8 9	371068 2912 4748 6577 8398 38	1253 3096 4932 6759 8580	1437 3280 5115 6942 8761	1622 3464 5298 7124 8943	1806 3647 5481 7306	0143 1991 3831 5664 7488 9306	0328 2175 4015 5846 7670 9487	0513 2360 4198 6029 7852 9668	0698 2544 4382 6212 8034 9849	0883 2728 4565 6394 8216	185 184 184 183 182
				Pr	OPORTIC	ONAL PA	RTS.				
Diff	1	2	3	3	4	5 .	6		7	8	9
202 201 200 199 198 197 196 195 194	20.2 20.1 20.0 19.9 19.8 19.7 19.6 19.5 19.4	40.4 40.2 40.0 39.8 39.6 39.4 39.2 39.0 38.8	60 60 60 59 59 59 59 58 58	.3 .0 .7 .4 .1 .8 .5 .2	80.8 80.4 80.0 79.6 79.2 78.8 78.4 78.0 77.6	101.0 100.5 100.0 99.5 99.0 98.5 98.0 97.5 97.0	121. 120. 120. 119. 118. 118. 117. 117.	6 14 0 14 4 18 8 18 2 18 6 18 0 18	11.4 10.7 10.0 39.3 38.6 37.9 37.2 36.5 35.8	161.6 160.8 160.0 159.2 158.4 157.6 156.8 156.0 155.2	181.8 180.9 180.0 179.1 178.2 177.3 176.4 175.5 174.6
193 192 191 190 189 188 187 186	19 3 19 2 19 1 19 0 18 9 18 8 18 7 18 6	38.6 38.4 38.2 38.0 37.8 37.6 37.4 37.2	57. 57. 57. 56. 56. 56. 55.	.6 .3 .0 .7 .4	77.2 76.8 76.4 76.0 75.6 75.2 74.8 74.4	96.5 96.0 95.5 95.0 94.5 94.0 93.5 93.0	115. 115. 114. 114 113. 112. 112. 111.	2 18 6 18 0 18 4 18 8 18 2 18	35,1 34,4 33,7 33,0 32,3 31,6 30,9 30,2	154.4 153.6 152.8 152.0 151.2 150.4 149.6 148.8	173.7 172.8 171.9 171.0 170.1 169.2 168.3 167.4
185 184 183 182 181 180 179	18.5 18.4 18.3 18.2 18.1 18.0 17.9	37.0 36.8 36.6 36.4 36.2 36.0 35.8	55 55, 54, 54 54 54 54 54 53	2 9 6 3 0	74.0 73.6 73.2 72.8 72.4 72.0 71.6	92.5 92.0 91.5 91.0 90.5 90.0 89.5	108	0 12 4 12 8 12 2 12 6 12 0 12	29.5 28.8 28.1 27.4 26.7 26.0 25.3	148.0 147.2 146.4 145.6 144.8 144.0 143.2	166.5 165.6 164.7 163.8 162.9 162.0 161.1

No.	[No. 269 L. 431,												
N.	0	1	2	3	4	5	6	7	8	9	Diff.		
240	380211	0392	0573	0754	0934	1115	1296	1476	1656	1837	181		
1	2017	2197	2377	2557	2737	2917	3097	3277	3456	3636	180 179		
2 3 4 5	3815 5606	3995 5785	4174 5964	4353 6142	4533 6321	4712 6499	4891 6677	5070 6856	5249 7034	5428 7212	178		
4	7390	7568	7746	7924	8101	8279	8456	8634	8811	8989	178 178		
5	9166	9343	9520	9698	9875				25.22	0.000			
0	390935	1112	1288	1464	1641	0051 1817	0228 1993	0405 2169	0582 2345	0759 2521	177 176		
7	2697	2873	3048	3224	3400	3575	3751	3926	4101	4277	176		
6 7 8	4452	4627	4802	4977	5152	5326	5501	5676	5850	6025	175		
9	6199	6374	6548	6722	6896	7071	7245	7419	7592	7766	174		
250	7940	8114	8287	8461	8634	8808	8981	9154	9328	9501	173		
1	9674	9847	0020	0100	0365	0538	0711	0000	1050	1000	173		
9	401401	1573	1745	0192	2089	2261	0711 2433	0883 2605	1056 2777	1008 2049	172		
3	3121	3292	3464	3635	3807	3978	4149	4320	4193	4663	171 171		
4	4834	5005	5176	5346	5517	5688	5858	6029	6199	6370	171		
5	6540 8240	6710 8410	6881 8579	7051 8749	7221 8918	7391 9087	7561 9257	7731 9426	7901 9595	8070 9764	170 169		
2 3 4 5 6 7	9933	0410	0019	0140	0010	3001	9201	94.0	9090	9104	103		
		0102	0271	0440	0609	0777	0046	1114	1283	1451	169		
8	411620	1788	1956	2124	2293	2461	2629	2796	2964	3132	168		
9	3300	3467	3635	3803	3970	4137	4305	4472	4639	4806	167		
260	4973	5140	5307	5474	5641	5808	5974	6141	6308	6474	167		
1	6641 8301	6807 8467	6973 8633	7139 8798	7306 8964	7472 9129	7638 9295	7804 9460	7970 9625	8135 9791	166 165		
2 3	9956					0140			2020	3101	100		
		0121	0286	0451	0616	0781	0945	1110	1275	1439	165		
4 5	421604 3246	1768 3410	1933 3574	2097 3737	2261 3901	2426	2590 4228	2754 4392	2918 4555	3082 4718	164 164		
6	4882	5045	5208	5371	5534	5697	5860	6023	6186	6349	163		
7	6511	6674	6836	6999	7161	7324	7486	7648	7811	7973	162		
8	8135	8297	8459	8621	8783	8944	9106	9268	9429	9591	162		
9	9752	9914	0075	0236	0398	0559	0720	0881	1042	1203	161		
	40		0013	0.000	0.000	05.79	1 0120	1 0001	1043	1203	101		

					,				
Diff.	1	2	3	4	5	6	7	8	9
178	17.8	35.6	53.4	71.2	89.0	106.8	124.6	142.4	160.2
177	17.7	35.4	53.1	70.8	88.5	106.2	123.9	141.6	
									159.3
176	17.6	35.2	52.8	70.4	88.0	105.6	123.2	140.8	158.4
175	17.5	35.0	52.5	70.0	87.5	105.0	122.5	140.0	157.5
174	17.4	34.8	52.2	69.6	87.0	104.4	121.8	139.2	156.6
173	17.3	34.6	51.9	69.2	86.5	103.8	121.1	138.4	155.7
172	17.2	34.4	51.6	68.8	86.0	103.2	120.4	137.6	154.8
171	17.1	34.2	51.3	68.4	85.5	102.6	119.7	136.8	153.9
170	17.0	34.0	51.0	68.0	85.0	102.0	119.0	136.0	153.0
110			31.0	00.0	00.0	102.0	115.0	100.0	100.0
169	16.9	33.8	50.7	67.6	84.5	101.4	118.3	135.2	152.1
168	16.8	33.6	50.4	67.2	84.0	100.8	117.6	134.4	151.2
167	16.7	33.4	50.1	66.8	83.5	100.2	116.9	133.6	150.3
166	16.6	33.2	49.8	66.4	83.0	99.6	116.2	132.8	149.4
165	16.5	33.0	49.5	66.0	82.5	99.0		132.0	
							115.5		148.5
164	16.4	32.8	49.2	65.6	82.0	98.4	114.8	131.2	147.6
163	16.3	32.6	48.9	65.2	81.5	97.8	114.1	130.4	146.7
162	16.2	32.4	48.5	64.8	81.0	97.2	113.4	129.6	145.8
161	16.1	32.2	48.3	64.4	80.5	96.6	112.7	128.8	144.9

No.	270 L. 43	1.]							[N	o. 299]	L. 476,
N.	0	1	2	3	4	5	6	7	8	9	Diff.
270 1 2 3 4 5	431364 2969 4569 6163 7751 9333	1525 3130 4729 6322 7909 9491	1685 3290 4888 6481 8067 9648	1846 3450 5048 6640 8226 9806	2007 3610 5207 6799 8384 9964	2167 3770 5367 6957 8542	2328 3930 5526 7116 8701	2488 4090 5685 7275 8859	2649 4249 5844 7433 9017	2809 4409 6004 7592 9175	161 160 159 159 158
6 7 8 9 280	440909 2480 4045 5604 7158	1066 2637 4201 5760 7313	1224 2793 4357 5915 7468	1381 2950 4513 6071 7623	1538 3106 4669 6226 7778	0122 1695 3263 4825 6382 7933	0279 1852 3419 4981 6537 8088	0437 2009 3576 5137 6692 8242	0594 2166 3732 5293 6848 8397	0752 2323 3889 5449 7003 8552	158 157 157 156 155 155
1 2 3 4 5 6 7 8	8706 450249 1786 3318 4845 6366 7882 9392	0403 1940 3471 4997 6518 8033 9543	9015 0557 2093 3624 5150 6670 8184 9694	9170 0711 2247 3777 5302 6821 8336 9845	9324 0865 2400 3930 5454 6973 8487 9995	9478 1018 2553 4082 5606 7125 8638	9633 1172 2706 4235 5758 7276 8789	9787 1326 2859 4387 5910 7428 8940	9941 1479 3012 4540 6062 7579 9091	0095 1633 3165 4692 6214 7731 9242	154 154 153 153 152 152 152 151
9 290 1 2 3 4 5	460898 2398 3893 5383 6868 8347 9822	1048 2548 4042 5532 7016 8495 9969	1198 2697 4191 5680 7164 8643	1348 2847 4340 5829 7312 8790	1499 2997 4490 5977 7460 8938	0146 1649 3146 4639 6126 7608 9085	0296 1799 3296 4788 6274 7756 9233	0447 1948 3445 4936 6423 7904 9380	0597 2098 3594 5085 6571 8052 9527	0748 2248 3744 5234 6719 8200 9675	151 150 150 149 149 148 148
6 7 8 9	471292 2756 4216 5671	1438 2903 4362 5816	0116 1585 3049 4508 5962	0263 1732 3195 4653 6107	0410 1878 3341 4799 6252	0557 2025 3487 4944 6397	0704 2171 3633 5090 6542	0851 2318 3779 5235 6687	0998 2464 3925 5381 6832	1145 2610 4071 5526 6976	147 146 146 146 146 145
				Pro	PORTIC	ONAL P.	ARTS.				
Diff	2. 1	2	1 8		4	5	6		7	8	9
161 160 159 158 157 156 155 154 153 152 151 150 149	16.1 16.0 15.9 15.8 15.7 15.6 15.5 15.4 15.3 15.2 15.1	32.2 32.0 31.8 31.6 31.4 31.2 31.0 30.8 30.6 30.4 30.2 30.0 29.8	48 48 47 47 47 46 46 46 45 45 45 45	.5 .2 .9 .6 .3	64.4 64.0 63.6 63.2 62.8 62.4 62.0 61.6 61.2 60.8 60.4 60.0 65.0	80.5 80.0 79.5 79.0 78.5 78.0 77.5 76.0 75.5 75.0 74.5	96.6 96.0 95.4 94.8 93.6 93.6 92.8 91.8 90.6 99.4 88.8	10 10 10 10 10 10 10 10 10 10 10 10 10 1	12.7 12.0 11.3 10.6 10.9 10.9 10.2 10.5 10.6 10.7 10.6 10.6 10.7 10.6 10.6 10.6 10.6 10.6 10.6 10.6 10.6	128.8 128.0 127.2 126.4 125.6 124.8 124.0 123.2 122.4 121.6 120.8 120.0 119.2 118.4 117.6	144.9 144.0 143.1 142.2 141.3 140.4 139.5 138.6 137.7 136.8 135.9 135.0 134.1 133.2
148 147 146 145 144 143 142 141 140	14.8 14.7 14.6 14.5 14.4 14.3 14.2 14.1 14.0	29.6 29.4 29.2 29.0 28.8 28.6 28.4 28.2	44 43 43 43 42 42 42 42 42	.1 .8 .5 .2 .9	59.2 58.8 58.4 58.0 57.6 57.2 56.8 56.4 56.0	74.0 73.5 73.0 72.5 72.0 71.5 71.0 70.5 70.0	88.8 88.2 87.6 87.6 86.4 85.8 85.8 84.6 84.6	2 10 3 10 0 10 4 10 8 10	03.6 02.9 02.2 01.5 00.8 00.1 09.4 08.7 08.0	118.4 117.6 116.8 116.0 115.2 114.4 113.6 112.8 112.0	133.2 132.3 131.4 130.5 129.6 128.7 127.8 126.9 126.0

No. 8	300 L. 47	7.]							[N	o. 339 I	. 531
N.	0	1	2	8	4	5	6	7	8	9	Diff.
300	477121 8566	726 6 8711	7411 8855	7555 8999	7700 9143	7844 9287	7989 9431	8133 9575	8278 9719	8422 9863	145 144
2345678	480007 1443 2874 4300 5721 7138 8551	0151 1586 3016 4442 5863 7280 8692	0294 1729 3159 4585 6005 7421 8833	0438 1872 3302 4727 6147 7563 8974	0582 2016 3445 4869 6289 7704 9114	0725 2159 3587 5011 6430 7845 9255	0869 2302 3730 5153 6572 7986 9396	1012 2445 3872 5295 6714 8127 9537	1156 2588 4015 5437 6855 8269 9677	1299 2731 4157 5579 6997 8410 9818	144 143 143 143 143 141 141
9	9958	0099	0239	0380	0520	0661	0801	0941	1081	1222	140
3 4 5 6	491362 2760 4155 5544 6930 8311 9687	1502 2900 4294 5683 7068 8448 9824	1642 3040 4433 5822 7206 8586 9962	1782 3179 4572 5960 7344 8724	1922 3319 4711 6099 7483 8862	2062 3458 4850 6238 7621 8999	2201 3597 4989 6376 7759 9137	2341 3737 5128 6515 7897 9275	2481 3876 5267 6653 8035 9412	6791 8173	140 139 139 139 139 138
7 8 9	501059 2427 3791	1196 2564 3927	1333 2700 4063	0099 1470 2837 4199	0236 1607 2973 4335	0374 1744 3109 4471	0511 1880 3246 4607	0648 2017 3382 4743	0785 2154 3518 4878	2291 3655	13 13 13 13
320 1 2 3	5150 6505 7856 9203	5286 6640 7991 9337	5421 6776 8126 9471	5557 6911 8260 9606	5693 7046 8395 9740	5828 7181 8530 9874	5964 7316 8664	6099 7451 8799	6234 7586 8934	7721 9068	130 131 13
4 5 6 7 8 9	510545 1883 3218 4548 5874 7196 8514	0679 2017 3351 4681 6006 7328 8646	0813 2151 3484 4813 6139 7460 8777	0947 2284 3617 4946 6271 7592 8909	1081 2418 3750 5079 6403 7724 9040	1215 2551 3883 5211 6535 7855 9171	0009 1349 2684 4016 5344 6668 7987 9303	0143 1482 2818 4149 5476 6800 8119 9434	0277 1616 2951 4288 5609 6938 8251	5 1750 8084 2 4415 5741 2 7064 8282	13 13 13 13 13 13 13
1	9828	9959	0090	0221 1530	0353	0484	0615	0745	0876	1007	
2 3 4 5 6 7 8	521138 2444 3746 5045 6339 7630 8917	1269 2575 3876 5174 6469 7759 9045	1400 2705 4006 5304 6598 7888 9174	1530 2835 4136 5434 6727 8016 9302	1661 2966 4266 5563 6856 8145 9430	1792 3096 4396 5693 6985 8274 9559	1922 3226 4526 5822 7114 8402 9687	2053 3356 4656 5951 7243 8531 9815	2185 3486 4785 6081 7375 8660 9945	3616 4915 6210 7501 8788	13 13 13 13 12 12 12
9	530200	0328	0456	0584	0712	0840	0968	1096	1223	- 0072 3 1351	12 12
				Pro	PORTIO	NAL PA	ARTS.				
Diff	2. 1	2	1 :	3	4	5	6		7	8	9
139 138 137 136	13.9 13.8 13.7 13.6	27.8 27.6 27.4 27.2	41	.7 .4 .1	55.6 55.2 54.8 54.4	69.5 69.0 68.5 68.0	83. 82. 82. 81.	2 9)7.3)6.6)5.9)5.2	111.2 110.4 109.6 108.8	125 124 123 122

137	13.7	27.4	41.1	54.8	68.5	82.2	95.9	109.6	123.3
136	13.6	27.2	40.8	54.4	68.0	81.6	95.2	108.8	122.4
135	13.5	27.0	40.5	54.0	67.5	81.0	94.5	108.0	121.5
134	13.4	26.8	40.2	53.6	67.0	80.4	93.8	107.2	120.6
133	13.3	26.6	39.9	53.2	66.5	79.8	93.1	106.4	119.7
132	13.2	26.4	39.6	52.8	66.0	79.2	92.4	105.6	118.8
131	13.1	26.2	89.3	52.4	65.5	78.6	91.7	104.8	117.9
130	13.0	26.0	89.0	52.0	65.0	78.0	91.0	104.0	117.0
129	12.9	25.8	38.7	51.6	64.5	77.4	90.3	103.2	116.1
128	12.8	25.6	38.4	51.2	64.0	76.8	89.6	102.4	115.2
127	12 7	25.4	38.1	50.8	63.5	76.2	88.9	101.6	114.3

No. 8	340 L. 53	31.]							[N	io, 379	L. 579.
N.	0	1	2	8	4	5	6	7	8	9	Diff.
340 1 2 3 4 5 6	531479 2754 4026 5294 6558 7819 9076	1607 2882 4153 5421 6685 7945 9202	1734 3009 4280 5547 6811 8071 9327	1862 3136 4407 5674 6937 8197 9452	1990 3264 4534 5800 7063 8322 9578	2117 3391 4661 5927 7189 8448 9703	2245 3518 4787 6053 7315 8574 9829	2372 3645 4914 6180 7441 8699 9954	2500 3772 5041 6306 7567 8825	-	128 127 127 126 126 126
7 8 9	540329 1579 2825	0455 1704 2950	0580 1829 3074	0705 1953 3199	0830 2078 3323	0955 2203 3417	1080 2327 3571	1205 2452 3696	1330 2576 3820	1454 2701	125 125 125 124
350 1 2 3 4	4068 5307 6543 7775 9003	4192 5431 6666 7898 9126	4316 5555 6789 8021 9249	4440 5678 6913 8144 9371	4564 5802 7036 8267 9494	4688 5925 7159 8389 9616	4812 6049 7282 8512 9739	4936 6172 7405 8635 9861	5060 6296 7529 8758 9984	6419 7652 8881	124 124 123 123
5 6 7 8 9	550228 1450 2668 3883 5094	0351 1572 2790 4004 5215	0473 1694 2911 4126 5336	0595 1816 3033 4247 5457	0717 1938 3155 4368 5578	0840 2060 3276 4489 5699	0962 2181 3398 4610 5820	1084 2303 3519 4731 5940	1206 2425 3640 4852 6061	2547 3762	123 122 122 121 121 121 121
360 1 2 3	6303 7507 8709 990 7	6423 7627 8829	6544 7748 8948	6664 7868 9068	6785 7988 9188	6905 8108 9308	7026 8228 9428	7146 8349 9548	7267 8469 9667	7387	120 120 120
4 5 6 7 8	561101 2293 3481 4666 5848 7026	0026 1221 2412 3600 4784 5966 7144	0146 1340 2531 3718 4903 6084 7262	0265 1459 2650 3837 5021 6202 7379	0385 1578 2769 3955 5139 6320 7497	0504 1698 2887 4074 5257 6437 7614	0624 1817 3006 4192 5376 6555 7732	0743 1936 3125 4311 5494 6673 7849	0863 2055 3244 4429 5612 6791 7967	2174 3362 4548	119 119 119 119 118 118 118
370	820 2 9374	8319 949 1	8436 9608	8554 9725	8671 9842	8788 9959	8905	9023	9140	_	117
2 3 4 5 6 7 8 9	570543 1709 2872 4031 5188 6341 7492 8639	0660 1825 2988 4147 5303 6457 7607 8754	0776 1942 3104 4263 5419 6572 7722 8868	0893 2058 3220 4379 5534 6687 7836 8983	1010 2174 3336 4494 5650 6802 7951 9097	1126 2291 3452 4610 5765 6917 8066 9212	0076 1243 2407 3568 4726 5880 7032 8181 9326	0193 1359 2523 3684 4841 5996 7147 8295 9441	0309 1476 2639 3800 4957 6111 7262 8410 9555	1592 2755 3915 5072 6226 7377	717 116 116 116 116 115 115 115 114
				Pro	PORTIC	NAL PA	RTS.				
Diff	. 1	2	3	3	4	5	G		7	8	9
128 127 126 125 124 123 122 121 120 119	12.8 12.7 12.6 12.5 12.4 12.3 12.2 12.1 12.0 11.9	25.6 25.4 25.2 25.0 24.8 24.6 24.4 24.2 24.0 23.8	38 38 37 37 37 36 36 36 36 36	.1 .8 .5 .2 .9 .6 .3	51.2 50.8 50.4 50.0 49.6 49.2 48.8 48.4 48.0 47.6	64.0 63.5 63.0 62.5 62.0 61.5 61.0 60.5 60.0 59.5	76.8 76.9 75.6 75.0 74.4 73.8 73.2 72.6 72.0 71.4	88 88 88 86 86 85 84 84 84	.7	102.4 101.6 100.8 100.0 99.2 98.4 97.6 96.8 96.0 95.2	115.2 114.3 113.4 112.5 111.6 110.7 109.8 108.9 108.0 107.1

No. 8	380. L. 57	79.]	•						[N	o. 414	L. 617.
N.	0	1	2	3	4	5	6	7	8	9	Diff.
380	579784	9898	0012	0126	0241	0355	0469	0583	0697	0811	114
	580925	1039	1153	1267	1381	1495	1608	1722	1836	1950	
1 9	2063	2177	2291	2404	2518	2631	2745	2858	2972	3085	
2 3	3199	3312	3426	3539	3652	3765	3879	3992	4105	4218	
4	4331	4444	4557	4670	4783	4896	5009	5122	5235	5348	113
4 5	5461	5574	5686	5799	5912	6024	6137	6250	6362	6475	
6	6587	6700	6812	6925	7037	7149	7262	7374	7486	7599	
7	7711	7823	7935	8047	8160	8272	8384	8496	8608	8720	112
- 8	8832	8944	9056	9167	9279	9391	9503	9615	9726	9838	1
9	9950	0061	0173	0284	0396	0507	0619	0730	0842	0953	
390	591065	1176	1287	1399	1510	1621	1732	1843	1955	2066	
	2177	2288	2399	2510	2621	2732	2843	2954	3064	3175	111
1 2	3286	3397	3508	3618	3729	3840	3950	4061	4171	4282	
3	4393	4503	4614	4724	4834	4945	5055	5165	5276	5386	
4	5496	5606	5717	5827	5937	6047	6157	6267	6377	6487	110
5	6597	6707	6817	6927	7037	7146	7256	7366	7476	7586	110
6	7695	7805	7914	8024	8134	8243	8353	8462 9556	8572 9665	8681 9774	
7	8791	8900	9009	9119	9228	9337	9446	9550	3002	3114	400
8	9883	9992	0101	0210	C319	0428	0537	0646	0755	0864	109
9	600973	1082	1191	1299	1408	1517	1625	1734	1843	1951	
400	2060	2169	2277	2386	2494	2603	2711	2819	2928	3036	
	3144	3253	3361	3469	3577	3686	3794	3902	4010	4118	108
2	4226	4334	4442	4550	4658	4766	4874	4982	5089	5197	
1 2 3 4	5305	5413	5521	5628	5736	5844	5951	6059	6166	6274	1
- 4	6381	6489	6596	6704 7777	6811	6919	7026	7133	7241	7348	
5	7455	7562	7669	77777	7884	7991	8098	8205	8313	8419	107
6 7	8526	8633	8740	8847	8954	9061	9167	9274	9381	9488	
1 7	9594	9701	9808	9914	0021	0128	0234	0341	0447	0554	
8	610660	0767	0873	0979	1086	1192	1298	1405	1511	1617	
9	1723	1829	1936	2042	2148	2254	2360	2466	2572	2678	106
410	2784	2890	2996	3102	3207	3313	3419	3525	3630	3736	100
1	3842	3947	4053	4159	4264	4370	4475	4581	4686	4792	
2	4897	5003	5108	5213	5319	5424	5529	5634	5740	5845	1
3 4	5950	6055	6160	6265	6370	6476	6581	6686	6790	6895	105
4	7000	7105	7210	7315	7420	7525	7629	7734	7839	7943	1

Diff.	1	2	3	4	5	6	7	8	9
118 117 116 115 114 113 112	11.8 11.7 11.6 11.5 11.4 11.3 11.2	23.6 23.4 23.2 23.0 22.8 22.6 22.4	35.4 35.1 34.8 34.5 34.2 33.9 33.6	47.2 46.8 46.4 46.0 45.6 45.2 44.8	59.0 58.5 58.0 57.5 57.0 56.5 56.0	70.8 70.2 69.6 69.0 68.4 67.8 67.2	82.6 81.9 81.2 80.5 79.8 79.1 78.4	94.4 93.6 92.8 92.0 91.2 90.4 89.6	106.2 105.3 104.4 103.5 102.6 101.7 100.8
111 110 109 108 107 106 105 105 104	11.1 11.0 10.9 10.8 10.7 10.6 10.5 10.5	22.2 22.0 21.8 21.6 21.4 21.2 21.0 21.0 20.8	33.3 33.0 32.7 32.4 32.1 31.8 31.5 31.5 31.2	41.4 41.0 43.6 43.2 42.8 42.4 42.0 42.0 41.6	55.5 55.0 54.5 54.0 53.5 53.0 52.5 52.5 52.0	66.6 66.0 65.4 64.8 64.2 63.6 63.0 63.0 62.4	77.7 77.0 76.3 75.6 74.2 73.5 73.5 72.8	88.8 88.0 87.2 86.4 85.6 84.8 84.0 83.2	99.9 99.0 98.1 97.2 96.3 95.4 94.5 94.5 93.6

No.	415 L. 61	8.]							[1	No. 459 I	L. 662
N.	0	1	2	3	4	5	6	7	8	9	Diff.
415	618048 9093	8153 9198	8257 9302	8362 9406	8466 9511	8571 9615	8676 9719	8780 9824	8884 9928	8989	105
8 9	620136 1176 2214	0240 1280 2318	0344 1384 2421	0448 1488 2525	0552 1592 2628	0656 1695 2732	0760 1799 2835	0864 1903 2939	0968 2007 3042	2110	104
420 1 2 3 4 5 6	3249 4282 5312 6340 7366 8389	3353 4385 5415 6443 7468 8491	3456 4488 5518 6546 7571 8593	3559 4591 5621 6648 7673 8695	3663 4695 5724 6751 7775 8797 9817	3766 4798 5827 6853 7878 8900	3869 4901 5929 6956 7980 9002	3973 5004 6032 7058 8082 9104	4076 5107 6135 7161 8185 9206	5210 6238 7263 8287	103
7 8 9	9410 630428 1444 2457	9512 0530 1545 2559	9613 0631 1647 2660	9715 0733 1748 2761	0835 1849 2862	9919 0936 1951 2963	0021 1038 2052 3064	0123 1139 2153 3165	0224 1241 2255 3266	1342 2356	
430 1 2 3 4 5 6	3468 4477 5484 6488 7490 8489 9486	3569 4578 5584 6588 7590 8589 9586	3670 4679 5685 6688 7690 8689 9686	3771 4779 5785 6789 7790 8789 9785	3872 4880 5886 6889 7890 8888 9885	3973 4981 5986 6989 7990 8988 9984	4074 5081 6087 7089 8090 9088	4175 5182 6187 7189 8190 9188	4276 5283 6287 7290 8290 9287	5383 6388 7390 8389	101
7 8 9	640481 1474 2465	0581 1573 2563	0680 1672 2662	0779 1771 2761	0879 1871 2860	0978 1970 2959	0084 1077 2069 3058	0183 1177 2168 3156	0283 1276 2267 3255	1375 2366	99
440 1 2 3 4 5 6	3453 4439 5422 6404 7383 8360 9335	3551 4537 5521 6502 7481 8458 9432	3650 4636 5619 6600 7579 8555 9530	3749 4734 5717 6698 7676 8653 9627	3847 4832 5815 6796 7774 8750 9724	3946 4931 5913 6894 7872 8848 9821	4044 5029 6011 6992 7969 8945 99 19	4143 5127 6110 7089 8067 9043	4242 5226 6208 7187 8165 9140	5324 6306 7285 8262 9237	98
8 9	650308 1278 2246	0405 1375 2343	0502 1472 2440	0599 1569 2536	0696 1666 2633	0793 1762 2730	0890 1859 2826	0016 0987 1956 2923	0113 1084 2053 3019	1181	97
450 1 2 3 4 5 6 7	3213 4177 5138 6098 7056 8011 8965	3309 4273 5235 6194 7152 8107 9060	3405 4369 5331 6290 7247 8202 9155	3502 4465 5427 6386 7343 8298 9250	3598 4562 5523 6482 7438 8393 9346	3695 4658 5619 6577 7534 8488 9441	3791 4754 5715 6673 7629 8584 9536	3888 4850 5810 6769 7725 8679 9631	3984 4946 5906 6864 7820 8774 9726	5042 6002 6960 7916 8870	96
8 9	9916 660865 1813	0011 0960 1907	0106 1055 2002	0201 1150 2096	0296 1245 2191	0391 1339 2286	0486 1434 2380	0581 1529 2475	0676 1623 2569	0771 1718 2663	95
				Pro	PORTIO	NAL PA	RTS.				
Diff		2			4	5	6		7	8	. 9
105 104 103 102 101 100 99	10 5 10 4 10 3 10 2 10 1 10.0 9 9	21.0 20 8 20 6 20 4 20 2 20 0 19 8	31 30 30 30 30 30 29	.0	42.0 41 6 41.2 40 8 40.4 40 0 39 6	52 5 52.0 51 5 51 0 50 5 50 0 49 5	63 6 62 4 61 8 61 8 60 6 60 6 59 4	75 1 72 3 72 71 5 70 1 69	3.5 8 1 4 7 0 3	84 0 83 2 82.4 81 6 80 8 80 0 79 2	94.5 93.6 92.7 91.8 90.9 90.0 89.1

L. 69	o. 499 l	[N							2.]	460 L. 66	No.
Diff	9	8	7	6	5	4	3	2	1	0	N
	3607	3512	3418	3324	3230	3135	3041	2947	2852	662758	160
	4548	4454	4360	4266	4172	4078	3983	3889	3795	3701	1
9	5487 6424	5393	5299	5206	5112	5018	4924	4830	4736	4642	2
	7360	6331 7266	6237 7173	6143 7079	6050 6986	5956 6892	5862 6799	5769 6705	5675 6612	5581 6518	3
	8293	8199	8106	8013	7920	7826	7733	7640	7546	7453	5
	9224	9131	9038	8945	8852	8759	8665	8572	8479	8386	3 4 5 6 7
9	0153	0060	9967	9875	9782	9689	9596	9503	9410	9317	7
ð	1080	0988	0895	0802	0710	0617	0524	0431	0339	670246	8
	2005	1913	1821	1728	1636	1543	1451	1358	1265	1173	9
	2929	2836	2741	2652	2560	2467	2375	2283	2190	2098	170
	3850	3758	3666	3574	3482	3390	3297	3205	3113	3021	
9	4769	4677	4586	4494	4402	4310	4218	4126	4034	3942	1 2 3 4 5 6
	5687 6602	5595 6511	5503 6419	5412 6328	5320 6236	5228 6145	5137 6053	5045 5962	4953 5870	4861 5778	3
	7516	7424	7333	7242	7151	7059	6968	6876	6785	6694	5
	8427	8336	8245	7242 8154	8063	7972	7881	7789	7698	7607	6
9	9337	9246	9155	9064	8973	8882	8791	8700	8609	8518	7
	0245	0154	0063	9973	9882	9791	9700	9610	9519	9428	8
	1151	1060	0970	0879	0789	0698	0607	0517	0426	680336	9
	2055	1964	1874	1784	1693	1603	1513	1422	1332	1241	480
9	2957	2867	2777	2686	2596	2506	2416	2326	2235	2145	1
9	3857 4756	3767 4666	3677 4576	3587 4486	3497 4396	3407 4307	3317 4217	3227 4127	3137 4037	3047 3947	3
	5652	5563	5473	5383	5294	5204	5114	5025	4935	4845	4
	6547	6458	6368	5383 6279	6189	6100	6010	5921	5831	5742	5
	7410	7351	7261	7172	7083 7975	6994	6904	6815	6726	6636	6
8	8331 9220	8242 9131	8153 9042	8064 8953	7975	7886 8776	7796 8687	7707 8598	7618 8509	7529 8420	4 5 6 7 8
	9220	9151	9930	9841	8865 9753	9664	9575	9486	9398	9309	9
	0107	0019									Ü
	0993	0905	0816	0728 1612	0639	0550	0462	0373	0285	690196	490
	1877	1789	1700	1612	1524	1435	1347	1258	1170 2053	1081 1965	1
8	2759 3639	2671 3551	2583 3463	2494 3375	2406 3287	2318 3199	2230 3111	2142 3023	2935	1965 2847	3
	4517	4430	4342	4254	4166	4078	3991	3903	3815	3727	3 4
	5394	5307	5219	5131	5044	4956	4868	4731	4693	4605	5
	6269	6182	6094	6007	5919	5832	5744	5657	5569	5482	5 6 7
	7142 8014	7055 7926	6968 7839	6880 7752	6793 7665	6706 7578	6618 7491	6531 7404	6444 7317	6356 7229	8
8	8883	8796	8709	8622	8535	8149	8362	8275	8188	8100	8

Diff.	1	2	3	4	5	6	7	8	9
98 97 96 95 94 93 92 91 90 89 88 87 86	9.8 9.7 9.6 9.5 9.3 9.3 9.2 9.1 9.8 8.8 8.7	19.6 19.4 19.2 19.0 18.8 18.6 18.4 18.2 17.8 17.6 17.4	29.4 29.1 28.8 28.5 28.2 27.9 27.6 27.3 27.0 26.7 26.4 25.8	39.2 38.8 38.4 38.0 37.6 37.2 36.8 36.4 35.6 35.6 35.2 34.8	49.0 48.5 48.0 47.5 47.0 46.5 46.0 45.5 44.0 43.5 43.0	58.8 58.2 57.6 57.0 56.4 55.8 55.2 54.6 53.4 52.8 52.8 52.6	68.6 67.9 67.2 66.5 65.8 65.1 64.4 63.0 62.3 61.6 60.9	78.4 77.6 76.8 76.0 75.2 74.4 73.6 72.0 71.2 70.4 68.8	88.2 87.3 86.4 85.5 84.6 83.7 82.8 81.9 81.0 80.1 79.2 78.3

[No. 544 L. 736.

No. 500 L. 698.]

N.	0	1	2	.3	4	5	6	7	8	9	Diff.
500	698970 9838	9057 9924	9144	9231	9317	9404	9491	9578	9664	9751	
2 3 4 5 6 7 8 9	700704 1568 2431 3291 4151 5008 5864 6718	0790 1654 2517 3377 4236 5094 5949 6803	0011 0877 1741 2603 3463 4322 5179 6035 6888	0098 0963 1827 2689 3549 4408 5265 6120 6974	1050 1913 2775 3635 4494 5350 6266	0271 1136 1999 2861 3721 4579 5436 6291 7144	0358 1222 2086 2947 3807 4665 5522 6376 7229	0444 1309 2172 3033 3893 4751 5607 6462 7315	0531 1395 2258 3119 3979 4837 5698 6547 7400	5 1482 3 2344 9 3205 9 4065 7 4922 3 5778 6632	86
510	7570 8421 9270	7655 8506 9355	7740 8591 9440	7826 8676 9524	8761	7996 8846 9694	8081 8931 9779	8166 9015 9863	8251 9100 9948	9185	85
3 4 5 6 7 8	710117 0963 1807 2650 3491 4330 5167	0202 1048 1892 2734 3575 4414 5251	0287 1132 1976 2818 3659 4497 5335	0371 1217 2060 2902 3742 4581 5418	0456 1301 2144 2 2986 2 3826 4665	0540 1385 2229 3070 3910 4749 5586	0625 1470 2313 3154 3994 4833 5669	0710 1554 2397 3238 4078 4916 5753	0794 1639 2481 3328 4169 5000 5836	- 0033 4 0879 9 1723 1 2566 3 3407 2 4246 9 5084	84
520 1 2 3 4	6003 6838 7671 8502 9331	6087 6921 7754 8585 9414	6170 7004 7837 8668 9497	6254 7088 7920 8751 9580	8003 8834	6421 7254 8086 8917 9745	6504 7338 8169 9000 9828	6588 7421 8253 9083 9911	6671 750- 8336 9165 9994	7587 8419 9248	83
5 6 7 8 9	720159 0986 1811 2634 3456	0242 1068 1893 2716 3538	0325 1151 1975 2798 3620	0407 1233 2058 2881 3702	0490 3 1316 3 2140 2963	0573 1398 2222 3045 3866	0655 1481 2305 3127 3948	0738 1563 2387 3209 4030	0821 1646 2469 3291 4115	- 0077 1 0903 5 1728 0 2552 1 3374	82
530 1 2 3 4 5 6	4276 5095 5912 6727 7541 8354 9165 9974	4358 5176 5993 6809 7623 8435 9246	4440 5258 6075 6890 7704 8516 9327	4522 5340 6150 6972 7785 8597 9408	5422 6 6238 7053 7866 8678	4685 5503 6320 7134 7948 8759 9570	4767 5585 6401 7216 8029 8841 9651	4849 5667 6483 7297 8110 8922 9732	4951 5748 6564 7379 8191 9008 9818	5830 4 6646 9 7460 1 8273 3 9084	81
8 9	730782 1589	0055 0863 1669	0136 0944 1750	0217 1024 1830	1105	0378 1186 1991	0459 1266 2072	0540 1347 2152	0621 1428 2238	3 1508	
540 1 2 3 4	2394 3197 3999 4800 5599	2474 3278 4079 4880 5679	2555 3358 4160 4960 5759	2635 3438 4240 5040 5838	3518 4320 5120	2796 3598 4400 5200 5998	2876 3679 4480 5279 6078	2956 3759 4560 5359 6157	3037 3839 4640 5439 6237	3117 3919 4720 5519	80
				PR	OPORTIC	NAL PA	ARTS.				
Diff	. 1	2	3		4	5	6		7	8	9
87 86 85 84	8.7 8.6 8.5 8.4	17.4 17.2 17.0 16.8	26 25 25 25 25	1 .8 .5 .2	34.8 34.4 34.0 33.6	43 5 43 0 42 5 42 0	52 2 51 6 51.0 50.4	60	0.9	69 6 68 8 68 0 67.2	78 3 77 4 76 5 75 6

	545 L. 78	10.]							[N	o. 584	L. 10
N.	0	1	2	3	4	5	C	7	8	9	Dif
545	736397	6476	6556	6635	6715	6795	6874	6954	7034	7113	
6	7193	7272	7352	7431	7511	7590	7670	7749	7829	7908	
7	7987	8067	8146	8225	8305	7590 8384	8463	8543	8622	8701	
8	8781	8860	8939	9018	9097	9177	9256	9335	8622 9414	9493	
9	9572	9651	9731	9810	9889	9968			0111	0100	
							0047	0126	0205	0284	7
50	740363	0442	0521	0600	0678	0757	0836	0915	0994	1073	ì
1	1152	1230	1309	1388	1467	1546	1624	1703	1782	1860	
2	1939	2018	2096	2175	9954	1546 2332	2411	2480	2568	2647	
2 3	2725	2804	2882	2961	2254 3039	3118	3196	2489 3275	2568 3353	3431	
4	3510	3588	3667	2961 3745	3823	3902	3980	4058	4136	4915	
5	4293	4371	4449	4528	4606	4684	4762	4840	4919	4007	}
6	4293 5075	5153	4449 5231	5309	5387	5465	5543	5621	5699	4215 4997 5777	7
7	5855	5933	6011	6089	6167	6245	6323	6401	6479	6556	١ '
4 5 6 7 8	6634	6712	6790	6868	6945	7023	7101	7179	7256	7334	
9	7412	7489	7567	7645	7722	7800	7878	7955	8033	8110	
60	8188	8266	8343	8421	8498	8576	8653	8731	8808	8885	
1	8963	9040	9118	9195	9272	9350	9427	9504	9582	9659	
2	9736	9814	9891	9968		2000		3304	3002	3003	}
					0045	0123	0200	0277	0354	0431	
3	750508	0586	0663	0740	0817	6894	0971	1048	1125	1202	
4	1279	1356	1433	1510	1587	1664	1741	1818	1895	1972	,
5	2048	2125	2202	2279	2356	1664 2433	2509	1818 2586	2663	2740	
6	2816	2893	2970	3047	3123 3889	3200 3966	3277	3353	3430	3506 4272	
7	3583	3660	3736	3813	3889	3966	2509 3277 4042	4119	4195	4272	8
8	4348	4425	4501	4578	4654	4730	4807	4883	4960	5036	
9	5112	5189	5265	5341	5417	5494	5570	5646	5722	5799	
70	5875	5951	6027	6103	6180	6256	6332	6408	6484	6560	
1	6636	6712	6788	6864	6940	7016	7092	7168	7244	7320	1 7
2	7396	7472	7548	7624	7700	7775	7851	7927	8003	8079	
2 3 4	8155	8230	8306	8382	8458	8533	8609	8685	8761	8836	
	8912	8988	9063	9139	9214	9290	9366	9441	9517	9592	1
5	9668	9743	9819	9894	9970						
c	760422	0498	0550	0010	0504	0045	0121	0196	0272 1025 1778	0347	
6	1176	1251	0573 1326	0649 1402	0724 1477	0799	0875	0950	1025	1101 1853	
8	1928	2003	2078		1411	1552	1627	1702	1448	1853	
9	2679	2754	2829	2153 2904	2228 2978	2303	2378	2453	2529	2604	1 7
-						3053	3128	3203	3278	3353	
580	3428	3503	3578	3653	3727	3802	3877	3952	4027 4774	4101	
1	4176	4251	4326	4400	4475	4550 5296	4624 5370	4699	4774	4848	
3	4923	4998	5072	5147	5221	5296	5310	5445	5520	5594	
4	5669	5743	5818	5892	5966	6041	6115	6190	6264	6338	
4	6413	6487	6562	6636	6710	6785	6859	6933	7007	7082	

PROPORTIONAL PARTS.

Diff.	1	2	3	4	5	6	7	8	9
83 82 81 80 79 78 77 76 75	8.3 8.2 8.1 8.0 7.8 7.6 7.5 7.4	16.6 16.4 16.2 16.0 15.8 15.6 15.4 15.2 15.0 14.8	24.9 24.6 24.3 24.0 23.7 23.4 23.1 22.8 22.5 22.2	33.2 32.8 32.4 32.0 31.6 31.2 30.8 30.4 30.0 29.6	41.5 41.0 40.5 40.0 39.5 39.0 38.5 38.0 37.5 37.0	49.8 49.2 48.6 48.0 47.4 46.8 46.2 45.6 44.4	58.1 57.4 56.7 56.0 55.3 54.6 53.9 53.2 52.5 51.8	66.4 65.6 64.8 64.0 63.2 62.4 61.6 60.8 60.0 59.2	74.7 73.8 72.9 72.0 71.1 70.2 69.3 68.4 67.5 66.6

No.	585 L. 76	7.]							[]	No. 629	L. 799
N.	0	1	2	3	4	5	6	7	8	9	Diff.
585 6 7 8	767156 7898 8638 9377	7230 7972 8712 9451	7304 8046 8786 9525	7379 8120 8860 9599	7453 8194 8934 9673	7527 8268 9008 9746	7601 8342 9082 9820	7675 8416 9156 9894	7749 8490 9230 9968	7823 8564 9303	74
9	770115	0189	0263	0336	0410	0484	0557	0631	0705	- 0042 0778	
590 1 2 3 4 5 6 7 8	0852 1587 2322 3055 3786 4517 5246 5974 6701 7427	0926 1661 2395 3128 3860 4590 5319 6047 6774 7499	0999 1734 2468 3201 3933 4663 5392 6120 6846 7572	1073 1808 2542 3274 4006 4736 5465 6193 6919 7644	1146 1881 2615 3348 4079 4809 5538 6265 6992 7717	1220 1955 2688 3421 4152 4882 5610 6338 7064 7789	1293 2028 2762 3494 4225 4955 5683 6411 7137 7862	1367 2102 2835 3567 4298 5028 5756 6483 7209 7934	1440 2175 2908 3640 4371 5100 5829 6556 7282 8006	1514 2248 2981 3713 4444 5173 5902 6629 7354 8079	73
600	8151 8874 9596	8224 8947 9669	8296 9019 9741	8368 9091 9813	8441 9163 9885	8513 9236 9957	8585 9308	8658 9380	8730 9452		
3 4 5 6 7 8 9	780317 1037 1755 2473 3189 3904 4617	0389 1109 1827 2544 3260 3975 4689	0461 1181 1899 2616 3332 4046 4760	0533 1253 1971 2688 3403 4118 4831	0605 1324 2042 2759 3475 4189 4902	0677 1396 2114 2831 3546 4261 4974	0029 0749 1468 2186 2902 3618 4332 5045	0101 0821 1540 2258 2974 3689 4403 5116	0173 0893 1612 2329 3046 3761 4475 5187	0965 1684 2401 3117 3832 4546	72
610 1 2 3 4 5 6	5330 6041 6751 7460 8168 8875 9581	5401 6112 6822 7531 8239 8946 9651	5472 6183 6893 7602 8310 9016 9722	5543 6254 6964 7673 8381 9087 9792	5615 6325 7035 7744 8451 9157 9863	5686 6396 7106 7815 8522 9228 9933	5757 6467 7177 7885 8593 9299	5828 6538 7248 7956 8663 9369	5899 6609 7319 8027 8734 9440	6680 7390 8098 8804	71
7 8 9	790285 0988 1691	0356 1059 1761	0426 1129 1831	0496 1199 1901	0567 1269 1971	0637 1340 2041	0004 0707 1410 2111	0074 0778 1480 2181	0144 0848 1550 2252	0918 1620 2322	
620 1 2 3 4 5 6 7	2392 3092 3790 4488 5185 5880 6574 7268 7960	2462 3162 3860 4558 5254 5949 6644 7337 8029	2532 3231 3930 4627 5324 6019 6713 7406 8098	2602 3301 4000 4697 5393 6088 6782 7475 8167	2672 3371 4070 4767 5463 6158 6852 7545 8236	2742 3441 4139 4836 5532 6227 6921 7614 8305	2812 3511 4209 4906 5602 6297 6990 7683 8374	2882 3581 4279 4976 5672 6366 7060 7752 8443	2952 3651 4349 5045 5741 6436 7129 7821 8513	3721 4418 5115 5811 6505 7198 7890 8582	70
9	8651	8720	8789	.8858	8927	8996	9065	9134	9203	9272	69
				Pro	PORTIO	NAL PA	RTS.				
Diff	f. 1	2		3	4	5	6		7	8	9
75 74 73 72 71 70 69	7.5 7.4 7.3 7.2 7.1 7.0 6.9	15.0 14.8 14.6 14.4 14.2 14.0 13.8	22 21 21 21 21	.2 .9 .6 .3	30.0 29.6 29.2 28.8 28.4 28.0 27.6	37.5 37.0 36.5 36.0 35.5 35.0 34.5	45.44.43.43.43.42.042.041.	5 5 5 5 4 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6	2.5 1.8 1.1 0.4 9.7 9.0 8.3	60.0 59.2 58.4 57.6 56.8 56.0 55.2	67. 66. 65. 64. 63. 63. 62.

No.	630 L. 79	99.]							[]	No. 674	L. 829.
N.	0	1	2	3	4	5	6	7	8	9	Diff.
630	799341	9409	9478	9547	9616	9685	9754	9823	9892	9961	
1 2 3 4 5 6 7 8 9	800029 0717 1404 2089 2774 3457 4139 4821 5501	0098 0786 1472 2158 2842 3525 4208 4889 5569	0167 0854 1541 2226 2910 3594 4276 4957 5637	0236 0923 1609 2295 2979 3662 4344 5025 5705	0305 0992 1678 2363 3047 3730 4412 5093 5773	0373 1061 1747 2432 3116 3798 4480 5161 5841	0442 1129 1815 2500 3184 3867 4548 5229 5908	0511 1198 1884 2568 3252 3935 4616 5297 5976	0580 1266 1952 2637 3321 4003 4685 5365 6044	3 1335 2 2021 2705 1 3389 3 4071 4753 5 5433	68
640 1 2 3 4 5	806180 6858 7535 8211 8886 9560	6248 6926 7603 8279 8953 9627	6316 6994 7670 8346 9021 9694	6384 7061 7738 8414 9088 9762	6451 7129 7806 8481 9156 9829	6519 7197 7873 8549 9223 9896	6587 7264 7941 8616 9290 9964	6655 7332 8008 8684 9358	6728 7400 8076 8751 9425	7467 8143 8818	
6 7 8 9	810233 0904 1575 2245	0300 0971 1642 2312	0367 1039 1709 2379	0434 1106 1776 2445	0501 1173 1843 2512	0569 1240 1910 2579	0636 1307 1977 2646	0031 0703 1374 2044 2713	0098 0770 1441 2111 2780	0 083? 1 1508 1 2178 0 2847	67
650 1 2 3 4 5 6 7 8 9	2913 3581 4248 4913 5578 6241 6904 7565 8286 8885	2980 3648 4314 4980 5644 6308 6970 7631 8292 8951	3047 3714 4381 5046 5711 6374 7036 7698 8358 9017	3114 3781 4447 5113 5777 6440 7102 7764 8424 9083	3181 3848 4514 5179 5843 6506 7169 7830 8490 9149	3247 3914 4581 5246 5910 6573 7235 7896 8556 9215	3314 3981 4647 5312 5976 6639 7301 7962 8622 9281	3381 4048 4714 5378 6042 6705 7367 8028 8688 9346	3448 4114 4780 5445 6109 6771 7432 8094 8754 9412	4 4181 4847 5 5511 6 175 6 6838 7499 4 8160 4 8820	66
660 1 2 3 4 5 6 7 8 9 670 1 2 3 4	9544 820201 0858 1514 2168 2822 3474 4126 4776 6723 7369 8015 8660	9610 0267 0924 1579 2233 2887 3539 4191 4841 5491 6140 6787 7434 8080 8724	9676 0333 0989 1645 2299 2952 3605 4256 4906 5556 6204 6852 7499 8144 8789	9741 0399 1055 1710 2364 3018 3670 4321 4971 5621 6269 6917 7563 8209 8853	9807 0464 1120 1775 2430 3083 3735 4386 5036 5686 6334 6981 7628 8273 8918	9873 0530 1186 1841 2495 3148 3800 4451 5101 5751 6399 7046 7692 8338 8982	9939 0595 1251 1906 2560 3213 3865 4516 5166 5815 6464 7111 7757 8402 9046	0004 0661 1317 1972 2626 3279 3930 4581 5231 5880 6528 7175 7821 8467 9111	0070 0727 1382 2037 2691 3344 3996 4646 5296 5945 6593 7240 7886 8531 9175	0792 1448 2103 2756 4061 64061 65361 6658 7305 7951 8595	65
			7	Pro	PORTIO	nal Pa	RTS.				
:Diff	1	2	9		4	5	6		7	8	9
68 67 66 65 64	6 8 6 7 6 6 6 5 6.4	13 6 13 4 13.2 13 0 1£ 8	20 20 19 19 19	8	27 2 26 8 26 4 26 0 25 6	34 0 33 5 33 0 32.5 32 0	40 8 40 2 39 6 39 0 38.4	46 46 45	9 2 5	54 4 53 6 52 8 52 0 51 2	61 2 60 3 59 4 58 5 57.6

L. 857	1			1	1					1	
Diff	9	8	7	6	5	4	3	2	1	0	N.
	9882	9818	9754	9690	9625	9561	9497	9432	9368	329304 9947	6
6-	0525 1166 1806 2445	0460 1102 1742 2381	0396 1037 1678 2317	0332 0973 1614 2253	0268 0909 1550 2189	0204 0845 1486 2126	0139 0781 1422 2062	0075 0717 1358 1998	0011 0653 1294 1934	330589 1230 1870	-
	3083 3721 4357 4993 5627 6261	3020 3657 4294 4929 5564 6197	2956 3593 4230 4866 5500 6134	2892 3530 4166 4802 5437 6071	2828 3466 4103 4739 5373 6007	2764 3402 4039 4675 5310 5944	2700 3338 3975 4611 5247 5881	2637 3275 3912 4548 5183 5817	2573 3211 3848 4484 5120 5754	2509 3147 3784 4421 5056 5691	80 1 2 3
65	6894 7525 8156 8786	6830 7462 8093 8723 9352	6767 7399 8030 8660 9289	6704 7336 7967 8597 9227	6641 7273 7904 8534 9164	6577 7210 7841 8471 9101	6514 7146 7778 8408 9038	6451 7083 7715 8345 8975	6387 7020 7652 8282 8912	6324 6957 7588 8219 8849	4 5 6 7 8 9
	0043	9981	9918	9855	9792	9729	9667	9604	9541	9478	1
	0671 1297 1922 2547 3170 3793 4415 5036	0608 1234 1860 2484 3108 3731 4353 4974	0545 1172 1797 2422 3046 3669 4291 4912	0482 1109 1735 2360 2983 3606 4229 4850	0420 1046 1672 2297 2921 3544 4166 4788	0357 0984 1610 2235 2859 3482 4104 4726	0294 0921 1547 2172 2796 3420 4042 4664	0232 0859 1485 2110 2734 3357 3980 4601	0169 0796 1422 2047 2672 3295 3918 4539	840106 0733 1359 1985 2609 3233 3855 4477	2 3 4 5 6 7 8 9
6	5656 6275 6894 7511 8128 8743 9358 9972	5594 6213 6832 7449 8066 8682 9297 9911	5532 6151 6770 7388 8004 8620 9235 9849	5470 6090 6708 7326 7943 8559 9174 9788	5408 6028 6646 7264 7881 8497 9112 9726	5346 5966 6585 7202 7819 8435 9051 9665	5284 5904 6523 7141 7758 8374 8989 9604	5222 5842 6461 7079 7696 8312 8928 9542	5160 5780 6399 7017 7634 8251 8866 9481	5098 5718 6337 6955 7573 8189 8805 9419	700 1 2 3 4 5 6 7
	0585 1197	0524 1136	0462 1075	0401 1014	0340 0952	0279 0891	0217 0830	0156 0769	0095 0707	850033 0646	8 9
6	1809 2419 3029 3637 4245 4852 5459 6064 6668 7272	1747 2358 2968 3577 4185 4792 5398 6003 6608 7212	1686 2297 2907 3516 4124 4731 5337 5943 6548 7152	1625 2236 2846 3455 4063 4670 5277 5882 6487 7091	1564 2175 2785 3394 4002 4610 5216 5822 6427 7031	1503 2114 2724 3333 3941 4549 5156 5761 6366 6970	1442 2053 2663 3272 3881 4488 5095 5701 6306 6910	1381 1992 2602 3211 3820 4428 5034 5640 6245 6850	1320 1931 2541 3150 3759 4367 4974 5580 6185 6789	1258 1870 2480 3090 3698 4306 4913 5519 6124 6729	710 1 2 3 4 5 6 7 8 9
				RTS.	NAL PA	PORTIO	Pro				
. 9	8	7		6	5	4	3	;	2	1	Diff.
58 57 56 55 54 54	52.0 51.2 50.4 49.6 48.8 48.0	5.5 1.8 1.1 3.4 2.7 2.0	44	39.0 38.4 37.8 37.8 36.6 36.0	32.5 32.0 31.5 31.0 30.5	26.0 25.6 25.2 24.8 24.4	.9	19 19 18 18 18 18	13.0 12.8 12.6 12.4 12.2	6.5 6.4 6.3 6.2 6.1	65 64 63 62 61

No.	720 L. 85	7.]	1		1	11		ı	LI	Vo. 764	L, 883
N.	0	1	2	3	4	5	6	7	8	9	Diff.
720 1 2 3 4	857332 7935 8537 9138 9739	7393 7995 8597 9198 9799	7453 8056 8657 9258 9859	7513 8116 8718 9318 9918	7574 8176 8778 9379 9978	7634 8236 8838 9439	7694 8297 8898 9499	7755 8357 8958 9559	7815 8417 9018 9619	7875 8477 9078 9679	60
5 6 7 8 9	860338 0937 1534 2131 2728	0398 0996 1594 2191 2787	0458 1056 1654 2251 2847	0518 1116 1714 2310 2906	0578 1176 1773 2370 2966	0038 0637 1236 1833 2430 3025	0098 0697 1295 1893 2489 3085	0158 0757 1355 1952 2549 3114	0218 0817 1415 2012 2608 3204	0278 0877 1475 2072 2668 3263	
730 1 2 3 4 5 6 7 8 9	3323 3917 4511 5104 5696 6287 6878 7467 8056 8644	3382 3977 4570 5163 5755 6346 6937 7526 8115 8703	3442 4036 4630 5222 5814 6405 6996 7585 8174 8762	3501 4096 4689 5282 5874 6465 7055 7644 8233 8821	3561 4155 4748 5341 5933 6524 7114 7703 8292 8879	3620 4214 4808 5400 5992 6583 7173 7762 8350 8938	3680 4274 4867 5459 6051 6642 7232 7821 8409 8997	3739 4333 4926 5519 6110 6701 7291 7880 8468 9056	3799 4392 4985 5578 6169 6760 7350 7939 8527 9114	3858 4452 5045 5637 6228 6819 7409 7998 8586 9173	59
740 1	9232 9818	9290 9877	9349 9935	9408 9994	9466	9525	9584	9642	9701	9760	
2 3 4 5 6 7 8 9	870404 0989 1573 2156 2739 3321 3902 4482	0462 1047 1631 2215 2797 3379 3960 4540	0521 1106 1690 2273 2855 3437 4018 4598	0579 1164 1748 2331 2913 3495 4076 4656	0638 1223 1806 2389 2972 3553 4134 4714	0111 0696 1281 1865 2448 3030 3611 4192 4772	0170 0755 1339 1923 2506 3088 3669 4250 4830	0228 0813 1398 1981 2564 3146 3727 4308 4888	0287 0872 1456 2040 2622 3204 3785 4366 4945	0345 0930 1515 2008 2681 3262 3844 4424 5003	58
750 1 2 3 4 5 6 7	5061 5640 6218 6795 7371 7947 8522 9096 9669	5119 5698 6276 6853 7429 8004 8579 9153 9726	5177 5756 6333 6910 7487 8062 8637 9211 9784	5235 5813 6391 6968 7544 8119 8694 9268 9841	5293 5871 6449 7026 7602 8177 8752 9325 9898	5351 5929 6507 7083 7659 8234 8809 9383 9956	5409 5987 6564 7141 7717 8292 8866 9440	5466 6045 6622 7199 7774 8349 8924 9497	552 4 6102 6680 7256 7832 8407 8981 9555	5582 6160 6737 7314 7889 8464 9039 9612	
9	880242	0299	0356	0413	0471	0528	$0013 \\ 0585$	$0070 \\ 0642$	0127 0699	0185 0756	
760 1 2 3 4	0814 1385 1955 2525 3093	0871 1442 2012 2581 3150	0928 1499 2069 2638 3207	0985 1556 2126 2695 3264	1042 1613 2183 2752 3321	1099 1670 2240 2809 3377	1156 1727 2297 2866 3434	1213 1784 2354 2923 3491	1271 1841 2411 2980 3548	1328 1898 2468 3037 3605	57
				Pro	PORTIC	NAL PA	RTS.				
Diff	. 1	2	8		4	5	6		7	8	9
59 58 57 56	5.9 5.8 5.7 5.6	11.8 11.6 11.4 11.2	17 17 17 17 16	7 .4 .1 .8	23.6 23.2 22.8 22.4	29.5 29.0 28.5 28.0	35.4 34.8 34.2 33.6	8 40	1.3 0.6 0.9 0.2	47.2 46.4 45.6 44.8	53. 52. 51. 50.

No.	765 L. 88	3.]							[No. 809	L. 908.
N.	0	1	2	3	4	5	6	7	8	9	Diff.
765 6 7 8 9	883661 4229 4795 5361 5926	3718 4285 4852 5418 5983	3775 4342 4909 5474 6039	3832 4399 4965 5531 6096	3888 4455 5022 5587 6152	3945 4512 5078 5644 6209	4002 4569 5135 5700 6265	4059 4625 5192 5757 6321	4115 4682 5248 5813 6378	2 4739 5305 5 5870	
770 1 2 3 4 5 6	6491 7054 7617 8179 8741 9302 9862	6547 7111 7674 8236 8797 9358 9918	6604 7167 7730 8292 8853 9414 9974	6660 7223 7786 8348 8909 9470	6716 7280 7842 8404 8965 9526	6773 7336 7898 8460 9021 9582	6829 7392 7955 8516 9077 9638	6885 7449 8011 8573 9134 9694	6948 7505 8067 8629 9190 9750	7561 8123 8685 9246	56
7 8 9	890421 0980 1537	0477 1035 1593	0533 1091 1649	$0030 \\ 0589 \\ 1147 \\ 1705$	0086 0645 1203 1760	0141 0700 1259 1816	0197 0756 1314 1872	0253 0812 1370 1928	0309 0868 1426 1988	3 0924 3 1482	
780 1 2 3 4 5 6 7 8 9	2095 2651 3207 3762 4316 4870 5423 5975 6526 7077	2150 2707 3262 3817 4371 4925 5478 6030 6581 7132	2206 2762 3318 3873 4427 4980 5533 6085 6636 7187	2262 2818 3373 3928 4482 5036 5588 6140 6692 7242	2317 2873 3429 3984 4538 5091 5644 6195 6747 7297	2373 2929 3484 4039 4593 5146 5699 6251 6802 7352	2429 2985 3540 4094 4648 5201 5754 6306 6857 7407	2484 3040 3595 4150 4704 5257 5809 6361 6912 7462	2546 3096 3651 4206 4759 5312 5864 6416 6967 7517	3151 3706 4261 9 4814 2 5367 4 5920 6471 7022	
790 1 2 3 4	7627 8176 8725 9273 9821	7682 8231 8780 9328 9875	7737 8286 8835 9383 9930	7792 8341 8890 9437 9985	7847 8396 8944 9492	7902 8451 8999 9547	7957 8506 9054 9602	8012 8561 9109 9656	8067 8615 916- 9711	8670 9218 9766	55
5 6 7 8 9	900367 0913 1458 2003 2547	0422 0968 1513 2057 2601	0476 1022 1567 2112 2655	0531 1077 1622 2166 2710	0039 0586 1131 1676 2221 2764	0094 0640 1186 1731 2275 2818	0149 0695 1240 1785 2329 2873	0203 0749 1295 1840 2384 2927	0258 0804 1349 1894 2438 2981	0859 1404 1 1948 3 2492	
800 1 2 3 4 5 6 7 8 9	3090 3633 4174 4716 5256 5796 6335 6874 7411 7949	3144 3687 4229 4770 5310 5850 6389 6927 7465 8002	3199 3741 4283 4824 5364 5904 6443 6981 7519 8056	3253 3795 4337 4878 5418 5958 6497 7035 7573 8110	3307 3849 4391 4932 5472 6012 6551 7089 7626 8163	3361 3904 4445 4986 5526 6066 6604 7143 7680 8217	3416 3958 4499 5040 5580 6119 6658 7196 7734 8270	3470 4012 4553 5094 5634 6173 6712 7250 7787 8324	3524 4066 4607 5148 5688 6227 6766 7304 7841 8378	3578 3578 364120 4661 35202 35742 6281 6820 7358 7895	54
				Pro	PORTIC	nal Pa	RTS.				
Diff	f. 1	2		3	4	5	6		7	8	9
57 56 55 54	5.7 5.6 5.5 5.4	11.4 11.2 11.0 10.8	17 16 16 16	.8	22.8 22.4 22.0 21.6	28.5 28.0 27.5 27.0	34.5 33.6 33.6 32.4	3 3	9.9 9.2 8.5 7.8	45.6 44.8 44.0 43.2	51.3 50.4 49.5 48.6

No.	810 L . 90	8.]							[]	No. 854]	L. 931.
N.	0	1	2	3	4	5	6	7	8	9	Diff.
810 1 2	908485 9021 9556	8539 9074 9610	8592 9128 9663	8646 9181 9716	8699 9235 9770	8753 9289 9823	8807 9342 9877	8860 9396 9930	8914 9449 9984	8967 9503	
3 4 5 6 7 8	910091 0624 1158 1690 2222 2753 3284	0144 0678 1211 1743 2275 2806 3337	0197 0731 1264 1797 2328 2859 3390	0251 0784 1317 1850 2381 2913 3443	0304 0838 1371 1903 2435 2966 3496	0358 0891 1424 1956 2488 3019 3549	0411 0944 1477 2009 2541 3072 3602	0464 0998 1530 2063 2594 3125 3655	0518 1051 1584 2116 2647 3178 3708	1104 1637 2169 2700 3231	53
820 1 2 3 4 5 6 7 8 9	3814 4343 4872 5400 5927 6454 6980 7506 8030 8555	3867 4396 4925 5453 5980 6507 7033 7558 8083 8607	3920 4449 4977 5505 6033 6559 7085 7611 8135 8659	3973 4502 5030 5558 6085 6612 7138 7663 8188 8712	4026 4555 5083 5611 6138 6664 7190 7716 8240 8764	4079 4608 5136 5664 6191 6717 7243 7768 8293 8816	4132 4660 5189 5716 6243 6770 7295 7820 8345 8869	4184 4713 5241 5769 6296 (822 7348 7873 8397 8921	4237 4766 5294 5822 6349 6875 7400 7925 8450 8973	4819 5347 5875 6401 6927 7453 7978 8502	
830	9078 9601	9130 9653	9183 9706	9235 9758	9287 9810	9340 9862	9392 9914	9444 9967	9496		
2 3 4 5 6 7 8 9	920123 0645 1166 1686 2206 2725 3244 3762	0176 0697 1218 1738 2258 2777 3296 3814	0228 0749 1270 1790 2310 2829 3348 3865	0280 0801 1322 1842 2362 2881 3399 3917	0332 0853 1374 1894 2414 2933 3451 3969	0384 0906 1426 1946 2466 2985 3503 4021	0436 0958 1478 1998 2518 3037 3555 4072	0489 1010 1530 2050 2570 3089 3607 4124	0019 0541 1068 1588 2108 2628 3140 3658 4176	0593 1114 2 1634 2 2154 2 2674 0 3192	52
840 1 2 3 4 5 6 7 8 9 850	4279 4796 5312 5828 6342 6857 7370 7883 8396 8908 9419	4331 4848 5364 5879 6394 6908 7422 7935 8447 8959	4383 4899 5415 5931 6445 6959 7473 7986 8498 9010	4434 4951 5467 5982 6497 7011 7524 8037 8549 9061 9572	4486 5003 5518 6034 6548 7062 7576 8088 8601 9112 9623	4538 5054 5570 6085 6600 7114 7627 8140 8652 9163 9674	4589 5106 5621 6137 6651 7165 7678 8191 8703 9215 9725	4641 5157 5673 6188 6702 7216 7730 8242 8754 9266 9776	4698 5209 5723 6240 6754 7268 7781 8298 8805 9317 9827	8 4744 9 5261 5 5776 0 6291 4 6805 7319 7832 8 8345 8 8857 9368	
1 2 3 4	9930 930440 0949 1458	9981 0491 1000 1509	0032 0542 1051 1560	0083 0592 1102 1610	0134 0643 1153 1661	0185 0694 1204 1712	0236 0745 1254 1763	0287 0796 1305 1814	0338 0847 1356 1863	0898	51
				Pro	PORTIO	NAL PA	RTS.	,			
Diff	2. 1	2	8	3	4	5	6		7	8	9
53 52 51 50	5.3 5.2 5.1 5.0	10.6 10.4 10.2 10.0	15 15 15 15	.6 .3	21.2 20.8 20.4 20.0	26.5 26.0 25.5 25.0	31.8 31.2 30.6 30.6	36	7.1 5.4 5.7 5.0	42.4 41.6 40.8 40.0	47.7 46.8 45.9 45.0

[No. 899 L. 954,

No. 855 L. 931.]

	N.	0	1	2	3	4	5	6	7	8	9	Diff.
	355 6 7 8 9	931966 2474 2981 3487 3993	2017 2524 3031 3538 4044	2068 2575 3082 3589 4094	2118 2626 3133 3639 4145	2169 2677 3183 3690 4195	2220 2727 3234 3740 4246	2271 2778 3285 3791 4296	2322 2829 3335 3841 4347	2372 2879 3386 3892 4397	2930 3437 2 3943	
	860 1 2 3 4 5 6 7 8 9	4498 5003 5507 6011 6514 7016 7518 8019 8520 9020	4549 5054 5558 6061 6564 7066 7568 8069 8570 9070	4599 5104 5608 6111 6614 7116 7618 8119 8620 9120	4650 5154 5658 6162 6665 7167 7668 8169 8670 9170	4700 5205 5709 6212 6715 7217 7718 8219 8720 9220	4751 5255 5759 6262 6765 7267 7769 8269 8770 9270	4801 5306 5809 6313 6815 7317 7819 8320 8820 9320	4852 5356 5860 6363 6865 7367 7869 8370 8870 9369	4902 5406 5910 6413 6910 7418 7919 8420 8920 9419	5 5457 5960 5960 6463 6966 7468 77969 9470 8970 9469	50
	870	9519	9569	9619	9669	9719	. 9769	9819	9869	9918		
	1 2 3 4 5 6 7 8	940018 0516 1014 1511 2008 2504 3000 3495 3989	0068 0566 1064 1561 2058 2554 3049 3544 4038	0118 0616 1114 1611 2107 2603 3099 3593 4088	0168 0666 1163 1660 2157 2653 3148 3643 4137	0218 0716 1213 1710 2207 2702 3198 3692 4186	0267 0765 1263 1760 2256 2752 3247 3742 4236	0317 0815 1313 1809 2306 2801 3297 3791 4285	0367 0865 1362 1859 2355 2851 3346 3841 4335	0417 0915 1412 1909 2405 2901 3396 3890 4384	0964 1462 1958 2455 2950 3445 3939 4433	
	880 1 2 3 4 5 6 7 8 9	4483 4976 5469 5961 6452 6943 7434 7924 8413 8902	4532 5025 5518 6010 6501 6992 7483 7973 8462 8951	4581 5074 5567 6059 6551 7041 7532 8022 8511 8999	4631 5124 5616 6108 6600 7090 7581 8070 8560 9048	4680 5173 5665 6157 6649 7139 7630 8119 8608 9097	4729 5222 5715 6207 6698 7189 7679 8168 8657 9146	4779 5272 5764 6256 6747 7238 7728 8217 8706 9195	4828 5321 5813 6305 6796 7287 7777 8266 8755 9244	4877 5370 5862 6354 6845 7336 7826 8315 8804 9292	5912 6403 6894 7385 7875 8364 8853	49
18	890	9390 9878	9439 9926	9488 9975	9536	9585	9634	9683	9731	9780	9829	
	2 3 4 5 6 7 8 9	950365 0851 1338 1823 2308 2792 3276 3760	0414 0900 1386 1872 2356 2841 3325 3808	0462 0949 1435 1920 2405 2889 3373 3856	0024 0511 0997 1483 1969 2453 2938 3421 3905	0073 0560 1046 1532 2017 2502 2986 3470 3953	0121 0608 1095 1580 2066 2550 3034 3518 4001	0170 0657 1143 1629 2114 2599 3083 3566 4049	0219 0706 1192 1677 2163 2647 3131 3615 4098	0267 0754 1240 1726 2211 2696 3180 3663 4146	0316 0803 1289 1775 2260 2744 3228 3711 4194	
					Pro	PORTIO	NAL PA	RTS.				
	Diff.	1	2	3		4	5	6	1	7	8	9
	51 50 49 48	5.1 5.0 4.9 4.8	10.2 10.0 9.8 9.6	15. 15. 14. 14.	$\begin{array}{c c}0\\7\end{array}$	20.4 20.0 19.6 19.2	25.5 25.0 24.5 24.0	30.6 30.0 29.4 28.8	35 35 34 33	.3	40.8 40.0 39.2 38.4	45.9 45.0 44.1 43.2

N.	0	1	2	3	4	5	6	7	8	9	Diff
000	954243	4291	4339	4387	4435	4484	4532	4580	4628	4677	
1	4725	4773	4821	4869	4918	4966	5014	5062	5110	5158	
2	5207	5255	5303	5351	5399	5447	5495	5543	5592	5640	
3	5688	5736	5784	5832	5880	5928	5976	6024	6072	6120	
4 5 6 7	6168	6216	6265	6313	6361	6409	6457	6505	6553	6601	4
5	6649	6697	6745	6793	6840	6888	6936	6984	7032	7080	_ *
6	7128	7176	7224	7272	7320	7368	7416	7464	7512	7559	
7	7607	7655	7703	7751	7799	7847	7894	7942	7990	8038	
8	8086	8134	8181	8229 8707	8277	8325	8373	8421 8898	8468	8516 8994	
	8564	8612	8659		8755	8803	8850		8946		
010	9041	9089	9137	9185	9232	9280	9328	9375	9423	9471	
1 2	9518 9995	9566	9614	9661	9709	9757	9804	9852	9900	9947	
	0000	0042	0090	0138	0185	0233	0280	0328	0376	0423	
3	960471	0518	0566	0613	0661	0709	0756	0804	0851	0899	
4	0946	0994	1041	1089	1136	1184	1231 1706	1279 1753	1326	1374	
4 5 6 7 8	1421	1469	1516	1563	1611	1658	1706	1753	1801	1848	1
6	1895	1943	1990	2038	2085	2132	2180	2227	2275	2322	
7	2369	2417	2464	2511	2559	2606	2653	2701	2748	2795	
8	2843	2890	2937	2985	3032	3079	3126	3174	3221	3268	
9	3316	3363	3410	3457	3504	3552	3599	3646	3693	3741	
920	3788	3835	3882	3929	3977	4024	4071	4118	4165	4212	
1	4260	4307	4354	4401	4448	4495	4542	4590	4637	4684	
2	4731	4778	4825	4872	4919	4966	5013	5061	5108	5155	
3	5202	5249 5719	5296	5343	5390	5437	5484	5531	5578	5625	
2 3 4 5 6 7	5672	5719	5766	5813	5860	5907	5954	6001 6470	6048	6095 6564	1
e e	6142 6611	6189 6658	6236 6705	6283 6752	6329 6799	6376 6845	6423 6892	6939	6517 6986	7033	
7	7080	7127	7173	7220	7967	7314	7361	7408	7454	7501	
8	7548	7595	7642	7688	7267 7735	7782	7829	7875	7922	7969	
9	8016	8062	8109	8156	8203	8249	8296	8343	8390	8436	
30	8483	8530	8576	8623	8670	8716	8763	8810	8856	8903	
1	8950	8996	9043	9090	9136	9183	9229	9276	9323	9369	
2	9416	9463	9509	9556	9602	9649	9695	9742	9789	9835	
3	9882	9928	9975								
				0021	0068	0114	0161	0207	0254	0300	
4	970347	0393	0440	0486	0533	0579	0626	0672	0719	0765	
5	0812	0858	0904	0951	0997	1044	1090	1137	1183	1229	
6	1276	1322	1369	1415	1461	1508	1554	1601	1647	1693	
6 7 8	1740	1786	1832	1879	1925 2388	1971 2434	2018 2481	2064 2527	2110 2573	2157 2619	
9	2203 2666	2249 2712	2295 2758	2342 2804	2851	2897	2943	2989	3035	3082	-
									3497	3543	
40	3128 3590	3174	3220 3682	3266 3728	3313 3774	3359 3820	3405 3866	3451 3913	3959	4005	
$\frac{1}{2}$	4051	3636 4097	4143	4189	4235	4281	4327	4374	4420	4466	
3	4512	4558	4604	4650	4696	4742	4788	4834	4880	4926	
4	4972	5018	5064	5110	5156	5202	5248	5294	5340	5386	4

Diff.	1	2	3	4	5	6	7	8	9
47	4.7	9.4	14.1	18.8	23.5	28.2	32.9	37.6	42.3
46		9.2	13.8	18.4	23.0	27.6	32.2	36.8	41.4

No.	945 L. 9	75.]								[No. 989	L. 995.	
N.	0	1	2	3	4		5	6	7	8	9	Diff.	
945 6 7 8 9	975432 5891 6350 6808 7266	5478 5937 6396 6854 7312	5524 5983 6442 6900 7358	5570 6029 6488 6946 7403	5616 6075 6533 6992 7449		5662 6121 6579 7037 7495	5707 6167 6625 7083 7541	5753 6212 6671 7129 7586	579 625 671 717 763	8 6304 7 6763 5 7220		
950 1 2 3 4	7724 8181 8637 9093 9548	7769 8226 8683 9138 9594	7815 8272 8728 9184 9639	7861 8317 8774 9230 9685	7906 8363 8819 9275 9730		7952 8409 8865 9321 9776	7998 8454 8911 9366 9821	8043 8500 8956 9412 9867	808 854 900 945 991	6 8591 2 9047		
5 6 7 8 9	980003 €458 0912 1366 1819	0049 0503 0957 1411 1864	0094 0549 1003 1456 1909	0140 0594 1048 1501 1954			0231 0685 1139 1592 2045	0276 0730 1184 1637 2090	0322 0776 1229 1683 2135	036 082 127 172 218	1 0867 5 1320 8 1773 1 2226		
960 1 2 3 4 5 6 7 8 9	2271 2723 3175 3626 4077 4527 4977 5426 5875 6324	2316 2769 3220 3671 4122 4572 5022 5471 5920 6369	2362 2814 3265 3716 4167 4617 5067 5516 5965 6413	2407 2859 3310 3762 4212 4662 5112 5561 6010 6458	2452 2904 3356 3807 4257 4707 5157 5606 6055 6503		2497 2949 3401 3852 4302 4752 5202 5651 6100 6548	2543 2994 3446 3897 4347 4797 5247 5696 6144 6593	2588 3040 3491 3942 4392 4842 5292 5741 6189 6637	263 308 353 398 443 488 533 578 623 668	66 5830 4 6279 2 6727	45	
970 1 2 3 4 5 6 7	6772 7219 7666 8113 8559 9005 9450 9895	6817 7264 7711 8157 8604 9049 9494 9939	6861 7309 7756 8202 8648 9094 9539 9983	6906 7353 7800 8247 8693 9138 9583	6951 7398 7845 8291 8737 9183 9628		6996 7443 7890 8336 8782 9227 9672	7040 7488 7934 8361 8826 9272 9717	7085 7532 7979 8425 8871 9316 9761	713 757 802 847 891 936 980	1 9405		
8 9	990339 0783	0383 0827	0428 0871	0028 0472 0916	0072 0516 0960		0117 0561 1004	0161 0605 1049	0206 0650 1093	025 069 113	4 0738		
980 1 2 3 4 5 -6 7 8 9	1226 1669 2111 2554 2995 3436 3877 4317 4757 5196	1270 1713 2156 2598 3039 3480 3921 4361 4801 5240	1315 1758 2200 2642 3083 3524 3965 4405 4845 5284	1359 1802 2244 2686 3127 3568 4009 4449 4889 5328	1403 1846 2288 2730 3172 3613 4053 4493 4933 5372		1448 1890 2333 2774 3216 3657 4097 4537 4977 5416	1492 1935 2377 2819 3260 3701 4141 4581 5021 5460	1536 1979 2421 2863 3304 3745 4185 4625 5065 5504	158 202 246 290 334 378 422 466 510 554	3 2067 5 2509 7 2951 8 3392 9 3833 9 4273 9 4713 8 5152	44	
	Proportional Parts.												
Diff	. 1	2	3		4		5	6		7	8	9	

	22. 22. 21.	0
		0

27.6 27.0 26.4 25.8 32.2 31.5 30.8 30.1 36.8 36.0 35.2 34.4 41.4 40.5 39.6 38.7

18.4 18.0 17.6 17.2

4.6 4.5 4.4 4.3

46

45 44 43 $9.2 \\ 9.0 \\ 8.8 \\ 8.6$

13.8 13.5 13.2 12.9

		5.]									L. 999
N.	0	1	2	3	4	5	6	7	8	9	Diff.
990	995635	5679	5723	5767	5811	5854	-5898	5942	5986	6030	
1	6074	6117	6161	6205	6249	6293	6337	6380	6424	6468	44
3	6512	6555	6599	6643	6687	6731	6774	6818	6862	6906	
3	6949	6993	7037	7080	7124	7168	7212	7255	7299	7343	
4	7386	7430	7474	7517	7561	7605	7648	7692	7736	7779	
5	7823	7867	7910	7954	7998	8041	8085	8129	8172	8216	
6	8259	8303	8347	8390	8434	8477	8521	8564	8608	8652	1
7	8695	8739	8782	8826	8869	8913	8956	9000	9043	9087	
8	9131	9174	9218	9261	9305	9348	9392	9435	9479	9522	
9	9565	9609	9652	9696	9739	9783	9826	9870	9913	9957	4

LOGARITHMS OF NUMBERS FROM 1 TO 100.

N.	Log.	N.	Log.	N.	Log.	N.	Log.	N.	Log.
1	0.000000	21	1.322219	41	1.612784	61	1.785330	81	1.908485
2	0.301030	22	1.342423	42	1.623249	62	1.792392	82	1.913814
3	0.477121	23	1.361728	43	1.633468	63	1.799341	83	1.919078
4	0.602060	24	1.380211	44	1.643453	64	1.806180	84	1.924279
5	0.698970	25	1.397940	45	1.653213	65	1.812913	85	1.929419
6	0.778151	26	1.414973	46	1.662758	66	1.819544	86	1.934498
7	0.845098	27	1.431364	47	1.672098	67	1.826075	87	1.939519
8	0.903090	28	1.447158	48	1.681241	68	1.832509	88	1.944483
9	0.954243	29	1.462398	49	1.690196	69	1.838849	89	1.949390
10	1.000000	30	1.477121	50	1.698970	70	1.845098	90	1.954243
11	1.041393	31	1.491362	51	1.707570	71	1.851258	91	1.959041
12	1.079181	32	1.505150	52	1.716003	72	1.857332	92	1.963788
13	1.113943	33	1.518514	53	1.724276	73	1.863323	93	1.968483
14	1.146128	34	1.531479	54	1.732394	74	1.869232	94	1.973128
15	1.176091	35	1.544068	55	1.740363	75	1.875061	95	1.977724
16	1.204120	36	1.556303	56	1.748188	76	1.880814	96	1.982271
17	1.230449	37	1.568202	57	1.755875	77	1.886491	97	1.986772
18	1.255273	38	1.579784	58	1.763428	78	1.892095	98	1.991226
19	1.278754	39	1.591065	59	1.770852	79	1.897627	99	1.995635
20	1.301030	40	1.602060	60	1.778151	80	1.903090	100	2.000000

	Value at 0°.	Sign in 1st.	Value at 90°.	Sign in 2d Quad.	Value at 180°.	Sign in 3d	Value	Sign in 4th	Value
Sin	O O R O R & &	† + + + +	R & & R O O R	+ - + - +	O O R 2 R R & & &	Quad. + + + + + + + + + + + + + + + + + + +	270° R	Quad.	360°. O O R O R O R ∞ ∞

R signifies equal to rad; ∞ signifies infinite; O signifies evanescent.

0.		TAB	LE X	-LOGARI	THMIC S	INES	,		179°
	,	Sine.	q-l	Tang.	Cotang.	q+l	D 1"	Cosine.	,
0 60 120 180 240 300 360 420 480 540 600	0 1 2 3 4 5 6 7 8 9	Inf. neg. 6.463726 .764756 6.940847 7.065786 .162696 .241877 .308824 .36684 .417968 .463726	4.685 575 575 575 575 575 575 575 575 575 575 575 575 575 575 574 576 574 576 574 576	6.463726 .764756 6.940847 7.065786 .162696 .241878 3.08825 .366817 417970	Inf. pos. 13.536274 235244 13.059153 12.934214 .837304 .758122 .691175 .633183 .582030 .536273	15.314 425 425 425 425 425 425 425 425 424 424	.02 .00 .00 .00 .02	ten ten ten ten ten ten 9.999999 .999999 .999999 .999999	60 59 58 57 56 55 54 53 52 51
660 720 780 840 900 960 1020 1080 1140 1200	11 12 13 14 15 16 17 18 19 20	7.505118 .542906 .577668 .609853 .639816 .667845 .694173 .718997 .742478 .764754	574 577 574 577 574 577 574 577 573 577 573 577 573 577 573 577 573 577 573 577 573 577	7 .542909 7 .577672 7 .609857 8 .639820 8 .667849 8 .694179 0 .719003 0 .742484	12.494880 .457091 .422328 .390143 .360180 .332151 .305821 .280997 .257516 .235239	424 423 423 423 422 422 422 421 421 421 420	.00 .02 .00 .02 .00 .02 .00 .02 .00 .02	9.99998 .999997 .999996 .99996 .99995 .99994 .99993 .99993	49 48 47 46 45 44 43 42 41 40
1260 1320 1380 1440 1500 1560 1620 1680 1740 1800	21 22 23 24 25 26 27 28 29 30	7.785943 .806146 .825451 .843934 .861662 .878695 .895085 .910879 .926119 .940842	572 58 572 58 572 58 571 58 571 58 571 58 570 58 570 58 570 58 570 58	806155 825460 843944 8 861674 8 878708 4 895099 4 910894 5 926134	12.214049 .193845 .174540 .156056 .138326 .121292 .104901 .089106 .073866 .059142	420 419 419 418 417 417 416 416 415 414	.02 .02 .02 .00 .02 .02 .02 .02 .02 .03	9.999992 .999991 .999990 .99989 .99988 .99988 .99986 .99986 .99988	39 38 37 36 35 34 33 32 31 30
1860 1920 1980 2040 2100 2160 2220 2280 2340 2400	31 32 33 34 35 36 37 38 39 40	7.955082 .968870 .982233 7.995198 8.007787 .020021 .031919 .043501 .054781 .065776	569 58 569 58 568 58 568 58 567 59 566 59 566 59 565 59	7 .968889 .982253 7 .995219 0 8.007809 .020044 2 .031945 3 .043527 3 .054809	12.044900 .031111 .017747 12.004781 11.992191 .979956 .968055 .956473 .945191 .934194	413 413 412 411 410 409 408 407 407 406	.02 .02 .02 .03 .02 .02 .03 .02 .03	9.999982 .999981 .999980 .999979 .999976 .999975 .999973 .999972 .999971	29 28 27 26 25 24 23 22 21 20
2460 2520 2580 2640 2700 2760 2820 2880 2940 3000	41 42 43 44 45 46 47 48 49 50	8.076500 .086965 .097183 .107167 .116926 .126471 .135810 .144953 .153907 .162681	565 59 564 59 563 59 562 60 562 60 561 60 560 60 560 60	0.086997 0.097217 0.107203 0.116963 1.126510 0.135851 1.144996 1.153952	11. 923469 .913003 .902783 .892797 .883037 .873490 .864149 .855004 .846048 .837273	405 404 402 401 400 399 398 397 396 395	.03 .02 .03 .03 .02 .03 .03 .02 .03 .03	9.99969 .99968 .99966 .99964 .99963 .99959 .99959 .99958 .99956 .99954	19 18 17 16 15 14 13 12 11 10
3060 3120 3180 3240 3300 3360 3420 3480 3540 3600	51 52 53 54 55 56 57 58 59 60	8.171280 .179713 .187985 .196102 .204070 .211895 .219581 .227134 .234557 8.241855	559 600 558 600 557 611 556 613 555 614 554 616 553 619 4.685	3 .179763 .188036 .196156 .204126 .211953 .219641 .227195	11.828672 .820237 .811964 .803844 .795874 .788047 .780359 .772805 .765379 11.758079	393 392 391 389 388 387 385 384 382 381 15.314	.03 .03 .03 .03 .03 .03 .03 .03	9.99952 .99950 .99948 .99946 .99944 .99940 .99938 .99936 9.99934	9876543210
	<u> </u>	Cosine.	$\frac{1}{q-l}$	Cotang.	Tang.	$\left \frac{1}{q+l}\right $	D.1"	Sine.	-
	1	- Cosine.	1 4 - 1	Journey.	Tang.	14-11	D 1	bine.	1

1°		TAI	SLE .	Χ.–	-LOGARI	THMIC S	INES	,		178°
"	,	Sine.	q -	- 7	Tang.	Cotang.	q+l	D 1"	Cosine.	,
3600 3660 3720 3780 3840 3900 3960 4020 4080 4140 4200	C 1 2 3 4 5 6 7 8 9 10	8.241855 .249033 .256094 .263042 .269881 .276614 .283243 .289773 .296207 .302546 .308794	4.65 553 552 551 551 550 549 548 547 546 546 546	85 619 620 622 623 625 627 628 630 632 633 635	8.241921 .249102 .256165 .263115 .269956 .276691 .283323 .289856 .296292 .302634 .308884	11.758079 .750898 .743835 .730885 .730044 .723309 .716677 .710144 .703708 .697366 .691116	15.314 381 380 378 377 375 373 372 370 368 367 365	.03 .05 .03 .03 .05 .03 .05 .05 .03	9.999934 .999932 .999929 .999927 .999922 .999920 .999918 .999913 .999913	60 59 58 57 56 55 54 53 52 51 50
4260 4320 4380 4440 4500 4560 4620 4680 4740 4800	11 12 13 14 15 16 17 18 19 20	8.314954 .321027 .327016 .332924 .338753 .344504 .350181 .355783 .361315 .366777	544 543 542 541 540 539 539 538 537 536	637 638 640 642 644 646 648 649 651 653	8.315046 .321122 .327114 .333025 .338856 .344610 .350289 .355895 .361430 .366895	11.684954 .678878 .672886 .666975 .661144 .655390 .649711 .644105 .638570 .633105	363 362 360 358 356 354 352 351 349 347	.05 .03 .05 .05 .05 .05 .05 .05 .05	9.999907 .999905 .999902 .999699 .999897 .999894 .999888 .999885 .999882	49 48 47 46 45 44 43 42 41 40
4860 4920 4980 5040 5100 5160 5220 5280 5340 5400	21 22 23 24 25 26 27 28 29 30	8.372171 .377499 .382762 .387962 .393101 .398179 .403199 .408161 .413068 .417919	535 534 533 532 531 530 529 527 526 525	$\begin{array}{c} 655 \\ 657 \\ 659 \\ 661 \\ 663 \\ 666 \\ 670 \\ 672 \\ 674 \end{array}$	8.372292 .377622 .382889 .388092 .393234 .398315 .403338 .408304 .413213 .418068	11.627708 .622378 .617111 .611908 .606766 .601685 .596662 .591696 .586787 .581932	345 343 341 339 337 334 332 330 328 326	.05 .05 .05 .05 .05 .05 .05 .05 .07	9.999879 .999876 .999873 .999870 .999867 .999864 .999858 .999854 .999851	39 38 37 36 35 34 33 32 31 30
5460 5520 5580 5640 5700 5760 5820 5880 5940 6000	31 32 33 34 35 36 37 38 39 40	8.422717 .427462 .432156 .436800 .411394 .445941 .450440 .454893 .459301 .463665	524 523 522 521 520 518 517 516 515 514	676 679 681 683 685 688 690 693 695	8.422869 .427618 .432315 .436962 .441560 .446110 .450613 .455070 .459481 .463849	11.577181 .572382 .567685 .563088 .558440 .553890 .549887 .544930 .540519 .536151	324 321 319 317 315 312 310 307 305 303	.05 .07 .05 .05 .07 .05 .07 .05 .07	9.99848 .999844 .999841 .999838 .999834 .999827 .999824 .999820 .999816	29 28 27 26 25 24 23 22 21 20
6060 6120 6180 6240 6300 6360 6420 6480 6540 6600	41 42 43 44 45 46 47 48 49 50	8.467985 .472263 .476498 .480693 .484848 .488963 .493040 .497078 .501080 .505045	512 511 510 509 507 506 505 503 502 501	700 702 705 707 710 713 715 718 720 723	8.468172 .472454 .476693 .480892 .485050 .489170 .493250 .497293 .501298 .505267	11.531828 .527546 .523507 .519108 .514950 .510830 .506750 .502707 .498702 .494733	300 298 295 293 290 287 285 282 280 277	.05 .07 .07 .07 .05 .07 .07 .07	9.99813 .999809 .999805 .999801 .959797 .999794 .999786 .999782 .999778	19 18 17 16 15 14 13 12 11
6660 6720 6780 6840 6900 6960 7020 7080 7140 7200	51 52 53 54 55 56 57 58 59 60	8.508974 .512867 .516726 .520551 .524343 .528102 .531828 .535523 .539186 8.542819	499 498 497 495 494 492 491 490 488 487 4.68	726 729 731 734 737 740 743 745 745 751	8.509200 .513098 .516961 .520790 .524586 .528349 .532080 .535779 .539447 8.543084	11.490800 .486902 .483039 .479210 .475414 .471651 .467920 .464221 .460553 11.456916	274 271 269 266 263 260 257 255 252 249 15.314	.07 .08 .07 .07 .07 .07 .08 .07 .07	9.999774 .999769 .999765 .999767 .999757 .999748 .999744 .999740 9.999735	9 8 6 5 4 3 2 1 0
"	-,	Cosine.	- q -	ı	Cotang.	Tang.	$\frac{1}{q+l}$	D 1*	Sine.	,

' Sine, D. 1°. Cosine. D. 1°. Tang. D. 1°. Cotang. ' 0 8 542319 60.05 9.999735 .07 8.543094 60.12 11.456916 6 1 .546422 59.55 .999731 .9 .546691 60.12 433309 55 2 .54995 59.07 .999728 .08 .550268 59.65 149732 56 3 .553339 58.58 .999717 .07 .557336 58.20 .44464 56 5 .560340 58.10 .999713 .07 .560281 58.20 .449172 55 6 .563999 57.65 .999708 .08 .564291 57.72 .435709 56 6 .563999 57.65 .999704 .07 .567727 57.27 .43273 55 8 .570836 56.75 .999609 .08 .57117 56.83 428273 55 8<
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
11 8.580892 55.02 9.999685 .08 8.581208 55.10 11.418792 45.584193 54.60 .999680 .08 .584514 55.10 .415486 45.468
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
' Cosine, D. 1". Sine. D. 1". Cotang. D. 1". Tang. '

3°		TABL	E X.—L	OGARI	THMIC S	INES,		176°
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	8.718800 .721204 .723595 .725972 .728337 .730688 .733027 .735354 .737667 .739969 .742259	40.07 39.85 39.62 39.42 39.18 38.98 38.78 38.55 38.37 38.17 37.95	9.99404 .999398 .999391 .999384 .999378 .999364 .999350 .999350 .999343 .999336	.10 .12 .12 .10 .12 .12 .12 .12 .12 .12 .12 .12 .12	8.719396 .721806 .724204 .726588 .728959 .731317 .733663 .735996 .738317 .740626 .742922	40.17 39.97 39.73 39.52 39.30 39.10 38.88 38.68 38.48 38.27 38.08	11.280604 .278194 .275796 .273412 .271041 .268683 .266337 .264004 .261683 .259374 .257078	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	8.744536 .746802 .749055 .751297 .753528 .755747 .757955 .760151 .762337 .764511	37.77 37.55 37.37 37.18 36.98 36.80 36.60 36.43 36.23 36.07	9.999329 .999322 .999315 .999308 .999301 999294 .999287 .999279 .999272 .999265	.12 .12 .12 .12 .12 .12 .13 .13 .12 .12	8.745207 .747479 .749740 .751989 .754227 .756453 .758668 .760872 .763065 .765246	37.87 37.68 37.48 37.30 37.10 36.92 36.73 36.55 36.35 36.18	11.254793 .252521 .250260 .248011 .245773 .243547 .241332 .239128 .236935 .234754	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	8.766675 .768828 .770970 .773101 .775223 .777333 .779434 .781524 .783605 .785675	35.88 35.70 35.52 35.37 35.17 35.02 34.83 34.68 34.50 34.35	9.999257 .999250 .999242 .999235 .999227 .999220 .999212 .999205 .999197 .999189	.12 .13 .12 .13 .12 .13 .12 .13 .13 .13	8.767417 .769578 .771727 .773866 .775995 .778114 .780222 .782320 .784408 .786486	36.02 35.82 35.65 35.48 35.32 35.13 34.97 34.80 34.63 34.47	11.232583 .230422 .228273 .226134 .224005 .221886 .219778 .217680 .215592 .213514	39 38 371 36; 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	8.787736 .789787 .791828 .793859 .795881 .797894 .799897 .801892 .803876 .805852	34.18 34.02 33.85 33.70 33.55 33.38 33.25 33.07 32.93 32.78	9.999181 .999174 .999166 .999158 .999150 .999142 .999134 .999126 .999118 .999110	.12 .13 .13 .13 .13 .13 .13 .13 .13	8.788554 .790613 .792662 .794701 .796731 .798752 .800763 .802765 .804758 .806742	34.32 34.15 33.98 33.83 33.68 33.52 33.57 33.37 33.22 33.07 32.92	11.211446 .209387 .207338 .205299 .203269 .201248 .199237 .197235 .195242 .193258	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	8.807819 .809777 .811726 .813667 .815599 .817522 .819436 .821343 .823240 .825130	32.63 32.48 32.35 32.30 32.05 31.90 31.78 31.62 31.50 31.35	9.999102 .999094 .999086 .999077 .999069 .999053 .999044 .999036 .999027	.13 .13 .15 .13 .13 .13 .13 .15 .13	8.808717 .810683 .812641 .814589 .816529 .818461 .820384 .822298 .824205 .826103	32.57 32.63 32.47 32.33 32.20 32.05 31.90 31.78 31.63 31.48	11.191283 .189317 .187359 .185411 .183471 .181539 .179616 .177702 .175795 .173897	19 18 17 16 15 14 13 12 11
51 52 53 54 55 56 57 58 59 60	8.827011 .828884 .830749 .832607 .834456 .836297 .838130 .839956 .841774 8.843585	31.22 31.08 30.97 30.82 30.68 30.55 30.43 30.30 30.18	9.999019 .999010 .999002 .998993 .998984 .998976 .998967 .998958 .998950 9.998941	.15 .13 .15 .15 .15 .13 .15 .15 .15	8.827992 .829874 .831748 .833613 .835471 .837321 .839163 .840998 .842825 8.844644	31.37 31.23 31.08 30.97 30.83 30.70 30.58 30.45 30.32	11.172008 .170126 .168252 .166387 .164529 .162679 .160837 .159002 .157175 11.155356	9 8 7 6 5 4 3 2 1
,	Cosine.	D 1".	Sine.	D. 1".	Cotang.	D. 1*.	Tang.	-

4°			,	,				175
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 6 7 8 9	8.843585 .845387 .847183 .848971 .850751 .852525 .854291 .856049 .857801 .859546 .861283	30.03 29.93 29.80 29.67 29.57 29.43 29.30 29.20 29.08 28.95 28.85	9.998941 .998932 .998923 .998914 .998905 .998896 .998887 .998869 .998860 .998851	.15 .15 .15 .15 .15 .15 .15 .15 .15 .15	8.844644 .846455 .848260 .850057 .851846 .853628 .855403 .857171 .858932 .860686 .862433	30.18 30.08 29.95 29.82 29.70 29.58 29.47 29.35 29.23 29.12 29.00	11 155356 .153545 .151740 .149943 .148154 .146372 .144597 .142829 .141068 .139314 .137567	60 59 58 57 56 55 54 53 52 51
11 12 13 14 15 16 17 18 19 20	8.863014 .864738 .866455 .868165 .869868 .871565 .873255 .874938 .876615 .878285	28.73 28.62 28.50 28.38 28.28 28.17 28.05 27.95 27.83 27.73	9.998841 .998832 .998823 .998813 .998804 .998795 .998776 .998766 .998757	.15 .15 .17 .15 .15 .17 .15 .17 .15	8.864173 .865906 .867632 .869351 .871064 .872770 .874469 .876162 .877849 .879529	28.88 28.77 28.65 28.55 28.43 28.32 28.32 28.12 28.00 27.88	11.135827 .134094 .132368 .130649 .128936 .127230 .125331 .123838 .122151 .120471	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	8.879949 .881607 .883258 .884903 .886542 .888174 .889801 .891421 .893035 .894643	27.63 27.52 27.42 27.32 27.20 27.12 27.00 26.90 26.80 26.72	9.998747 .998738 .998728 .998718 .998708 .998699 .998699 .99869 .99869 .99869	.15 .17 .17 .17 .15 .17 .17 .17	8.881202 .882869 .884530 .886185 .887833 .889476 .891112 .892742 .894366 .895984	27.78 27.68 27.58 27.47 27.38 27.27 27.17 27.07 26.97 26.87	11.118798 .117131 .115470 .113815 .112167 .110524 .108888 .107258 .105634 .104016	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	8.896246 .897842 .899432 .901017 .902596 .904169 .905736 .907297 .908853 .910404	26.60 26.50 26.42 26.32 26.22 26.12 26.02 25.93 25.85 25.75	9.998649 .998639 .998629 .998619 .998509 .998589 .998589 .998588 .998588	.17 .17 .17 .17 .17 .17 .17 .18 .17 .17	8.897596 .899203 .900803 .902398 .903987 .905570 .907147 .908719 .910285 .911846	26.78 26.67 26.58 26.48 26.38 26.28 26.20 26.10 26.02 25.92	11.102404 .100797 .099197 .097602 .096013 .094430 .092853 .091281 .089715 .088154	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	8.911949 .913488 .915022 .916550 .918073 .919591 .921103 .922610 .924112 .925609	25.65 25.57 25.47 25.38 25.30 25.20 25.12 25.03 24.95 24.85	9,998548 .998537 .998527 .998516 .998506 .998495 .998474 .998464 .998453	.18 .17 .18 .17 .18 .17 .18 .17 .18	8.913401 .914951 .916495 .918034 .919568 .921096 .922619 .924136 .925649 .927156	25.83 25.73 25.63 25.57 25.47 25.38 25.28 25.28 25.12 25.12	11.086599 .085049 .083505 .081966 .080432 .078904 .077381 .075864 .074351 .072844	19 18 17 16 15 14 13 12 11
51 52 53 54 55 56 57 58 59 60	8.927100 .928587 .930068 .931544 .933015 .934481 .935942 .937398 .938850 8.940296	24.78 24.68 24.60 24.52 24.43 24.35 24.27 24.20 24.10	9.998442 .998431 .998421 .998410 .998399 .998388 .998377 .998366 .998355 9.998344	.18 .17 .18 .18 .18 .18 .18 .18	8.928658 .930155 .931647 .933134 .934616 .936093 .937565 .939032 .940494 8.941952	24.95 24.87 24.78 24.70 24.62 24.53 24.45 24.37 24.30	11.071342 .069845 .068353 .066866 .065384 .063907 .062435 .060968 .059506 11.058048	9 8 7 6 5 3 2 1 0
1	Cosine,	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	′
								0.5

,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1",	Cotang.	′
0 1 2 3 4 5 6 7 8 9 10	8.940296 .941738 .943174 .944606 .946034 .947456 .948874 .950287 .951696 .953100 .954499	24.03 23.93 23.87 23.80 23.70 23.63 23.55 23.48 23.40 23.32 23.25	9.998344 .998333 .998322 .998311 .998300 .998289 .998277 .998266 .998255 .998243	.18 .18 .18 .18 .18 .19 .20 .18 .19 .20 .18 .20	8.941952 .943404 .944852 .946295 .947734 .949168 .950597 .952021 .953441 .954856	24.20 24.13 24.05 23.98 23.90 23.82 23.73 23.67 23.58 23.52 23.45	11.058048 .056596 .055148 .053705 .052266 .050832 .049403 .047979 .046559 .045144 .043733	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	8.955894 .957284 .958670 .960052 .961429 .962801 .964170 .965534 .966893 .968249	23.17 23.10 23.03 22.95 22.87 22.82 22.73 22.65 22.60 22.52	9.998220 .998209 .998197 .998186 .998174 .998163 .998151 .998139 .998128	.18 .20 .18 .20 .18 .20 .20 .20 .18 .20 .20	8.957674 .959075 .960473 .961866 .963255 .964639 .966019 .967394 .968766	23.35 23.30 23.22 23.15 23.07 23.00 22.92 22.87 22.78 22.72	11.042326 .040925 .039527 .038134 .036745 .035361 .033981 .032606 .031234 .029867	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	8.969600 .970947 .972289 .973628 .974962 .976293 .977619 .978941 .980259 .981573	22.45 22.37 22.32 22.23 22.18 22.10 22.03 21.97 21.90 21.83	9.998104 .998092 .998080 .998068 .998056 .998044 .998032 .998020 .998008 .997996	.20 .20 .20 .20 .20 .20 .20 .20 .20 .20	8.971496 .972855 .974209 .975560 .976906 .978248 .979586 .980921 .982251 .983577	22.65 22.57 22.52 22.43 22.37 22.30 22.25 22.17 22.10 22.03	11.028504 .027145 .025791 .024440 .023094 .021752 .020414 .019079 .017749 .016423	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	8.982883 .984189 .985491 .986789 .988083 .989374 .990660 .991943 .993222 .994497	21.77 21.72 21.63 21.57 21.52 21.43 21.38 21.38 21.32 21.25 21.18	9.997984 .997972 .997959 .997947 .997935 .997922 .997910 .997897 .997885 .997872	.20 .22 .20 .20 .22 .20 .22 .20 .22 .20	8.984899 .986217 .987532 .988842 .990149 .991451 .992750 .994045 .995337 .996624	21.97 21.92 21.83 21.78 21.70 21.65 21.58 21.53 21.45 21.40	11.015101 .013783 .012468 .011158 .009851 .008549 .007250 .005935 .004663 .003376	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	8.995768 .997036 .998299 8.999560 9.000816 .002069 .003318 .004563 .005805 .007044	21.13 21.05 21.02 20.93 20.88 20.82 20.75 20.70 20.65 20.57	9.997860 .997847 .997835 .997829 .997890 .997797 .997784 .997771 .997758 .997745	.22 .20 .22 .22 .22 .20 .22 .22 .22	8.997908 8.999188 9.000465 .001738 .003007 .004272 .005534 .006792 .008047 .009298	21.33 21.28 21.22 21.15 21.08 21.03 20.97 20.92 20.85 20.80	11.002092 11.000812 10.999535 .998262 .99693 .995728 .994466 .993208 .991953 .990702	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.008278 .009510 .010737 .011962 .013182 .014400 .015613 .016824 .018031 9.019235	20 53 20 45 20 42 20 33 20 30 20 22 20 18 20 12 20 07	9.997732 .997719 .997706 .997693 .997687 .997687 .997644 .997628 9.997614	.22 .22 .22 .22 .22 .22 .22 .22 .22	9.010546 .011790 .013031 .014268 .015502 .016732 .017959 .019183 .020403 9.021620	20.73 20.68 20.62 20.57 20.50 20.45 20.40 20.33 20.28	10.989454 .988210 .986969 .985732 .984498 .983268 .982041 .980817 .979597 10.978380	9 8 7 6 5 4 3 2 1
,	Cosine.	D. 1'.	Sine.	D. 1'.	Cotang.	D. 1".	Tang.	/

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,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2	9.019235 .020435 .021632	20.00 19.95	9.997614 .997601 .997588	.22	9.021620 .022834	20.23 20.17	10.978380 .977166	60 59
3 4	.022825	19.88 19.85	.997574	.23	.024044 .025251 .026455	20.12 20.07	.975956	58
5	.025203	19.78 19.72	.997561 .997547	.23	.027655	20.00 19.95	.973545 .972345	56 55
6 7 8	.026386	19.68 19.62	.997534 .997520	.23	.028852	19.90 19.85	.971148 .969954	54 53
8	.028744	19.57	.997507 .997493	.23	.031237 .032425	19.80	.968763 .967575	52 51
10	.031089	19 52 19.47	.997480	.22	.033609	19.73 19.70	.966391	50
11 12	9.032257 .033421	19.40 19.35	9.997466 .997452	.23	9.034791 .035969	19.63	10.965209 .964031	49 48
13 14	.034582	19.32	.997439	.23	.037144	19.58 19.53	.962856 .961684	47
15	.036896	19.25 19.20	.997411	.23	.039485	19.48 19.43	.960515	45
16 17	.038048	19.15	.997397	.23	.040651	19.37	.959349 .958187	44 43
18 19	.040342	19.08 19.05	.997369 .997355	.23	.042973 .044130	19.33 19.28	.957027 .955870	42
20	.042625	19.00 18.95	.997341	.23	.045284	19.23 19.17	.954716	41 40
21 22	9.043762 .044895	18.88	9.997327 .997313	.23	9.046434 .047582	19.13	10.953566 .952418	39 38
23 24	.046026 .047154	18.85 18.80	.997299 .997285	.23 .23	.048727	19.08 19.03	.951273 .950131	37 36
25	.648279	18.75 18.68	.997271	.23	.051008	18.98 18.93	.948992	35
26 27	.049400	18.65	.997257 .997242	,25	.052144	18.88	.947856 .946723	34 33
28 29	.051635 .052749	18.60 18.57	.997228 .997214	.23	.054407 .055535	18 83 18.80	.945593 .944465	32
30	.053859	18.50 18.45	.997199	.25	.056659	18.73 18.70	.943341	31 30
31 32	9.054966	18.42	9.997185 .997170	.25	9.057781	18.65	10.942219 .941100	29 28
33 34	.057172 .058271	18.35 18.32	.997156	.23 .25	.060016 .061130	$18.60 \\ 18.57$.939984	27
35	.059367	18.27 18.22	.997141 .997127	.23	.062240	18.50 18.47	.938870 .937760	26 25
36 37	.060460	18.18	.997112 .997098	.23	.063348	18.42	.936652 .935547	24 23
38 39	.062639 .063724	18.13 18.08	.997083	.25 .25	.065556	18.38 18.32	.934444	22
40	.064806	18.03 17.98	.997068 .997053	.25	.066655 .067752	18.28 18.25	.933345 .932248	21 20
41 42	9.065885 .066962	17 05	9.997039 .997024	.25	9.068846 .069938	18.20	10.931154 .930062	19
43	.068036	17.90 17.85	.997009	.25	.071027	18.15 18.10	.928973	18 17
44 45	.069107 .070176	17.95 17.90 17.85 17.82 17.77 17.73 17.67	.996994	.25	.072113 .073197	18.07	.927887	16 15
46 47	.071242	17.73	.996964	.25 .25	.074278	18.02 17.97	.925722	14
48	.072306	17.67 17.63	.996949	.25 .25	.075356 .076432	17.93	.924644 .923568	13
49 50	.074424	17.60	.996919 .996904	.25	.077505 .078576	17.88 17.85	.922495 .921424	11 10
51	9.076533	17.55	9.996889	.25 .25	9.079644	17.80	10.920356	9
52 53	.077583	17.50 17.47	.996874	.27	.080710 .081773	17.77 17.72	.919290	8 7
54	.079676	17.49 17.38	. 996843	.25 .27	.082833	17.67 17.63	.918227 .917167	6
55 56	.080719	17.33	.996828	.27	.083891	17 60	.916109 .915053	5 4
57 58	.082797 .083832	17.30 17.25	.996797	.25 .25	.086000	17.55 17.50	.914000	3
59	.084864	17.20 17.17	.996782 .996766	.27 .25	.087050	17.55 17.50 17.47 17.43	.912950 .911902	2
60	9.085894		9.996751		9.089144		10.910856	0
,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	1 '
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7°		TABLE	X. 110	GAILL.	11.1110 01	11 110,		172°
,	Sine.	D. 1'.	Cosine.	D. 1'.	Tang.	D. 1'.	Cotang.	'
0 1 2 3 4 5 6 7 8 9	9 085894 .086922 .087947 .088970 .089990 .091008 .092024 .093037 .094047 .095056 .096062	17, 13 17, 08 17, 05 17, 00 16, 97 16, 93 16, 88 16, 83 16, 82 16, 77 16, 72	9.996751 .996735 .996720 .996704 .996688 .996673 .996641 .996625 .996610 .996594	27 .25 .27 .27 .27 .27 .27 .27 .27	9.089144 .090187 .091228 .092266 .093302 .094336 .095367 .096395 .097422 .098446 .099468	17.38 17.35 17.30 17.27 17.23 17.18 17.13 17.12 17.07 17.03 16.98	10.910856 .909813 .908772 .907734 .906698 .905664 .904633 .903605 .902578 .901554 .900532	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.097065 .098066 .099065 .100062 .101056 .102048 .103037 .104025 .105010 .105992	16.68 16.65 16.62 16.57 16.53 16.48 16.47 16.42 16.37 16.35	9.996578 .996562 .996546 .996530 .996514 .996498 .996482 .996465 .996449 .996433	.27 .27 .27 .27 .27 .27 .27 .28 .27	9.100487 .101504 .102519 .103532 .104542 .105550 .106556 .107559 .108560 .109559	16.95 16.92 16.88 16.83 16.80 16.77 16.72 16.68 16.65 16.65	10.899513 .898496 .897481 .896468 .895458 .894450 .893444 .892441 .891440 .890441	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.106973 .107951 .108927 .109901 .110873 .111842 .112809 .113774 .114737 .115698	16.30 16.27 16.23 16.20 16.15 16.12 16.08 16.05 16.02 15.97	9.996417 .996400 .996384 .996368 .996351 .996318 .996302 .996285 .996269	.28 .27 .27 .28 .27 .28 .27 .28 .27 .28	9.110556 .111551 .112548 .113538 .114521 .115507 .116491 .117472 .118452 .119429	16.58 16.53 16.50 16.47 16.43 16.40 16.35 16.33 16.28 16.25	10.889444 .888449 .887457 .886467 .885479 .884493 .883509 .882528 .851548 .880571	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9 116656 .117613 118567 .119519 .120469 .121417 .122362 .123306 .124248 .125187	15.95 15.90 15.87 15.83 15.80 15.75 15.73 15.70 15.65 15.63	9.996252 .996235 .996219 .996202 .996185 .996186 .996151 .996134 .996117	.28 .27 .28 .28 .28 .28 .28 .28 .28	9.120404 .121377 .122348 .123317 .124284 .125249 .126211 .127172 .128130 .129087	16.22 16.18 16.15 16.12 16.08 16.03 16.03 16.02 15.97 15.95 15.90	10.879596 .878623 .877652 .876683 .875716 .874751 .873789 .872828 .871870 .870913	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9 126125 .127060 .127993 .128925 .129854 130781 .131706 .132630 .133551 .134470	15 58 15 55 15 53 15 48 15 45 15 42 15 40 15 35 15 32 15 28	9.996083 .996066 .996049 .996032 .996032 .995998 .995980 .995963 .995946 .995928	.28 .28 .28 .28 .28 .30 .28 .28 .30 .28	9.130041 .130994 .131944 .132893 .138339 .134784 .135726 .136667 .137605 .138542	15.88 15.83 15.82 15.77 15.75 15.70 15.68 15.63 15.62 15.57	10.869959 .869006 .868056 .867107 .866161 .865216 .864274 .863333 .862395 .861458	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9 135387 .136303 .137216 .138128 .139037 .139944 .140850 .141754 .142655 .143555	15.27 15.22 15.20 15.15 15.12 15.10 15.07 15.02	995911 .995894 .995876 .995859 .995841 .995823 .995806 .995788 .995771 9.995753	.28 .30 .28 .30 .30 .28 .30 .28 .30	9 139476 .140409 .141340 .142269 .143196 .144121 .145044 .145966 .146885 9.147803	15.55 15.52 15.48 15.45 15.42 15.38 15.37 15.32 15.30	10 860524 .859591 .858660 .857731 .856804 .855879 .854956 .854034 .853115 10 .852197	9 8 7 6 5 4 3 2 1 0
,	Cosine.	D. 1'.	Sine.	D. 1'.	Cotang.	D. 1".	Tang.	,

8°			-,					171°
,	Sine.	D. 1".	Cosine.	D. 1'.	Tang.	D. 1".	Cotang.	1
0 1 2 3 4 5 6 7 8 9	9.143555 .144453 .145349 .146243 .147136 .148026 .148015 .149802 .150686 .151569 .152451	14.97 14.93 14.90 14.88 14.83 14.82 14.78 14.73 14.72 14.70 14.65	9.995753 .995735 .995717 .995699 .99564 .995646 .995628 .995610 .995573	.30 .30 .30 .30 .30 .28 .30 .30 .30 .30	9.147803 .148718 .149632 .150544 .151454 .152363 .153269 .154174 .155077 .155978 .156877	15.25 15.23 15.20 15.17 15.15 15.10 15.08 15.05 15.02 14.98 14.97	10.852197 .851282 .850368 .849456 .848546 .847637 .846731 .845826 .844923 .844022 .843123	60 59 58 57 56 55 54 53 52 51
11 12 13 14 15 16 17 18 19 20	9.153330 .154208 .155083 .155957 .156830 .157700 .158569 .159435 .160301 .161164	14.63 14.58 14.57 14.55 14.50 14.48 14.43 14.43 14.38 14.35	9.995555 .995537 .995519 .995501 .995402 .995464 .995446 .995427 .995409 .995390	.30 .30 .30 .32 .30 .30 .32 .30 .32 .30	9.157775 .158671 .159565 .160457 .161347 .162236 .168123 .164008 .164892 .165774	14.93 14.90 14.87 14.83 14.82 14.78 14.75 14.73 14.70 14.67	10.842225 .841329 .840435 .839543 .83863 .837764 .836877 .835992 .835108 .834226	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.162025 .162885 .163743 .164600 .165454 .166307 .167159 .168008 .168856 .169702	14.33 14.30 14.28 14.23 14.22 14.20 14.15 14.13 14.10 14.08	9.995372 .995353 .995334 .995316 .995297 .995278 .995260 .995241 .995222 .995203	.32 .30 .32 .32 .30 .32 .30 .32 .32 .32 .32	9.166654 .167532 .168409 .169284 .170157 .171029 .171899 .172767 .173634 .174499	14.63 14.62 14.58 14.55 14.53 14.50 14.47 14.45 14.42 14.38	10.833346 .832468 .831591 .830716 .829843 .828971 .828101 .827233 .826366 .825501	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.170547 .171389 .172230 .173070 .173908 .174744 .175578 .176411 .177242 .178072	14.03 14.02 14.00 13.97 13.93 13.90 13.88 13.85 13.83 13.80	9.995184 .995165 .995146 .995127 .995108 .995089 .995070 .995051 .995032 .995013	.92 .93 .93 .93 .93 .93 .93 .93 .93 .93 .93	9.175362 .176224 .177084 .177942 .178799 .179655 .180508 .181360 .182211 .183059	14.37 14.33 14.30 14.28 14.27 14.22 14.20 14.18 14.13	10.824638 .823776 .822916 .822058 .821201 .820345 .819492 .818640 .817789 .816941	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.178900 .179726 .180551 .181374 .182196 .183016 .183834 .184651 .185466 .186280	13.77 13.75 13.72 13.70 13.67 13.63 13.62 13.58 13.57 13.53	9.994993 .994974 .994955 .994935 .994916 .994896 .994877 .994857 .994838 .994818		9.183907 .184752 .185597 .186439 .187280 .188120 .188958 .189794 .190629 .191462	14.08 14.08 14.03 14.02 14.00 13.97 13.93 13.92 13.88 13.87	10.816093 .815248 .814403 .813561 .812720 .811880 .811042 .810206 .809371 .808538	19 18 17 16 15 14 13 12 11
51 52 53 54 55 56 57 58 59 60	9.187092 .187903 .188712 .189519 .190325 .191130 .191933 .192734 .193534 9.194332	13.52 13.48 13.45 13.43 13.42 13.38 13.35 13.33 13.30	9.994798 .994779 .994759 .994739 .994720 .994700 .994680 .994660 .994640 9.994620	.33 .33 .33 .32 .33 .33 .33 .33	9.192294 .193124 .193953 .194780 .195606 .196430 .197253 .198074 .198894 9.199713	13.83 13.82 13.78 13.77 13.73 13.72 13.68 13.67 13.65	10.807706 .806876 .806047 .805220 .804394 .803570 .802747 .801926 .801106 10.800287	9 8 7 6 5 4 3 2 1 0
	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	•

								1.70
,	Sine.	D. 1*.	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.194332 .195129 .195925 .196719 .197511 .198302 .199091 .199879 .200666 .201451 .202234	13.28 13.27 13.23 13.20 13.18 13.15 13.13 13.12 13.08 13.05 13.05	9.994620 .994600 .994580 .994560 .994540 .994519 .994479 .994479 .994459 .994438	.89	9.199713 .200529 .201345 .202159 .203971 .203782 .204592 .204592 .205400 .206207 .207013 .207817	13.60 13.60 13.57 13.53 13.52 13.50 13.47 13.45 13.43 13.40 13.37	10.800287 .799471 .798655 .797841 .797029 .796218 .793408 .794600 .793793 .792987 .792183	60 59 58 57 56 55 54 53 52 51 50
11 12 18 14 15 16 17 18 19 20	9.203017 .203797 .204577 .205354 .206131 .206906 .207679 .208452 .209222 .209992	13.00 13.00 12.95 12.95 12.92 12.88 12.88 12.83 12.83 12.80	9.994398 .994377 .994357 .994366 .994316 .994295 .994274 .994254 .994233 .994212	.35 .35 .35 .35 .35 .35 .35 .35 .35	9.208619 .209420 .210220 .211018 .211815 .212611 .213405 .214198 .214989 .215780	13.35 13.33 13.30 13.28 13.27 13.23 13.23 13.18 13.18 13.18	10.791381 .790580 .789780 .788982 .788185 .787389 .786595 .785802 .785011 .784220	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.210760 .211526 .212291 .213055 .213818 .214579 .215338 .216097 .216854 .217609	12.77 12.75 12.73 12.72 12.68 12.65 12.65 12.62 12.58 12.57	9.994191 .994171 .994150 .994129 .994108 .994087 .994066 .994045 .994024 .994003	.83 .85 .85 .85 .85 .85 .85 .85 .85	9.216568 .217356 .218142 .218926 .219710 .220492 .221272 .222052 .222830 .223607	13.13 13.10 13.07 13.07 13.03 13.00 13.00 12.97 12.95 12.92	10.783432 .782644 .781858 .781074 .780290 .779508 .778728 .777748 .777770 .776393	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.218363 .219116 .219868 .220618 .221367 .222115 .222861 .223606 .224349 .225092	12.55 12.53 12.50 12.48 12.47 12.43 12.43 12.38 12.38 12.38	9.993982 .993960 .993939 .993918 .993857 .993875 .993854 .993832 .993811 .993789	.37 .35 .35 .35 .35 .37 .35 .37 .35	9.224382 .225156 .225929 .226700 .227471 .228239 .229007 .229773 .230539 .231302	12.90 12.88 12.85 12.85 12.80 12.77 12.77 12.77 12.72 12.72	10.775618 .774844 .774071 .773300 .772529 .771761 .770993 .770227 .769461 .768698	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.225833 .226573 .227311 .228048 .228784 .229518 .230252 .230984 .231715 .232444	12.33 12.30 12.28 12.27 12.23 12.23 12.23 12.20 12.18 12.15 12.13	9.993768 .993746 .993725 .993703 .993681 .993660 .993638 .993616 .993594 .993572	.57 .55 .57 .57 .55 .57 .57 .57	9.232065 .232826 .233586 .234345 .235103 .235859 .236614 .237368 .238120 .238872	12.68 12.67 12.65 12.63 12.50 12.58 12.57 12.53 12.53 12.50	10.767935 .767174 .766414 .765655 .764897 .764141 .763386 .762632 .761880 .761128	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.233172 .233899 .234625 .235349 .236073 .236795 .237515 .238235 .238953 9.239670	12.12 12.10 12.07 12.07 12.03 12.00 12.00 11.97 11.95	9.993550 .993528 .993506 .993464 .993462 .993418 .993396 .993374 9.993351	.37 .37 .37 .37 .37 .37 .37 .37 .37	9.239622 .240371 .241118 .241865 .242610 .243354 .244097 .244839 .245579 9.246319	12.48 12.45 12.45 12.40 12.38 12.37 12.33 12.33	10.760378 .759629 .758882 .758135 .757390 .756646 .755903 .755161 .754421 10.753681	9 8 7 6 5 4 3 2 1
	Cosine.	D. 1'.	Sine.	D. 1".	Cotang.	D. 1".	Tang.	,

10°	COSINES, TANGENTS, AND COTANGENTS.									
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,		
0	9.239670	11.00	9,993351		9,246319	40.00	10.753681	60		
1	. 240386	11.93 11.92	.993329	.37	.247057	12.30 12.28	.752943	59		
2 3	.241101	11.92	.993307	.38	.247794	12.28	752206	58		
3	.241814	11.87	.993284	.37	.248530	12.23	.751470	57		
4 5 6 7 8	.242526 .243237	11.85	.993262	.37	.249264	12.23	.750736 .750002	56 55		
6	.243947	11.83	.993240	.38	.250730	12.20	.749270	54		
7	.244656	11.82	.993195	.37	.251461	12.18	.748539	53		
8	. 245363	11.78	.993172	.38	.252191	12.17	.747809	52		
9	.246069	11.77	.993149	.38	.252920	12.15 12.13	.747809 .747080	51		
10	.246775	11.78 11.77 11.77 11.77	.993127	.38	.253648	12.10	.746352	50		
11	9.247478	11.72	9.993104	.38	9.254374	12.10	10.745626	49		
12	.248181	11.70	.993081	.37	.255100	12.07	.744900	48		
13	.248883	11.67	.993059	.38	.255824	12.05	.744176	47		
14	.249583	11.65	. 993036	.38	.256547	12.03	.743453 .742731	46 45		
16	.250980	11.63	.992990	.38	.257269	12.02	.742010	44		
17	.251677	11.62	.992967	.38	.258710	12.00	.741290	43		
18	.252373	11.60 11.57	.992944	.38 .38	.259429	11.98 11.95	.740571	42		
19	.253067	11.57	.992921	.38	. 260146	11.95	.739854	41		
20	.253761	11.53	. 992898	.38	.260863	11.92	.739137	40		
21	9.254453	11.52	9.992875	.38	9.261578	11.90	10.738422	39		
22	.255144	11.50	.992852	.38	.262292	11.88	.737708	38		
23	.255834	11.48	.992829	.38	.263005	11.87	.736995 .736283	37		
24 25	.256523 .257211	11.47	.992806 .992783	.38	.263717	11.85	.735572	36 35		
26	.257898	11.45	.992759	.40	.265138	11.83	.734862	34		
27	.258583	11.42	.992736	.38	.265847	11.82	.734153	33		
28	. 259268	11.42	. 992713	.38	.266555	11.80	.733445	32		
29	.259951	11.30	.992690	.38	.267261	11.77	.732739	31		
30	.260633	11.38 11.37 11.35	.992666	.38	.267967	11.80 11.77 11.77 11.73	.732033	30		
81	9.261314		9.992643	.40	9.268671	11 72	10.731329	29		
32	.261994	11.33 11.32	.992619	.38	.269375	11.73 11.70 11.70	.730625	28		
33	.262673	11.30	.992596	.40	.270077	11.70	.729923	27 26		
34 35	.263351	11.27	.992572 .992549	.38	.270779 .271479	11.67	.729221 .728521	25		
36	.264703	11.27	.992525	.40	.272178	11.65	.727822	24		
37	.265377	11.23 11.23	.992501	.40	.272876	11.63	.727124	23		
38	.266051	11.20	.992478	.40	.273573	11.62 11.60	.726427	22		
39	.266723	11.20	.992454	.40	.274269	11.58	.725731	21		
40	.267395	11.17	.992430	.40	.274964	11.57	.725036	20		
41	9.268065	11.15	9.992406	.40	9.275658	11.55	10.724342	19		
42	.268734	11.13	.992382	.38	.276351	11.53	.723649 .722957	18 17		
43	.269402 .270069	11.12	.992359	.40	.277043 .277734	11.52	.722957	16		
45	.270735	11.10	.9923311	.40	.278424	11.50	.721576	15		
46	.271400	11.08	.992287	.40	.279113	11.48 11.47	.720887	14		
47	.272064	11.07 11.03	.992263	.40	.279801	11.47	.720199	13		
48	.272726	11.03	.992239	.42	.280488	11.43	.719512	12		
49 50	.273388 .274049	11.02	.992214 .992190	.40	.281174	11.40	.718826 .718142	11 10		
	1	10.98		.40		11.40				
51	9.274708	10.98	9.992166	.40	9.282542	11.38	10.717458	9 8 7 6 5 4 3 2		
52 53	.275367 .276025	10.97	.992142 .992118	.40	.283225	11.37 11.35 11.33 11.32	.716775 .716093	7		
54	.276681	10.93	.992118	.42	.284588	11.35	.715412	6		
55	.277337	10.93	.992069	.40	.285268	11.33	.714732	5		
56	.277991	10.90	.992044	.42	.285947	11.32	.714053	4		
57	.278645	10.87	.992020	.40	.286624	11.28	.713376	3		
58	.279297	10.93 10.93 10.90 10.87 10.85	.991996	.42	.287301	11.28 11.28 11.27 11.25	712099	1		
60	9.280599	10.85	9.991947	.40	9.288652	11.25	.712699 .712023 10.711348	0		
1-					l			_		
/	Cosine.	D. 1'.	Sine.	D. 1".	Cotang.	D. 1'.	Tang.	/		
-										

11°	TABLE X.—LUGARITHMIC SINES,									
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1*.	Cotang.	/		
0 1	9.280599 .281248	10.82	9.991947	.42	9.288652 .289326	11.23	10.711348 .710674	60 59		
2	.281897	10.82 10.78	.991897	.42	.289999	11.22 11.20	.710001	58		
2 3 4 5 6 7	.282544	10.77	.991873	.42	.290671	11.18	.709329	57		
5	.283836	10.77	.991823	.42	.292013	11.18	.708658	56 55		
6	.284480	10.73 10.73	.991799	.40 .42	.292682	11.15 11.13	.707318	54		
7	.285124	10.70	.991774	.42	.293350	11.13	.706650	53		
8 9	.285766 .286408	10.70	.991749 .991724	.42	.294017 .294684	11.12	.705983 .705316	52 51		
10	.287048	10.67 10.67	.991699	.42	.295349	11.08 11.07	.704651	50		
11	9.287688		9.991674	1	9,296013		10.703987	49		
12	.288326	10.63 10.63	.991649	.42	.296677	11.07	.703323	48		
13	.288964	10.60	.991624	.42	.297339	11.03 11.03	.702661	47		
14 15	.289600	10.60	.991599	.42	.298001 .298662	11.02	.701999 .701338	46 45		
16	.290870	10.57 10.57	.991549	.42	,299322	11.00 10.97	.700678	44		
17	.291504	10.55	.991524	.43	.299980	10.97	.700020	43		
18	.292137	10.52	.991498 .991473	.42	.300638 .301295	10.95	.699362 .698705	42 41		
20	.293399	10.52	.991448	.42	.301951	10.93	.698049	40		
21	9.294029	10.50	9.991422		9.302607	10.93	10,697393	39		
22 23	.294658	10.48 10.47	.991397	.42	.303261	10.90 10.88	.696739	38		
23	.295286	10.45	.991372	.43	.303914	10.88	.696086	37		
25	.295913	10.43	.991346 .991321	.42	.304567 .305218	10.85	.695433 .694782	36 35		
26	.297164	10.42	.991295	.43	.305869	10.85 10.83 10.82	.694131	34		
27	.297788	10.40 10.40 10.37 10.35	.991270	.43	.306519	10.83	,693481	33		
28 29	.298412 .299034	10.37	.991244 .991218	.43	.307168 .307816	10.80	.692832 .692184	32 31		
30	.299655	10.35	.991193	.42	.308463	10.78	.691537	30		
31	9.300276	10.35	9.991167	.43	9.309109	10.77	10.690891	29		
32	.300895	10.32 10.32	.991141	.43	.309754	10.75 10.75	.690246	28		
33	.301514	10.30	.991115	.42	.310399	10.73	.689601	27		
35	.302132	10.27	.991090	.43	.311042 .311685	10.72	.688958 .688315	26 25		
36	.303364	10.27 10.25	.991038	.43	.312327	10.70 10.68	.687673	24		
37 38	.303979	10.23	.991012	.43	.312968	10.65	.687032	23		
39	.304593	10.23	.990986	.43	.313608 .314247	10.65	.686392 .685753	22 21		
40	.305819	10.20 10.18	.990934	.43	.314885	10.63	.685115	20		
41	9.306430	4	9.990908	.43	9.315523	10.63	10.684477	19		
42	.307041	10.18	.990882	.43 .45	.316159	10.60 10.60	.683841	18		
43	.307650 .308259	10.15 10.15 10.13	.990855	.43	.316795	10.58	.683205	17		
44 45	.308259	10.13	.990829	.43	.317430 .318064	10.57	.682570 .681936	16 15		
46	.309474	10.12 10.10	.990777	.43 .45	.318697	10.55 10.55	.681303	14		
47	.310080	10.08	.990750	,43	319330	10.55	.680670	13		
48 49	.310685 .311289	10.07	.990724	.45	.319961	10.52	.680039 .679408	12 11		
50	.311893	10.07 10.03	.990671	.43	.321222	10.50	.678778	10		
51	9.312495	10.03	9.990645	.43	9.321851	10.48	10.678149	9		
52	.313097	10.03	.990618	.45 .45	.322479	10.47 10.45	.677521	8		
53 54	.313698 .314297	9.98	.990591 .990565	.43	.323106	10.45	.676894	7		
55	.314897	10.00	.990538	.45	.324358	10.42	.676267 .675642	5		
56	.315495	9.97	.990511	.45	.324983	10.42 10.40	.675017	4		
57 58	.316092 .316689	9.95	.990485	.45	.325607	10.40	.6:4393	3		
59	.317284	9.92	.990438	.45	.326231	10.37	.673769 .673147	8 7 6 5 4 3 2		
60	.317284 9.317879	9.92	9.990404	.45	9.327475	10.37	10.672525	ō		
-	Cosine	D. 1".	Sino	D 1"	Cotone	D 11				
I	' Cosine. D. 1". Sine. D. 1". Cotang. D. 1". Tang. '									

12° 167								
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.317879 .318473 .319066 .319058 .320249 .320840 .321430 .322019 .322607 .323194 .323780	9.90 9.88 9.87 9.85 9.85 9.83 9.82 9.78 9.77	9.990404 .990378 .990351 .990324 .990297 .990243 .990215 .990188 .990161 .990134	.43 .45 .45 .45 .45 .45 .47 .45 .45 .45	9.327475 328095 328715 329334 329953 330570 331187 331803 332418 333033 333646	10.33 10.33 10.32 10.32 10.28 10.28 10.27 10.25 10.25 10.22 10.22	10.672525 .671905 .671985 .670666 .670047 .669430 .668813 .668197 .667582 .666967	60 59 58 57 56 55 54 53 52 51
11 12 13 14 15 16 17 18 19 20	9.324366 .324950 .325534 .326117 .326700 .327281 .327862 .328442 .329021 .329599	9.73 9.73 9.72 9.72 9.68 9.68 9.67 9.65 9.63 9.62	9.990107 .990079 .990052 .990025 .989997 .989970 .989942 .989915 .989887 .989860	.47 .45 .45 .47 .45 .47 .45 .47 .45	9.334259 .834871 .335482 .336093 .336702 .337311 .337919 .338527 .339133 .339739	10.20 10.18 10.18 10.15 10.15 10.13 10.10 10.10 10.08	10.665741 .665129 .664518 .663907 .663298 .662689 .662081 .661473 .660867 .660261	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.330176 .330753 .331329 .331903 .332478 .333051 .333624 .334195 .334767 .335337	9.62 9.60 9.57 9.58 9.55 9.55 9.52 9.53 9.50 9.48	9.989832 .989804 .989777 .989749 .989721 .989693 .989665 .989637 .989610 .989582	.47 .45 .47 .47 .47 .47 .47 .45 .47	9.340344 .340948 .341552 .342155 .342757 .343558 .343558 .344558 .345157 .345755	10.07 10.07 10.05 10.03 10.02 10.00 10.00 9.98 9.97 9.97	10.659656 .659052 .658448 .657845 .657243 .656642 .655442 .654843 .654245	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.335906 .336475 .337043 .337610 .338176 .338742 .339307 .339871 .340434 .340996	9.48 9.47 9.45 9.43 9.43 9.42 9.40 9.38 9.37 9.37	9.989553 .989525 .989497 .989469 .989441 .989413 .989356 .989356 .989328 .989300	.47 .47 .47 .47 .47 .47 .48 .47 .48	9.346353 .346949 .347545 .348141 .348735 .349329 .349922 .350514 .351106 .351697	9.93 9.93 9.99 9.90 9.88 9.87 9.87 9.85 9.83	10.653647 .653051 .652455 .651859 .651265 .650671 .650078 .649486 .648894 .648303	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.341558 .342119 .342679 .343239 .343797 .344355 .344912 .345469 .346024 .346579	9.35 9.33 9.33 9.30 9.30 9.28 9.28 9.25 9.25	9.989271 .989243 .989214 .989186 .989157 .989128 .989100 .989071 .989042 .989014	.47 .48 .47 .48 .48 .47 .48 .48 .47 .48	9.352287 .352876 .353465 .354053 .354640 .355227 .355813 .356398 .356982 .357566	9.82 9.82 9.80 9.78 9.77 9.77 9.73 9.73 9.72	10.647713 .647124 .646535 .645947 .645360 .644773 .644187 .643602 .643018 .642434	19 18 17 16 15 14 13 12 11
51 52 53 54 55 56 57 58 59 60	9.347134 .347687 .348240 .348792 .349343 .349893 .350443 .350992 .351540 9.352088	9.22 9.22 9.20 9.18 9.17 9.17 9.15 9.13 9.13	9.988985 .988956 .988927 .988898 .988869 .988840 .988811 .988782 .988753 9.988724	.48 .48 .48 .48 .48 .48 .48 .48	9.358149 .358731 .359313 .359893 .360474 .361053 .361632 .362210 .362787 9.363364	9.70 9.70 9.67 9.68 9.65 9.65 9.63 9.62 9.62	10.641851 .641269 .640687 .640107 .639526 .638947 .638368 .637790 .637213 10.636636	9 8 7 6 5 4 3 2 1
,	Cosine.	D. 1°.	Sine,	D. 1".	Cotang.	D. 1".	Tang.	7.

13°		IADL	E X.—1.	OUALL.	IIIMIC S	114 1509		166*
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1*.	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.352088 .352635 .353181 .353726 .354271 .354815 .355358 .355901 .356443 .356984 .357524	9.12 9.10 9.08 9.08 9.07 9.05 9.05 9.03 9.02 9.00	9.988724 .988695 .988666 .988636 .988607 .988578 .988548 .988519 .988489 .988460 .988430	.48 .48 .50 .48 .48 .50 .48 .50 .48	9.363364 .363940 .364515 .365090 .365664 .366237 .366810 .367382 .367953 .368524 .369094	9.60 9.58 9.58 9.57 9.55 9.55 9.53 9.52 9.52 9.50 9.48	10.636636 .636060 .635485 .634910 .634336 .633763 .633190 .632618 .632047 .631476 .630906	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.358064 .358603 .359141 .359678 .360215 .360752 .361287 .361822 .362356 .362889	8.98 8.97 8.95 8.95 8.95 8.92 8.92 8.92 8.88	9.988401 .988371 .988342 .988312 .988282 .988252 .988223 .988193 .988163 .988133	.50 .48 .50 .50 .50 .48 .50 .50	9.369663 .370232 .370799 .371367 .371933 .372499 .373064 .373629 .374193 .374756	9.48 9.45 9.47 9.43 9.43 9.42 9.42 9.40 9.38 9.38	10.630337 .629768 .629201 .628633 .628067 .627501 .626936 .626371 .625807 .625244	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.363422 .363954 .364485 .365016 .365546 .366075 .366604 .367131 .367659 .368185	8.87 8.85 8.85 8.83 8.82 8.82 8.78 8.80 8.77	9.988103 .988073 .988043 .988013 .987983 .987953 .987922 .987892 .987862 .987832	.50 .50 .50 .50 .50 .52 .50 .50 .50	9.375319 .375881 .376442 .377003 .377563 .378122 .378681 .379239 .379797 .380354	9.37 9.35 9.35 9.33 9.32 9.30 9.30 9.28 9.27	10.624681 .624119 .628558 .622997 .622437 .621878 .621319 .620761 .620203 .619646	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.368711 .369236 .369761 .370285 .370808 .371330 .371852 .372373 .372894 .373414	8.75 8.75 8.75 8.72 8.72 8.70 8.68 8.68 8.68	9.987801 .987771 .987740 .987710 .987679 .987649 .987618 .987588 .987557	.50 .50 .50 .50 .50 .50 .50 .50 .52 .50	9,380910 .381466 .382020 .382575 .383129 .383682 .384234 .384786 .385337 .385888	9.27 9.23 9.25 9.23 9.22 9.20 9.18 9.18 9.17	10.619090 .618534 .617980 .617425 .616871 .616318 .615766 .615214 .614663 .614112	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.373933 .374452 .374970 .375487 .376003 .376519 .377035 .377549 .378063 .378577	8.65 8.63 8.62 8.60 8.60 8.57 8.57 8.57 8.53	9.987496 .987465 .987434 .987403 .987379 .987341 .987310 .987279 .987248 .987217	.50 .52 .52 .52 .52 .52 .52 .52 .52	9.386438 .386987 .387536 .388084 .388631 .389178 .389724 .390270 .390815 .391360	9.15 9.15 9.13 9.12 9.10 9.10 9.08 9.08 9.05	10.613562 .613013 .612464 .611916 .611369 .610822 .610276 .609730 .609185 .608640	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9·379089 .379601 .380113 .380624 .381134 .381643 .382152 .382661 .383168 9.383675	8.53 8.53 8.52 8.50 8.48 8.48 8.48 8.45	9.987186 .987155 .987124 .987092 .987061 .987030 .986998 .986967 .986936 9.986904	.52 .52 .53 .52 .52 .52 .53 .52 .53	9.391903 .392447 .392989 .393531 .394613 .395154 .395694 .396233 9.396771	9.07 9.03 9.03 9.03 9.02 9.00 9.00 8.98 8.97	10.608097 .607553 .607011 .606469 .605927 .605386 .604846 .604306 .603767	9 8 7 6 5 4 3 2 1
,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	1

1	4°	COSINES, TANGENTS, AND COTANGENTS. 165										
	,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1'.	Cotang.	1			
	0 1 2 3 4 5 6 7 8 9 10	9.383675 .384182 .384687 .385192 .385697 .386201 .386704 .387207 .387207 .388210 .388711	8.45 8.42 8.42 8.42 8.42 8.40 8.38 8.38 8.37 8.35 8.35 8.33	9.986904 .986873 .986841 .986809 .986746 .986746 .986683 .986619 .986519	.52 .53 .53 .52 .53 .53 .52 .53 .53	9.396771 397309 397846 398383 398919 399455 399990 400524 401058 401591 402124	8.97 8.95 8.95 8.93 8.93 8.92 8.90 8.88 8.88 8.88	10.603229 .602691 .602154 .601617 .601081 .600545 .600010 .599476 .598942 .598409	60 59 58 57 56 55 54 53 52 51 50			
	11 12 13 14 15 16 17 18 19 20	9.389211 .389711 .390210 .390708 .391206 .391703 .392199 .392695 .393191 .393685	8.33 8.32 8.30 8.30 8.25 8.27 8.27 8.27 8.27 8.23 8.23	9.986555 .986523 .986491 .986459 .986427 .986395 .986363 .986331 .986299 .986266	.53 .53 .53 .53 .53 .53 .53 .53 .55 .55	9.402656 .403187 .403718 .404249 .404778 .405308 .405836 .406364 .406892 .407419	8.85 8.85 8.85 8.83 8.83 8.80 8.80 8.80 8.78	10.597344 .596813 .596282 .595751 .595222 .59462 .594164 .593636 .593108 .592581	49 48 47 46 45 44 43 42 41 40			
	21 22 23 24 25 26 27 28 29 30	9.394179 .394673 .395166 .395658 .396150 .396641 .397132 .397621 .398111 .398600	8.23 8.22 8.20 8.20 8.18 8.18 8.15 8.17 8.15 8.13	9.986234 .986202 .986169 .986137 .986104 .986072 .986039 .986007 .985974 .985942	.53 .55 .53 .55 .55 .55 .55 .55 .55	9.407945 .408471 .408996 6.409521 .410045 .410569 .411092 .411615 .412137 .412658	8.77 8.75 8.75 8.73 8.73 8.73 8.70 8.68 8.68	10.592055 .591529 .591004 .590479 .589955 .589431 .588908 .588385 .587863 .587342	39 38 37 36 35 34 33 32 31 30			
	31 32 33 34 35 36 37 38 39 40	9.399088 .399575 .400062 .400549 .401035 .401520 .402005 .402489 .402972 .403455	8.12 8.12 8.12 8.10 8.08 8.08 8.07 8.05 8.05 8.05	9.985909 .985876 .985843 .985811 .985778 .9857745 .985712 .985679 .985646 .985613	.55 .55 .53 .55 .55 .55 .55 .55 .55	9.418179 .413699 .414219 .414738 .415257 .415775 .416293 .416810 .417326 .417842	8.67 8.65 8.65 8.63 8.63 8.62 8.60 8.60	10.586821 .586301 .585781 .585262 .584743 .584225 .583707 .583190 .582674 .582158	29 28 27 26 25 24 23 22 21 20			
4	41 42 43 44 45 46 47 48 49 50	9.403938 .404420 .404901 .405382 .405862 .406341 .406820 .407777 .408254	8.03 8.02 8.02 8.00 7.98 7.98 7.98 7.97 7.95	9.985580 .985547 .985514 .985480 .985447 .985414 .985381 .985347 .985314 .985280	.55 .55 .57 .55 .55 .55 .57 .55 .57	9.418358 .418873 .419387 .419901 .420415 .420927 .421440 .421952 .422463 .422974	8.58 8.57 8.57 8.57 8.55 8.55 8.55 8.52 8.52 8.50	10.581642 .581127 .580613 .580099 .579585 .579073 .578560 .578048 .577537 .577026	19 18 17 16 15 14 13 12 11			
55555	51 52 53 54 55 56 57 58 59 50	9.408731 .409207 .409682 .410157 .410632 .411106 .411579 .412052 .412524 9.412996	7.93 7.93 7.92 7.92 7.92 7.88 7.88 7.88	9.985247 .985213 .985180 .985146 .985113 .985079 .985045 .985011 .984978 9.984944	.57 .55 .57 .55 .57 .57 .57 .57	9.423484 .423993 .424503 .425011 .425519 .426027 .426534 .427041 .427547 9.428052	8.48 8.50 8.47 8.47 8.47 8.45 8.45 8.43 8.42	10.576516 .576007 .575497 .574989 .574481 .573973 .573466 .572959 .572453 10.571948	9 8 7 6 5 4 3 2 1 0			
	/ 55	Cosine.	D. 1*.	Sine.	D. 1'.	Cotang.	D. 1'.	Tang.	′			

15°	1 ABIN X.—LOUARITH MIO STAND, 1									
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,		
0 1 2 3 4 5 6 7 8 9	9.412996 .413467 .413938 .414408 .414878 .415347 .415815 .416283 .416751 .417217 .417684	7.85 7.85 7.83 7.83 7.82 7.80 7.80 7.77	9, 984944 .984910 .984876 .984842 .984842 .984774 .984740 .984706 .984672 .984638 .984603	.57 .57 .57 .57 .57 .57 .57 .57 .57	9.428052 .428558 .429062 .429566 .430070 .430573 .431075 .431577 .432079 .432580 .433080	8.43 8.40 8.40 8.40 8.38 8.37 8.37 8.37 8.35 8.33 8.33	10.571948 .571442 .570938 .570434 .569930 .569427 .568925 .568423 .567921 .567420 .566920	60 59 58 57 56 55 54 53 52 51 50		
11 12 13 14 15 16 17 18 19 20	9.418150 .418615 .419079 .419544 .420007 .420470 .420933 .421395 .421857 .422318	7.75 7.73 7.75 7.72 7.72 7.72 7.70 7.70 7.68 7.67	9.984569 .984535 .984500 .984466 .984432 .984397 .984363 .984328 .984294 .984259	.57 .58 .57 .57 .58 .57 .58 .57 .58	9.433580 .434080 .434579 .435078 .435576 .436073 .436570 .437067 .437563 .438059	8.33 8.32 8.32 8.30 8.28 8.28 8.28 8.27 8.27 8.27	10.566420 .565920 .565421 .564922 .564424 .563927 .563430 .562933 .562437 .561941	49 48 47 46 45 44 43 42 41 40		
21 22 23 24 25 26 27 28 29 30	9.422778 .423238 .423697 .424156 .425073 .425530 .425987 .426443 .426899	7.67 7.65 7.65 7.65 7.63 7.62 7.62 7.60 7.60 7.58	9.984224 .984190 .984155 .984120 .984085 .984050 .984015 .983981 .983946 .983911	.57 .58 .58 .58 .58 .58 .57 .58 .58 .58	9.438554 .439048 .439543 .440036 .440529 .441022 .441514 .442006 .442497 .442988	8.23 8.25 8.22 8.22 8.22 8.20 8.20 8.18 8.18 8.18	10.561446 .560952 .560457 .559964 .559471 .558978 .558486 .557994 .557503 .557012	39 38 37 36 35 34 33 32 31 30		
31 32 33 34 35 36 37 38 39 40	9.427354 .427809 .428263 .428717 .429170 .429623 .430075 .430527 .430978 .431429	7.58 7.57 7.57 7.55 7.55 7.53 7.53 7.52 7.52 7.52	9.983875 .983840 .983805 .983770 .983735 .983700 .983664 .983629 .983594 .983558	.58 .58 .58 .58 .58 .60 .58 .60 .58	9.443479 .443968 .444458 .444947 .445435 .445923 .446411 .446898 .447384 .447870	8.15 8.17 8.15 8.13 8.13 8.13 8.10 8.10 8.10	10,556521 .556032 .555542 .555053 .554565 .554077 .558589 .553102 .552616 .552130	29 28 27 26 25 24 23 22 21 20		
41 42 43 44 45 46 47 48 49 50	9.431879 .432329 .432778 .433226 .433675 .434122 .434569 .435016 .435462 .435908	7.50 7.48 7.47 7.48 7.45 7.45 7.45 7.43 7.43 7.42	9.983523 .983487 .983452 .983416 .983381 .983345 .983209 .983273 .983238 .983202	.60 .58 .60 .58 .60 .60 .58 .60	9.448356 .448841 .449326 .449810 .450294 .450777 .451260 .451743 .452225 .452706	8.08 8.08 8.07 8.07 8.05 8.05 8.05 8.03 8.02 8.02	10.551644 .551159 .550674 .550190 .549706 .549293 .548740 .548257 .547775 .547294	19 18 17 16 15 14 13 12 11 10		
51 52 53 54 55 56 57 58 59 60	9.436353 .436798 .437242 .437686 .438129 .438572 .439014 .439456 .439897 9.440338	7.42 7.40 7.40 7.38 7.38 7.37 7.37 7.35 7.35	9.983166 .983130 .983094 .983058 .983022 .982986 .982950 .982914 .982878 9.982842	.60 .60 .60 .60 .60 .60 .60	9.453187 .453668 .454148 .454628 .455107 .455586 .456064 .456542 .457019 9.457496	8.02 8.00 8.00 7.98 7.98 7.97 7.97 7.95 7.95	10.546813 .546332 .545852 .545872 .544893 .544414 .543936 .543458 .542981 10.542504	9 8 7 6 5 4 3 2 1 0		
,	Cosine. D. 1'. Sine. D. 1'. Cotang. D. 1'. Tang.									

10								163
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.440338 .440778 .441218 .441658 .442096 .442535 .442973 .443410 .443847 .444284 .444720	7.33 7.33 7.33 7.30 7.30 7.32 7.38 7.28 7.28 7.28 7.25	9.982842 .982805 .982769 .982733 .982696 .982624 .982587 .982511 .982477	.62 .60 .60 .62 .60 .62 .60 .62 .62 .62	9.457496 .457973 .458449 .458925 .459400 .459875 .460349 .460823 .461297 .461770 .462242	7.95 7.93 7.93 7.92 7.92 7.90 7.90 7.88 7.87 7.88	10.542504 .542027 .541251 .541075 .540605 .540125 .539651 .539177 .538703 .538230 .537758	60 59 58 57 56 55 54 53 52 51
11 12 13 14 15 16 17 18 19 20	9.445155 .445590 .446025 .446459 .446893 .447326 .447759 .448191 .448623 .449054	7.25 7.25 7.23 7.22 7.22 7.22 7.20 7.20 7.18 7.18	9.982441 .982404 .982367 .982331 .982294 .982257 .982220 .982183 .982146 .982109	.62 .62 .60 .62 .62 .62 .62 .62 .62	9.462715 .463186 .463658 .464128 .464599 .465539 .46508 .466008 .466477 .466945	7.85 7.87 7.83 7.85 7.83 7.83 7.82 7.82 7.80 7.80	10.537285 .536814 .536342 .535872 .535401 .534931 .534461 .533992 .533523 .533055	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.449485 .449915 .450345 .450775 .451204 .451632 .452060 .452488 .452915 .453342	7.17 7.17 7.17 7.15 7.13 7.13 7.13 7.12 7.12 7.12	9.982072 .982035 .981998 .981961 .981924 .981886 .981849 .981812 .981774 .981737	.62 .62 .62 .63 .62 .63 .62 .63	9.467413 .467880 .468347 .468814 .469280 .469746 .470211 .470676 .471141 .471605	7.78 7.78 7.78 7.77 7.77 7.75 7.75 7.75	10.532587 .532120 .531653 .531186 .530720 .530254 .529789 .529324 .52859 .528395	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.453768 .454194 .454619 .455044 .455893 .456316 .456739 .457162 .457584	7.10 7.08 7.08 7.08 7.07 7.05 7.05 7.05 7.05 7.03 7.03	9.981700 .981662 .981625 .981587 .981549 .981512 .981474 .981436 .981399 .981361	.63 .62 .63 .63 .62 .63 .62 .63 .62	9.472069 .472532 .472995 .473457 .473919 .474381 .474842 .475303 .475763 .476223	7.72 7.72 7.70 7.70 7.70 7.68 7.68 7.67 7.67	10.527931 527468 .527005 .526543 .526081 .525619 .525158 .524697 .524237 .523777	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.458006 .458427 .45848 .459268 .459688 .460108 .460527 .460946 .461364 .461782	7.02 7.02 7.00 7.00 7.00 6.98 6.98 6.97 6.97 6.95	9.981323 .981285 .981247 .981209 .981171 .981133 .981095 .981057 .981019 .980981	.63 .63 .63 .63 .63 .63 .63 .63	9.476683 .477142 .477601 .478059 .478517 .478975 .479432 .479889 .480345 .480801	7.65 7.65 7.63 7.63 7.62 7.62 7.60 7.60	10.523317 .522858 .522399 .521941 .521483 .521025 .520568 .520111 .519655 .519199	19 18 17 16 15 14 13 12 11
51 52 53 54 55 56 57 58 59 60	9.462199 .462616 .463032 .463448 .463864 .464279 .464694 .465108 .465522 9.465935	6.95 6.93 6.93 6.93 6.92 6.92 6.90 6.90 6.88	9.980942 .980904 .980866 .980827 .980789 .980750 .980712 .980673 .980635 9.980596	.63 .63 .65 .65 .65 .63 .65 .63	9.481257 .481712 .482167 .482621 .483075 .483529 .483982 .484435 .484887 9.485339	7.58 7.58 7.57 7.57 7.57 7.55 7.55 7.55	10.518743 .518288 .517833 .517379 .516925 .516471 .516018 .515565 .515113 10.514661	9 8 6 5 4 3 2 1
,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	′

17°	TABLE X.—LOGARITHMIO SINES,								
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,	
0 1 2 3 4 5 6 7 8 9	9.465935 .466348 .466761 .467173 .467585 .467996 .468407 .468817 .469227 .469637 .470046	6.88 6.88 6.87 6.87 6.85 6.83 6.83 6.83	9.980596 .980558 .980519 .980480 .980442 .980403 .980364 .980325 .980286 .980247 .980208	.63 .65 .65 .63 .65 .65 .65	9.485339 .485791 .486242 .486693 .487143 .487593 .488043 .488492 .488941 .489390 .489388	7.53 7.52 7.52 7.50 7.50 7.50 7.48 7.48 7.48	10.514661 .514209 .513758 .513307 .512857 .512407 .511508 .511059 .510610 .510162	60 59 58 57 56 55 54 53 52 51 50	
11 12 13 14 15 16 17 18 19 20	9.470455 .470863 .471271 .471679 .472086 .472492 .472898 .473304 .473710 .474115	6.82 6.80 6.80 6.80 6.77 6.77 6.77 6.77 6.77 6.75 6.73	9.980169 .980130 .980091 .980052 .980012 .979973 .979934 .979895 .979855 .979816	.65 .65 .65 .67 .65 .65 .65 .67	9.490286 .490733 .491180 .491627 .492073 .492519 .492965 .493410 .493854 .494299	7.47 7.45 7.45 7.45 7.43 7.43 7.43 7.42 7.40 7.42 7.40	10.509714 .509267 .508820 .508373 .507927 .507481 .507035 .506590 .506146 .505701	49 48 47 46 45 44 43 42 41 40	
21 22 23 24 25 26 27 28 29 30	9.474519 .474923 .475327 .475730 .476133 .476536 .476938 .477340 .477741 .478142	6.73 6.73 6.72 6.72 6.72 6.70 6.68 6.68 6.68	9.979776 .979737 .979697 .979658 .979618 .979579 .979539 .979499 .979459 .979420	.65 .67 .65 .67 .65 .67 .67 .67 .65	9.494743 .495186 .495630 .496073 .496515 .496957 .497399 .497841 .498282 .498722	7.38 7.40 7.38 7.37 7.37 7.37 7.37 7.35 7.35 7.35	10.505257 .504814 .504370 .503927 .503485 .503643 .502601 .502159 .501718 .501278	39 38 37 36 35 34 33 32 31 30	
31 32 33 34 35 36 37 38 39 40	9.478542 .478942 .479342 .479741 .480140 .480539 .480937 .481334 .481731 .482128	6.67 6.67 6.65 6.65 6.65 6.63 6.62 6.62 6.62	9.979380 .979340 .979300 .979260 .979220 .979180 .979140 .979059 .979019	.67 .67 .67 .67 .67 .67 .67 .68 .67	9.499163 .499603 .500042 .500481 .500920 .501359 .501797 .502235 .502672 .503109	7.33 7.32 7.32 7.32 7.32 7.30 7.30 7.28 7.28 7.28	10.500837 .500397 .499958 .499519 .499080 .498641 .498203 .497765 .497328 .496891	29 28 27 26 25 24 23 22 21 20	
41 42 43 44 45 46 47 48 49 50	9.482525 .482921 .483316 .483712 .484107 .484501 .484595 .485289 .485682 .486075	6.60 6.58 6.60 6.58 6.57 6.57 6.57 6.55 6.55 6.55	9.978979 .978939 .978898 .978858 .978817 .978777 .978737 .978696 .978655 .978615	.67 .68 .67 .68 .67 .67 .68 .68 .67	9.503546 .503982 .504418 .504854 .505289 .505724 .506159 .506593 .507027 .507460	7.27 7.27 7.27 7.25 7.25 7.25 7.23 7.23 7.23 7.22	10.496454 .496018 .495582 .495146 .494711 .494276 .493841 .498407 .492973 .492540	19 18 17 16 15 14 13 12 11	
51 52 53 54 55 56 57 58 59 60	9.486467 486860 .487251 .487643 .488034 .488424 .488814 .489204 .489593 9.489982	6.55 6.52 6.53 6.52 6.50 6.50 6.50 6.48 6.48	9.978574 .978533 .978493 .978452 .978451 .978370 978329 .978288 .978247 9.978206	.68 .67 .68 .68 .68 .68 .68	9.507898 .508326 .508759 .509191 .509622 .510054 .510485 .510916 .511346 9.511776	7.29 7.29 7.20 7.18 7.20 7.18 7.18 7.17 7.17	10.492107 .491674 .491241 .490809 .490378 .489946 .489515 .489084 .488654 10.488224	9 8 7 6 5 4 3 2 1	
,	Cosine.	D 1.	Sine.	D. 1".	Cotang.	D. 1*.	Tang.	,	
107.									

107*

18°								161°
′	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1",	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.489982 .490371 .490759 .491147 .491535 .491922 .492308 .492695 .493081 .493466 .493851	6.48 6.47 6.47 6.47 6.45 6.43 6.43 6.42 6.42	9.978206 .978165 .978124 .978083 .978042 .978001 .977959 .977918 .977877 .977835	.68 .68 .68 .68 .70 .68 .70	9.511776 .512206 .512635 .513064 .513493 .513921 .514349 .514777 .515204 .515631 .516057	7.17 7.15 7.15 7.15 7.13 7.13 7.12 7.12 7.10	10.488224 .487794 .487365 .486936 .486507 .486079 .485651 .485233 .484796 .484369 .483943	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.494236 494621 495005 495388 495772 496154 496537 496919 497301 497682	6.42 6.42 6.40 6.38 6.40 6.37 6.38 6.37 6.35 6.35	9.977752 9.977711 .977669 .977628 .977586 .977544 .977503 .977419 .977377	.70 .68 .70 .68 .70 .70 .68 .70 .70 .70	9.516484 .516910 .517335 .517761 .518186 .518610 .519034 .519458 .519882 .520305	7.12 7.10 7.08 7.10 7.08 7.07 7.07 7.07 7.07 7.05 7.05	10.483516 .483090 .488665 .482239 .481814 .481390 .480966 .480966 .480542 .480118 .479695	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.498064 .498444 .498825 .499204 .499584 .499963 .500342 .500721 .501099 .501476	6.33 6.35 6.32 6.33 6.32 6.32 6.30 6.28 6.30	9.977335 .977293 .977251 .977267 .977167 .977125 .977083 .977041 .976999 .976957	.70 .70 .70 .70 .70 .70 .70 .70 .70	9.520728 .521151 .521573 .521995 .522417 .522838 .523259 .523680 .524100 .524520	7.05 7.03 7.03 7.03 7.02 7.02 7.02 7.00 7.00 7.00	10.479272 .478849 .478427 .478005 .477583 .477162 .476741 .476320 .475900 .475480	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.501854 .502231 .502607 .502984 .503360 .503735 .504110 .504485 .504860 .505234	6.28 6.27 6.28 6.27 6.25 6.25 6.25 6.25 6.23 6.23	9.976914 .976872 .976830 .976787 .976745 .976702 .976660 .976617 .976574 .976532	.70 .70 .72 .70 .72 .70 .72 .72 .70 .72	9.524940 .525359 .525778 .526197 .526615 .527033 .527451 .527868 .528285 .528702	6.98 6.98 6.98 6.97 6.97 6.97 6.95 6.95 6.95	10.475060 .474641 .474222 .473803 .473385 .472967 .472549 .472132 .471715 .471298	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.505608 .505981 .506354 .506727 .507471 .507843 .508214 .508585 .508956	6.22 6.22 6.22 6.20 6.20 6.20 6.18 6.18 6.18	9.976489 .976446 .976404 .976361 .976318 .976275 .976232 .976189 .976146 .976103	72 70 72 72 72 72 72 72 72 72 72	9.529119 .529535 .529951 .530366 .530781 .531196 .531611 .532025 .532439 .532853	6.93 6.93 6.92 6.92 6.92 6.90 6.90 6.90 6.88	10.470881 .470465 .470049 .469634 .469219 .468804 .468389 .467975 .467561 .467147	19 18 17 16 15 14 13 12 11
51 52 53 54 55 56 57 58 59 60	9.509326 .509696 .510065 .510434 .510803 .511172 .511540 .511907 .512275 9.512642	6.17 6.15 6.15 6.15 6.15 6.13 6.12 6.13 6.12	9.976060 .976017 .975974 .975930 .975887 .975844 .975800 .975757 .975714 9.975670	72 72 73 72 72 72 72 73 72 72 73	9.533266 .533679 .534092 .534504 .534916 .535328 .535739 .536150 .536561 9.536972	6.88 6.88 6.87 6.87 6.87 6.85 6.85 6.85	10.466734 .466321 .465908 .465496 .465084 .464672 .464261 .463850 .463439 10.463028	9 8 7 6 5 4 3 2 1 0
,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1'.	Tang.	1

,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.512642 .513009 .513375 .513741 .514107 .514472 .514837 .515202 .515566 .515930 .516294	6.12 6.10 6.10 6.10 6.08 6.08 6.08 6.07 6.07	9.975670 .975627 .975583 .975589 .975496 .975452 .975408 .975365 .975321 .975277 .975233		9.536972 .537382 .537792 .538202 .538611 .539020 .539429 .539827 .540245 .540653 .541061	6.83 6.83 6.83 6.82 6.82 6.82 6.80 6.80 6.80 6.78	10.463028 .462618 .462208 .461798 .461389 .460980 .460571 .460163 .459755 .459347 .458989	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.516657 .517020 .517382 .517745 .518107 .518468 .518829 .519190 .519551 .519911	6.05 6.03 6.05 6.03 6.02 6.02 6.02 6.02 6.00 6.00	9.975189 .975145 .975101 .975057 .975013 .974969 .974925 .974880 .974836 .974792	n national	9.541468 .541875 .542281 .542688 .543094 .543499 .543905 .544310 .544715 .545119	6.78 6.77 6.78 6.77 6.75 6.75 6.75 6.75	10,458532 .458125 .457719 .457312 .456906 .456501 .456995 .455690 .455285 .454881	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.520271 .520631 .520990 .521349 .521707 .522066 .522424 .522781 .523138 .523495	6.00 5.98 5.98 5.97 5.98 5.97 5.95 5.95 5.95	9.974748 .974703 .974659 .974614 .974570 .974525 .974481 .974436 .974391 .974347		9.545524 .545928 .546331 .546735 .547138 .547540 .547943 .548345 .548747 .549149	6.73 6.72 6.73 6.72 6.70 6.70 6.70 6.70 6.70 6.68	10.454476 .454072 .453669 .453265 .452862 .452460 .452057 .451655 .451253 .450851	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.523852 .524208 .524564 .524920 .525275 .525630 .525984 .526339 .526693 .527046	5.93 5.93 5.93 5.92 5.92 5.92 5.90 5.92 5.90 5.88	9.974302 .974257 .974212 .974167 .974122 .974077 .974032 .973987 .973987	.75 .75 .75 .75 .75 .75 .75 .75	9.549550 .549951 .550352 .550752 .551153 .551552 .552951 .552750 .553149	6.68 6.68 6.67 6.68 6.65 6.65 6.65 6.65 6.65	10.450450 .450049 .449648 .449248 .448847 .44848 .448048 .447649 .447250 .446851	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.527400 .527753 .528105 .528458 .529161 .529161 .529513 .529864 .530215 .530565	5.88 5.88 5.87 5.88 5.87 5.85 5.85 5.83 5.83	9.973852 .973807 .973761 .973716 .973625 .973580 .973580 .973489 .973444	75.77.57.77.67.77.67.77.67.77.77.77.77.77.77.77	9.553548 .553946 .554344 .554741 .555139 .55*593 .555933 .556329 .556725 .557121	6.63 6.63 6.62 6.63 6.62 6.62 6.60 6.60 6.60 6.60	10.446452 .446054 .445656 .445259 .444861 .444464 .444067 .443671 .443275 .442879	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.530915 .531265 .531614 .531963 .532312 .532661 .533009 .533357 .533704 9.534052	5.83 5.82 5.82 5.82 5.82 5.82 5.80 5.80 5.78 5.80	9.973398 .973352 .973307 .973261 .973215 .973169 .973124 .973078 .973032 9.972986	.77 .75 .77 .77 .77 .77 .77	9.557517 .557913 .558308 .558703 .559097 .559491 .559885 .560279 .560673 9.561066	6.60 6.58 6.58 6.57 6.57 6.57 6.57 6.57	10.442463 .442087 .441692 .441297 .440903 .440509 .440115 .439721 .439327 10.438934	9 8 7 6 5 4 3 2 1 0
1	Cosine.	D. 1",	Sine.	D. 1".	Cotang.	D. 1".	Tang.	1
100								70

109.

20°								159
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	1
0 1 2 3 4 5 6 7 8 9	9.534052 534399 534745 535092 535438 535783 536129 536474 536818 537163 537507	5.78 5.77 5.75 5.77 5.75 5.75 5.73 5.73	9.972986 .972940 .972894 .972848 .972802 .972755 .972709 .972663 .972677 .972570 .972524	77 77 77 78 77 77 77 78 77 77	9 561066 .561459 561851 562244 .562636 .563028 .563419 .564202 .564593 .564983	6 55 6 53 6 55 6 53 6 53 6 52 6 53 6 52 6 52 6 50 6 50	10.438934 .438541 .438149 .437756 .437364 .436972 .436581 .436189 .435798 .435407 .435017	60 59 58 57 56 55 54 58 52 51 50
11 12 13 14 15 16 17 18 19 20	9.537851 538194 .538538 53880 .539223 539565 .539907 .540249 .540590 .540931	5.72 5.73 5.70 5.72 5.70 5.70 5.68 5.68 5.68 5.68	9.972478 972481 972385 972338 .972291 .972245 .972198 .972151 .972105 .972058	.78 .78 .78 .78 .78 .78 .78 .78	9.565873 565763 .566153 566542 .566932 .567320 .567709 .568098 .568486 .568873	6.50 6.50 6.48 6.50 6.47 6.48 6.47 6.45 6.47	10.434627 .434237 .433847 .433458 .433688 .432680 .43291 .431902 .431514 .431127	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.541272 .541613 .541953 .54293 .542632 .542971 .543310 .543649 .543987 .544325	5.68 5.67 5.67 5.65 5.65 5.65 5.63 5.63 5.63	9.972011 .971964 .971917 .971870 .971823 .971776 .971729 .971682 .971635 .971588	.78 .78 .78 .78 .78 .78 .78 .78 .78	9.569261 .569648 .570035 .570422 .570802 .571195 .571181 .571967 .572352 .572738	6.45 6.45 6.45 6.45 6.43 6.43 6.42 6.43 6.42	10.430739 .430352 .429965 .429578 .429191 .428805 .428419 .42803 .427648 .427262	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.544663 .545000 .545338 .545674 .546011 .546347 .546683 .547019 .547354 .547689	5.62 5.63 5.60 5.62 5.60 5.60 5.58 5.58 5.58	9.971540 .971493 .971446 .971398 .971351 .971303 .971256 .971208 .971161 .971113	.78 .78 .80 .78 .80 .78 .80 .78 .80	9.573123 .573507 .573892 .574276 .574660 .575044 .575427 .575810 .576193 .576576	6.40 6.42 6.40 6.40 6.38 6.38 6.38 6.38 6.38	10.426877 .426493 .426108 .425724 .425340 .424956 .424573 .424190 .423807 .423424	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.548024 .548359 .548693 .549027 .549360 .549693 .550026 .550359 .550692 .551024	5.58 5.57 5.57 5.55 5.55 5.55 5.55 5.55	9.971066 .971018 .970970 .970922 .970874 .970827 .970779 .970731 .970683 970635	.80 .80 .80 .80 .78 .80 .80 .80	9.576959 .577341 .577723 .578104 .578486 .578867 .579248 579629 .580009 580389	6.37 6.37 6.35 6.35 6.35 6.35 6.35 6.33 6.33 6.33	10.423041 .422659 .422277 .421896 .421514 .421133 .420752 .420371 .419991 .419611	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.551356 .551687 .552018 .552349 .55268 .553010 .553841 .553670 .554000 9.554329	5.52 5.52 5.52 5.52 5.50 5.52 5.48 5.50 5.48	9.970586 970538 970490 .970442 .970394 .970394 .970297 .970249 .970200 9.970152	.80 .80 .80 .80 .82 .80 .82 .80	9.580769 .581149 581528 581907 .58286 .582665 .583044 .583422 .583800 9.584177	6.33 6.32 6.32 6.32 6.32 6.32 6.32 6.30 6.30 6.28	10.419231 .418851 .418472 .418093 .417714 .417335 .416956 .416578 .416200 10.415823	9 8 7 6 5 4 3 2 1
	Cosine,	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	

110° 69°

21•		TABL	E	OGARII	IIIMIO B	IN ES,		158°
1	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1*.	Cotang.	,
0	9.554329	5.48	9.970152	.82	9.584177	6.30	10.415823	60
1 9	.554658 .554987	5.48	.970103 .970055	.80	.584555 .584932	6.28	.415445	59 58
2 3	.555315	5.47 5.47	.970006	.82 .82	.585309	$\frac{6.28}{6.28}$.414691	57
4	.555643	5.47	.969957	.80	.585686 .586062	6.27	.414314	56 55
4 5 6 7 8	.555971	5.47	.969909	.82	.586439	6.28	.413561	54
7	.556626	5.45 5.45	.969811	.82	.586815	$6.27 \\ 6.25$.413185	53
8 9	.556953	5.45	.969762 .969714	.80	.587190 .587566	6.27	.412810 .412434	52 51
10	.557606	5.43 5.43	.969665	.82	.587941	$6.25 \\ 6.25$.412059	50
11	9.557932		9.969616	.82	9,588316	6.25	10.411684	49
12	.558258	5.43 5.42	.969567	.82	.588691	6.25	.411309	48
13	.558583	5.43	.969518	.82	.589066	6.23	.410934 .410560	47 46
15	.559234	5.42 5.40	.969420	.82	.589814	6.23 6.23	.410186	45
16	.559558	5.42	.969370	.82	.590188	6.23	.409812	44 43
17	.559883	5.40	.969321	.82	.590562	6.22	.409438	42
19	.560531	5.40 5.40	.969223	.82	.591308	6.22 6.22	.408692	41
20	. 560855	5.38	.969173	.82	.591681	6.22	.408319	40
21	9.561178	5.38	9.969124	.82	9.592054	6.20	10.407946	29
22 23	.561501 .561824	5.38	.969075 .969025	.83	.592426	6.22	.407574	38 37
24	.562146	5.37 5.37	.968976	.82	.593171	6.20 6.18	.406829	36
25	.562468	5.37	.968926	.82	.593542	6.20	.406458	35 34
26 27	.562790 .563112	5.37	.968877	.83	.593914	6.18	.406086 .405715	33
28	. 563433	5.35 5.37	.968777 .968728	.83 .82	.594656	6.18	.405344	32
29 30	.563755 .56407 5	5.33	.968728	.83	.595027	6.18	.404973 .404602	31
1	9.564396	5.35	9.968628	.83	9.595768	6.17	10.404232	29
31 32	.564716	5.33	.968578	.83	.596138	6.17	.403862	28
33	.565036	5.33 5.33	.968528	.83 .82	. 596508	6.17 6.17	.403492	27
34 35	.56535 6 .565676	5.33	.968479	.83	.596878	6.15	.403122	26 25
36	.565995	5.32 5.32	.968379	.83	.597616	6.15	.402384	24
37	.566314	5.30	.968329	.85	.597985	6.15	.402015	23 22
38	.566632	5.32	.968278	.83	.598354	6.13	.401646	21
40	.567269	5.30 5.30	.968178	.83	.599091	6.15 6.13	.400909	20
41	9.567587	5.28	9.968128	.83	9.599459	6.13	10.400541	19
42 43	.567904	5.30	.968078	.85	.599827	6.12	.400173	18 17
41	.568539	5.28 5.28	.967977	.83	.600562	6.13	.399438	16
45	.568856	5.27	.967927	.83 .85	.600929	6.12 6.12	.399071	15
46	.569172 .569488	5.27	.967876 .967826	.83	.601296 .601663	6.12	.398704	14 13
48	.569804	5.27 5.27	.967775 .967725 .967674	.85 .83	.602029	6.10	.397971	12
49	.570120	5.25	.967725	.85	.602395	6.10	.397605 .397239	11 10
		5.27		.83		6.10		9
51 52	9.570751 .571066	5.25	9.967624 .967573	.85	9.603127	6.10	10.396873	8
53	.571380	5.23 5.25	.967522	.85 .85	.603858	6.08	.396142	8 7 6 5 4 3 2
54	.571695 .572009	5.23	.967471 .967421	.83	.604223 .604588	6.08	.395777	6
56	.572323	5.23	.967370	.85	.604953	6.08	.395047	4
57	.572636	5.22 5.23	.967319	.85 .85	.605317	6.07	.394683	3
58	.572950	5.22	.967268	.85	.605682	6.07	.394318	2
60	9.573575	5.20	9.967166	.85	9.606410	6.07	10.393590	ō
1	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	
	cosine.	D. 1.	Sine.	D. I.	Cotang.	D. 1.	rang.	1

111° 68° 125

22*								1574
,	Sine.	D. 1".	Cosine.	D. 1'.	Tang.	D. 1*.	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.573575 .573888 .574200 .574512 .574824 .575136 .575447 .575758 .576069 .576879	5.22 5.20 5.20 5.20 5.20 5.18 5.18 5.18 5.17 5.17 5.17	9.967166 .967115 .967064 .967013 .966961 .966959 .966859 .966756 .966705 .966653	.85 .85 .85 .87 .85 .85 .85 .87 .85	9.606410 .606773 .607137 .607500 .607863 .608525 .60858 .608950 .609312 .609674 .610036	6.05 6.07 6.05 6.05 6.03 6.05 6.03 6.03 6.03 6.03 6.03	10.393590 .393227 .392863 .392500 .392137 .391775 .391412 .391050 .390888 .390836 .389964	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.576999 .577309 .577618 577927 .578236 .578545 .578853 .579162 .579470 .579777	5.17 5.15 5.15 5.15 5.15 5.15 5.13 5.13 5.13	9,966602 .966550 .966499 .966447 .966395 .966344 .966292 .966240 .966188 .966136	.87 .85 .87 .87 .85 .87 .87 .87	9.610397 .610759 .611120 .611480 .611841 .612201 .612561 .612921 .613281 .613641	6.03 6.02 6.00 6.02 6.00 6.00 6.00 6.00 6.00	10 389603 .389241 .388880 .388520 .388159 .387799 .387439 .387079 .386719 .386359	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.580085 580392 .580699 .581005 .581312 .581618 .581924 .582229 .582535 .582840	5.12 5.12 5.10 5.12 5.10 5.10 5.08 5.10 5.08 5.08	9.966085 966033 .965981 .965929 .965876 .965824 .965772 .965720 .965668 .965615	.87 .87 .88 .87 .87 .87 .87 .88	9.614000 .614359 .614718 .615077 .615435 .615793 .616151 .616509 .616867 .617224	5.98 5.98 5.98 5.97 5.97 5.97 5.97 5.97 5.97 5.97	10.386000 .385641 .385282 .384923 .384505 .384207 .383849 .383491 .383133 .382776	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.583145 .583449 583754 .584058 .584361 .584665 .584968 .585272 .585574 .585877	5.07 5.08 5.07 5.05 5.07 5.05 5.07 5.03 5.05 5.05	9 965563 965511 965458 965406 965353 965301 965248 . 965195 . 965143 . 965090	.87 .88 .87 .88 .87 .88 .87 .88	9 617582 617939 .618295 .618652 619068 .619364 .619720 .620076 .620432 .620787	5.95 5.98 5.98 5.98 5.93 5.93 5.93 5.93 5.92 5.92	10 382418 .382061 .381705 .381348 .380936 .380636 .380280 .379924 .379568 .379213	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.586179 .586482 .586783 .587085 .587386 .587688 .587689 .588289 .588289 .588590	5.05 5.02 5.03 5.02 5.03 5.02 5.00 5.00 5.00	9.965037 .964984 .964931 .964879 .964826 .964773 .964720 .964666 .964613 .964560	.88 .88 .87 .88 .88 .88 .90 .88	9.621142 621497 .621852 622207 .622561 .62369 .623623 .623976 .624330	5.92 5.92 5.92 5.90 5.90 5.90 5.90 5.88 5.88	10.378858 .378503 .378148 .377793 .377439 .377085 .376731 .376377 .376024 .375670	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.589190 .589489 .589789 .590088 .590686 .590686 .590984 .591282 .591580 9.591878	4.98 5.00 4.98 4.98 4.98 4.97 4.97 4.97 4.97	9.964507 .964454 .964400 .964347 .964294 .964240 .964187 .964133 .964080 9.964026	.88 .90 .88 .88 .90 .88 .90	9.624683 .625036 .625388 .625741 .626093 .626445 .626797 .627149 .627501 9.627852	5.88 5.87 5.88 5.87 5.87 5.87 5.87 5.87	10.375317 .374964 .374612 .374259 .373907 .373555 .373203 .372851 .372499 10.372148	9 8 7 6 5 4 3 2 1 0
,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	,

23°						,		196
	Sine.	D. 1".	Cosine.	D. 1*.	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.591878 .592176 .592473 .592770 .593667 .59363 .593659 .593955 .594251 .594547 .594842	4.97 4.95 4.95 4.95 4.93 4.93 4.93 4.93 4.92 4.92	9.964026 .963972 .963919 .963865 .963811 .963757 .963704 .963650 .963596 .963542 .963488	.90 .88 .90 .90 .90 .88 .90 .90	9.627852 628203 628554 628905 629255 629606 629956 630306 630656 631005 631355	5.85 5.85 5.85 5.83 5.83 5.83 5.83 5.83	10.372148 .371797 .371446 .371095 .370745 .370394 .370044 .369694 .369344 .368995 .368645	60 59 58 57 56 55 54 53 52 51
11 12 13 14 15 16 17 18 19 20	9.595137 .595432 .595727 .596021 .596315 .596609 .596903 .597196 .597490 .597783	4.92 4.92 4.90 4.90 4.90 4.88 4.90 4.88 4.87	9.963434 .963379 .963325 .963271 .963217 .963163 .963108 .963054 .962999 .962945	.90 .90 .90 .90 .90 .92 .90 .92	9.631704 .632053 .632402 .632750 .633699 .633447 .633795 .634143 .634490 .634838	5.82 5.82 5.80 5.82 5.80 5.80 5.80 5.78 5.80 5.78	10.368296 .367947 .367598 .367250 .366901 .366553 .366205 .365857 .36510 .365162	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.598075 .598368 .598660 .598952 .599244 .599536 .599827 .600118 .600409 .600700	4.88 4.87 4.87 4.87 4.87 4.85 4.85 4.85 4.85	9.962890 .962836 .962781 .962727 .962672 .962617 .962562 .962508 .962453 .962398	.90 .92 .90 .92 .92 .92 .92 .92 .92	9.635185 .635532 .635879 .636226 .636572 .636919 .637265 .637611 .637956 .638302	5.78 5.78 5.77 5.77 5.77 5.77 5.77 5.77	10.364815 .364468 .364121 .363774 .363428 .363081 .362735 .362389 .362044 .361698	39 38 37 36 35 34 33 32 31 30
31 32 33 34 85 36 37 38 39 40	9.600990 .601280 .601570 .601860 .602150 .602439 .602728 .603017 .603305 .603594	4.83 4.83 4.83 4.83 4.82 4.82 4.82 4.80 4.82	9.962343 .962288 .962233 .962178 .962123 .962067 .962012 .961957 .961902 .961846	.92 .92 .92 .93 .93 .92 .92 .93 .92	9.638647 .638992 .639337 .639682 .640027 .640371 .640716 .641060 .641404 .641747	5.75 5.75 5.75 5.75 5.75 5.73 5.73 5.73	10.361353 .361008 .360663 .360318 .359973 .359629 .359284 .358940 .358596 .358253	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.603882 .604170 .604457 .604745 .605032 .605319 .605606 .605892 .606179 .606465	4.80 4.78 4.80 4.78 4.78 4.77 4.77 4.77	9.961791 .961735 .961680 .961624 .961569 .961513 .961458 .961402 .961346 .961290	.93 .92 .93 .92 .93 .92 .93 .93 .93	9.642091 .642434 .642777 .643120 .643463 .643806 .644148 .644490 .644832 .645174	5.72 5.72 5.72 5.72 5.72 5.70 5.70 5.70 5.70 5.70	10.357909 .357566 .357323 .356880 .356537 .356194 .355852 .35510 .355168 .354826	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.606751 .607036 .607322 .607607 .607892 .608177 .608461 .608745 .609029 9.609313	4.75 4.77 4.75 4.75 4.75 4.73 4.73 4.73 4.73	9.961235 .961179 .961123 .961067 .961011 .960955 .960899 .960843 .960786 9.960730	.93 .93 .93 .93 .93 .93 .93 .93 .93	9.645516 .645857 .646199 .646540 .646881 .647222 .647562 .647903 .648243 9.648583	5.68 5.70 5.68 5.68 5.68 5.67 5.67 5.67	10.354484 .354143 .353801 .353460 .353119 .352778 .352438 .352097 .351757 10.351417	9 8 7 6 5 4 3 2 1 0
1	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	,

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24°			,	,				155
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1*.	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.609313 .609597 .609880 .610164 .610447 .610729 .611012 .611294 .611576 .611858 .612140	4.73 4.73 4.73 4.73 4.70 4.70 4.70 4.70 4.70 4.68	9.960730 .960674 .960618 .960561 .960505 .960448 .960392 .960335 .960279 .960222 .960165	.93 .93 .95 .93 .95 .95 .98 .95 .95	9.648583 .648923 .649263 .649602 .649942 .650281 .650620 .650959 .651297 .651636 .651974	5.67 5.65 5.65 5.65 5.65 5.63 5.63 5.63 5.63	10.351417 .351077 .350737 .350398 .350058 .349719 .349380 .349041 .348703 .348364 .348026	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.612421 .612702 .612983 .613264 .613545 .613825 .614105 .614385 .614665 .614944	4.68 4.68 4.68 4.68 4.67 4.67 4.67 4.67 4.65 4.65	9.960109 .960052 .959995 .959938 .959882 .959825 .959768 .959711 .959654 .959596	.95 .95 .95 .93 .95 .95 .95 .95 .95	9.652312 .652650 .652988 .653326 .654000 .654337 .654674 .655011 .655348	5.63 5.63 5.63 5.62 5.62 5.62 5.62 5.62 5.62 5.62 5.62	10.347688 .347350 .347012 .346674 .346877 .346000 .345663 .345326 .344989 .344652	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.615223 .615502 .615781 .616060 .616338 .616616 .616894 .617172 .617450 .617727	4.65 4.65 4.65 4.63 4.63 4.63 4.63 4.63 4.62 4.62	9,959539 ,959482 ,959425 ,959368 ,959310 ,95925 ,959138 ,959138 ,959080 ,959023	.95 .95 .95 .97 .95 .97 .95 .97	9.655684 .656020 .656356 .65692 .657028 .657364 .657699 .658034 .658369 .658704	5.60 5.60 5.60 5.60 5.58 5.58 5.58 5.58 5.58	10.344316 .343980 .343644 .343308 .342972 .342636 .342301 .341966 .341631 .341296	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.618004 .618581 .618558 .618834 .619110 .619386 .619662 .61938 .620213 .620488	4.62 4.62 4.60 4.60 4.60 4.60 4.58 4.58 4.58	9.958965 .958908 .95850 .958792 .958734 .958619 .958619 .958503 .958445	.95 .97 .97 .97 .95 .97 .97 .97	9.659039 .659373 .659708 .660042 .660376 .660710 .661043 .661377 .661710 .662043	5.57 5.58 5.57 5.57 5.57 5.55 5.55 5.55	10.340961 .340627 .340292 .339958 .339624 .339290 .338957 .338623 .338290 .337957	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.620763 .621038 .621313 .621587 .621861 .622135 .622409 .622682 .622956 .623229	4.58 4.58 4.57 4.57 4.57 4.57 4.55 4.55 4.55	9.958387 .958329 .958271 .958213 .958154 .958096 .958038 .957979 .957921 .957863	.97 .97 .97 .98 .97 .97 .98 .97 .97	9.662376 .662709 .663042 .663375 .663707 .664039 .664371 .664703 .665035	5.55 5.55 5.55 5.53 5.53 5.53 5.53 5.53	10.337624 .337291 .336958 .386625 .335961 .335629 .335297 .334965 .334634	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.623502 .623774 .624047 .624319 .624591 .624863 .625135 .625406 .625677 9.625948	4.53 4.55 4.53 4.53 4.53 4.53 4.52 4.52 4.52	9.957804 .957746 .957687 .957628 .957570 .957711 .957452 .957393 .957335	.97 .98 .98 .97 .98 .98 .98 .97 .98	9.665698 .666029 .666360 .666691 .667352 .667682 .668013 .668343 9.668673	5.52 5.52 5.52 5.50 5.52 5.50 5.50 5.50	10.334302 .333971 .333640 .333309 .332979 .332648 .332318 .331987 .331657 10.331327	9 8 7 6 5 4 3 2 1 0
,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	,

' Sine. D. 1". Cosine. D. 1". Tang. D. 1". Cotang. 0 9.625948 4.52 9.957276 .98 9.668673 5.48 10.331327 1 6.26219 4.52 .957217 .98 .669002 5.50 .330968 3 6.26760 4.50 .957040 .98 .669061 5.48 .330999 4 .627030 4.50 .957040 .98 .669091 5.50 .330099 5 .627300 4.50 .956981 .98 .670320 5.48 .339099 6 .627570 4.50 .956981 1.00 .670320 5.48 .33969 7 .627840 4.50 .956862 .98 .670649 5.47 .33931 7 .627840 4.48 .956684 .98 .671365 5.48 .339657 10 .628916 4.48 .956684 .98 .67291 5.47 .32331	٥		25°	IADL		TABLE X.	LUGAR	IIIMIC S	INES,		154°
1 .626219 4.52 .957217 .98 .696932 5.50 .330668 3 .626760 4.50 .957158 .98 .69332 5.50 .330668 3 .626760 4.50 .957040 .98 .669661 5.48 .330099 5 .627300 4.50 .956981 1.00 .670320 5.48 .330099 6 .627570 4.50 .956981 1.00 .670320 5.48 .339660 7 .627840 4.50 .956921 .98 .670649 5.48 .339681 8 .628109 4.48 .956802 .98 .670977 5.47 .329351 10 .628647 4.48 .956684 .98 .671663 5.48 .328634 11 9.629185 4.48 .956566 .98 .672919 5.47 .328037 12 .629185 4.47 .956367 .98 .673619 5.47 .3236726	'	Sine.	,	D. 1".		D. 1". Cosine	e. D. 1".	Tang.	D. 1*.	Cotang.	,
11 9.628916 4.48 9.956256 .98 9.672291 5.47 327351 13 629185 4.47 .956566 1.00 672917 5.47 327351 14 629721 4.47 .956447 1.00 .673274 5.45 327053 15 629989 4.47 .956387 1.00 .673602 5.47 .326736 16 .630524 4.45 .966268 1.00 .673593 5.47 .326071 18 .630759 4.45 .966268 1.00 .674257 5.47 .325743 19 .631059 4.45 .956089 1.00 .674257 5.45 .325699 20 .631326 4.45 .956089 1.00 .67537 5.43 .32569 21 9.631593 4.43 .955969 1.00 .675800 5.45 .324763 22 631859 4.43 .955969 1.00 .676849 5.43 .323110	1 2 3 4 5 6 7 8 9	.626219 .626490 .626760 .627030 .627300 .627570 .627840 .628109 .628378	1 2 3 4 5 6 7 8 9	4.52 4.50 4.50 4.50 4.50 4.50 4.48 4.48 4.48	9	4.52 .95721 4.50 .95710 4.50 .95700 4.50 .95700 4.50 .95698 4.50 .95698 4.50 .95680 4.48 .95680 4.48 .95680	7	.669002 .669332 .669661 .669991 .670320 .670649 .670977 .671306 .671635	5.50 5.48 5.50 5.48 5.47 5.48 5.47 5.48 5.47	.330998 .330668 .330339 .330009 .32965 .329351 .329023 .328694 .328365	60 59 58 57 56 55 54 53 52 51
22 631859 4.43 955969 1.00 675890 3 43 324110 23 632125 4.43 955909 1.00 676217 5.45 323783 24 632392 4.45 955849 1.00 676849 5.43 323457 25 632658 4.42 .955789 1.00 676869 5.42 .323131 26 633923 4.43 .955729 1.00 677580 5.43 .322480 27 633189 4.42 .955609 1.00 677586 5.43 .322480 28 633454 4.42 .955609 1.00 677846 5.43 .322151 29 .633719 4.42 .955488 1.00 .67846 5.42 .321829 30 .63384 4.42 .955488 1.00 .67846 5.42 .321504 31 9.634249 4.42 .955488 1.00 .679471 5.42 .32054	12 13 14 15 16 17 18 19 20	.629185 .629453 .629721 .629989 .630257 .630524 .630792 .631059	12 13 14 15 16 17 18 19 20	4.48 4.47 4.47 4.47 4.47 4.45 4.47 4.45 4.45		4.48 9.95662 4.47 9.5650 4.47 9.5644 4.47 9.5644 4.47 9.5632 4.45 9.5620 4.45 9.5620 4.45 9.5620 4.45 9.5608	56	.672619 .672947 .673274 .673602 .673929 .674257 .674254 .674911 .675237	5.47 5.45 5.45 5.45 5.47 5.45 5.45 5.45	.327053 .326726 .326398 .326071 .325743 .325416 .325089	49 48 47 46 45 44 43 42 41 40
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	22 23 24 25 26 27 28 29	.631859 .632125 .632392 .632658 .632923 .633189 .633454 .633719	22 23 24 25 26 27 28 29	4.43 4.45 4.43 4.42 4.43 4.42 4.42 4.42	9	4.43 95596 4.44 955594 4.45 95584 4.42 95572 4.43 95560 4.42 95560 4.42 95554 4.42 95554 4.42 95560	$\begin{array}{c c} 9 & 1.00 \\ 1.00 \\ 9 & 1.00 \\ 9 & 1.00 \\ 9 & 1.00 \\ 9 & 1.00 \\ 9 & 1.00 \\ 9 & 1.00 \\ 8 & 1.00 \\ \end{array}$.675890 .676217 .676543 .676869 .677194 .677520 .677846	5.45 5.48 5.43 5.42 5.43 5.43 5.42 5.42	.324110 .323783 .323457 .323131 .322806 .322480 .322154 .321829	39 38 37 36 35 34 33 32 31 30
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	32 33 34 35 36 37 38	.634514 .634778 .635042 .635306 .635570 .635834 .636097 .636360	32 33 34 35 36 37 38 39	4.42 4.40 4.40 4.40 4.40 4.38 4.38 4.38	9	4.42 9 95542 4.40 95536 4.40 95524 4.40 95512 4.40 95512 4.40 95512 4.38 95500 4.38 95494 4.38 95494	8 1.00 7 1.02 7 1.00 6 1.02 1.00 1.02 1.00 1.02 1.00 1.02 1.02	679146 .679471 .679795 .680120 .680444 .680768 .681092	5.42 5.40 5.42 5.40 5.40 5.40 5.40 5.40 5.40	.320854 .320529 .320205 .319880 .319556 .319232 .318908 .318584	29 28 27 26 25 24 23 22 21 20
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	12 13 14 15 16 47 48 19	637148 .637411 .637673 .637935 .638197 .638458 .638720 .638981	42 43 44 45 46 47 48 49	4.37 4.38 4.37 4.37 4.37 4.35 4.35 4.35 4.35	9	4.37 9 95482 4.38 95470 4.37 95464 4.37 95467 4.37 95451 4.37 95451 4.37 95433 4.35 95433 4.35 95433	3 1 02 1 1.02 1 1.02 1 0 1.02 9 1.02 8 1.02 7 1.02 6 1.02 1.02 1.02	.682387 .682710 .683033 .683356 .683679 .684001 .684324 .684646	5.40 5.38 5.38 5.38 5.38 5.37 5.38 5.37 5.37	.317613 .317290 .316967 .316644 .316321 .315999 .315676 .315354	19 18 17 16 15 14 13 12 11 10
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	52 53 54 55 56 57 58 59	.639764 .640024 .640284 .640544 .640804 .641064 .641324 .641583	52 53 54 55 56 57 58 59	4.35 4.33 4.33 4.33 4.33 4.33 4.33 4.33		4.35 9 95421 4.33 95415 4.33 95402 4.33 95890 4.33 95890 4.33 95884 4.32 95378 4.32 95378	3 1.02 1.03 1.02 1.02 1.02 1.03 1.02 1.03 1.02 1.03 1.02 1.03 1.02	. 685612 . 685934 686255 . 686577 . 686898 687219 . 687540 . 687861	5.37 5.37 5.35 5.37 5.35 5.35 5.35 5.35	314388 314066 313745 313423 313102 312781 312460 312139	9 8 7 6 5 4 3 2 1
Cosine. D. 1'. Sine. D. 1'. Cotang. D. 1'. Tang.	,	Cosine.	,	D. 1'.	1	D. 1'. Sine.	D. 1".	Cotang.	D. 1".	Tang.	,

,	Sine.	D. 1*.	Cosine.	D. 1'.	Tang.	D. 1*.	Cotang.	1
0 1 2 3 4 5 6 7 8 9	9.641842 642101 642360 642618 642877 643135 643639 643650 643908 644165 644423	4.32 4.32 4.30 4.32 4.30 4.30 4.28 4.30 4.28 4.30 4.28	9.953660 .953599 .953537 .953475 .953413 .953852 .953290 .953228 .953166 .958104 .953042	1.02 1.03 1.03 1.03 1.02 1.03 1.03 1.03 1.03 1.03 1.03	9.688182 .688502 .688823 .689143 .689463 .689783 .690103 .690423 .690742 .691062 .691381	5.33 5.32 5.33 5.33 5.33 5.33 5.32 5.32	10.311818 .311498 .311177 .310857 .310217 .310217 .309897 .309577 .309258 .308938 .308619	60 59 58 57 56 55 54 53 52 51
11 12 13 14 15 16 17 18 19 20	9.644680 .644986 .645193 .645450 .645706 .645962 .646218 .646474 .646729 .646984	4.27 4.28 4.28 4.27 4.27 4.27 4.27 4.27 4.25 4.25 4.27	9.952980 .952918 .952855 .952793 .952731 .952669 .952606 .952544 .952481	1.03 1.05 1.03 1.03 1.03 1.05 1.05 1.05 1.03 1.05	9.691700 .692019 .692358 .692656 .692975 .693293 .693612 .693930 .694248 .694566	5.32 5.32 5.30 5.32 5.30 5.32 5.30 5.30 5.30 5.30 5.30	10.308300 .307981 .307662 .307344 .307025 .306707 .306388 .306070 .305752 .305434	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.647240 .647494 .647749 .648004 .648258 .648512 .648766 .649020 .649274 .649527	4.23 4.25 4.25 4.23 4.23 4.23 4.23 4.23 4.23 4.23 4.23	9.952356 .952294 .952231 .952168 .952106 .952043 .951980 .951917 .951854 .951791	1.03 1.05 1.05 1.03 1.05 1.05 1.05 1.05 1.05 1.05	9.694883 .695201 .695518 .695836 .696153 .696470 .696787 .697103 .697420 .697736	5.30 5.28 5.30 5.28 5.28 5.28 5.27 5.28 5.27 5.28	10.305117 .304799 .304482 .304164 .303530 .303530 .303213 .302897 .302580 .302264	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.649781 .650034 .650287 .650539 .650792 .651044 .651297 .651549 .651800 .652052	4.22 4.20 4.22 4.20 4.22 4.20 4.22 4.20 4.20	9.951728 .951665 .951602 .951539 .951476 .951412 .951349 .951286 .951222 .951159	1.05 1.05 1.05 1.05 1.07 1.05 1.05 1.07 1.05 1.05	9.698053 .698369 .698685 .699001 .699316 .699632 .699947 .700263 .700578 .700893	5.27 5.27 5.27 5.25 5.27 5.25 5.27 5.25 5.25	10.301947 .301631 .301315 .300999 .30068 .300368 .300053 .299737 .299422 .299107	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.652304 .652555 .652806 .653057 .653308 .653558 .653508 .654059 .654309 .654558	4.18 4.18 4.18 4.17 4.17 4.17 4.15 4.17	9.951096 .951032 .950968 .950905 .950841 .950778 .950714 .950650 .950586 .950522	1.07 1.07 1.05 1.07 1.05 1.07 1.07 1.07 1.07	9.701208 .701523 .701837 .702152 .702466 .702781 .703095 .703409 .703722 .704036	5.25 5.23 5.25 5.25 5.25 5.23 5.23 5.23	10.298792 .298477 .298163 .297848 .297534 .297219 .296905 .296591 .296278 .295964	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.654808 .655058 .655307 .655556 .655805 .656054 .656302 .656551 .656799 9.657047	4.17 4.15 4.15 4.15 4.15 4.13 4.13 4.13 4.13	9.950458 .950394 .950330 .950266 .950202 .950138 .950074 .950010 .949945 9.949881	1.07 1.07 1.07 1.07 1.07 1.07 1.07 1.07	9.704350 .704663 .704976 .705290 .705603 .705916 .706228 .706541 .706854 9.707166	5.22 5.22 5.23 5.22 5.22 5.20 5.22 5.22 5.22 5.22 5.22	10.295650 .295337 .295024 .294710 .294397 .294084 .293772 .293459 .293146 10.292834	9 8 7 6 5 4 3 2 1 0
-/	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1'.	Tang.	
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27°				0 011111		7111300		152°
,	Sine.	D. 1".	Cosine.	D. 1*.	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.657047 657295 657542 .657790 .658037 .658284 .658531 .658778 .659025 .659271 .659271	4.13 4.12 4.13 4.12 4.12 4.12 4.12 4.12 4.10 4.10	9.949881 .949816 .949752 .949688 .949658 .949558 .949494 .949429 .949364 .949300 .949235	1.08 1.07 1.07 1.08 1.08 1.07 1.08 1.08 1.07 1.08	9.707166 .707478 .707478 .707790 .708102 .708414 .708726 .709037 .709349 .709660 .709971 .710282	5.20 5.20 5.20 5.20 5.20 5.18 5.18 5.18 5.18 5.18	10.292834 .292522 292210 .291898 .291586 .291274 .29063 .290651 .290340 .290029 .289718	60 59 58 57 56 55 54 53 52 51
11 12 13 14 15 16 17 18 19 20	9.659763 .660009 .660255 660501 660746 .660991 .661236 .661481 .661726 .661970	4.10 4.10 4.10 4.08 4.08 4.08 4.08 4.08 4.07 4.07	9.949170 949105 949040 948975 948910 .948845 948780 .948715 948650 .948584	1.08 1.08 1.08 1.08 1.08 1.08 1.08 1.08	9 710593 .710904 711215 .711525 .711836 .712146 .712456 .712766 .713076 .713386	5.18 5.18 5.17 5.18 5.17 5.17 5.17 5.17 5.17 5.17	10.289407 .289096 .288785 .288475 .288164 .287544 .287344 .286924 .286914	49 48 47 46 45 41 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.662214 .662459 .662703 662946 .663190 .663433 .663677 .663920 .664163 .664406	4.08 4.07 4.05 4.07 4.05 4.07 4.05 4.05 4.05 4.05	9.948519 948454 .948388 .948323 .948257 .948192 .948126 .948060 .947995 .947929	1.08 1.10 1.08 1.10 1.08 1.10 1.10 1.10	9.713696 714005 714314 .714624 .714933 .715242 .715551 715860 .716168 .716477	5.15 5.15 5.17 5.15 5.15 5.15 5.15 5.15	10.286304 .285995 .285686 285376 .285067 .284758 284449 .28449 .283832 .283523	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.664648 .664891 .665133 .665375 .665617 .665859 .666100 .666342 .666583 .666824	4.05 4.03 4.03 4.03 4.03 4.02 4.03 4.02 4.02 4.02	9.947863 947797 .947731 947665 .947660 .947533 .947467 .947401 .947335 .947269	1 10 1.10 1.10 1.08 1.12 1.10 1.10 1.10 1.10	9.716785 .717093 .717401 .717709 .718017 .718325 .718633 .718940 .719248 .719555	5 13 5.13 5.13 5.13 5.13 5.13 5.12 5.12 5.12	10.283215 .282907 .282599 .282291 281983 .281675 .281867 281060 .280752 .280445	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.667065 .667305 .667546 .667786 .668027 .668506 .668746 .668986 .669225	4.00 4.02 4.00 4.02 4.00 3.98 4.00 3.98 4.00 3.98 3.98	9 947203 .947136 .947070 947004 .946937 .946804 .946738 .94671 .946604	1 12 1.10 1.10 1.12 1.10 1.12 1.10 1.12 1.10	9.719862 .720169 .720476 .720476 .721089 .721396 .721702 .722009 .722315 .722621	5.12 5.12 5.12 5.10 5.12 5.10 5.12 5.10 5.10 5.10 5.10	10.280138 279831 .279524 .279217 .278911 .278604 .278298 .277991 .277685 .277379	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.669464 669703 669942 670181 670419 .670658 670896 .671134 .671372 9.671609	3.98 3.98 3.98 3.97 3.97 3.97 3.97 3.97	9.946538 .946471 .946404 .946337 .946270 .946203 .946136 .946069 .946002 9.945935	1.12 1.12 1.12 1.12 1.12 1.12 1.12 1.12	9.722927 723232 723528 .723544 724149 .724454 724760 725065 725370 9.725674	5.08 5.10 5.10 5.08 5.08 5.08 5.08 5.08 5.07	10.277073 .276768 .276462 .276156 .275851 .275546 .275240 .274935 .274630 10.274326	9 8 7 6 5 4 3 2 1
,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	-

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,	Sine.	D. 1*.	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.671609 671847 672084 672321 672558 672795 673032 673268 673505 673741 673977	3.97 3.95 3.95 3.95 3.95 3.95 3.95 3.95 3.95	9.945935 .945868 .945800 .945733 .945666 .945598 .945531 .945464 .945396 .94528 .945261	1.12 1.13 1.12 1.12 1.13 1.12 1.13 1.13	9.725674 .725979 .726284 .726588 .7265892 .727197 .727501 .727805 .728109 .728412 .728716	5.08 5.08 5.07 5.07 5.05 5.07 5.07 5.07 5.07 5.07	10.274326 .274021 .278716 .278412 .278108 .272803 .272499 .272195 .271891 .271588 .271284	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.674213 .674448 .674684 .674919 .675155 .675390 .675624 .675859 .676094 .676328	3.92 3.93 3.93 3.93 3.93 3.92 3.90 3.92 3.90 3.90 3.90	9.945193 .945125 .945058 .944990 .944922 .944854 .944718 .944650 .944582	1.13 1.12 1.13 1.13 1.13 1.13 1.13 1.13	9.729020 .729323 .729626 .729929 .730233 .730535 .730838 .731141 .731444 .731746	5.07 5.05 5.05 5.07 5.03 5.05 5.05 5.05 5.03 5.03	10.270980 .270677 .270374 .270071 .269767 .269465 .269162 .268859 .268556 .268254	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.676562 .676796 .677030 .677264 .677498 .677731 .677964 .678197 .678430 .678663	3.90 3.90 3.90 3.90 3.88 3.88 3.88 3.88 3.88	9.944514 .944367 .944309 .944241 .944172 .94404 .944036 .943967 .943899	1.13 1.15 1.13 1.13 1.15 1.13 1.13 1.15 1.13	9.732048 .732351 .732653 .732955 .733257 .733558 .733860 .734162 .734463 .734764	5.05 5.03 5.03 5.03 5.02 5.03 5.02 5.03 5.02 5.02 5.02	10.267952 .267649 .267347 .267045 .266743 .266442 .266140 .265838 .265537 .265236	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.678895 .679128 .679360 .679592 .679824 .680056 .680288 .680519 .680750 .680982	3.88 3.87 3.87 3.87 3.87 3.87 3.85 3.85 3.85 3.87	9.943830 .943761 .943693 .943624 .943555 .943486 .943417 .943348 .943279 .943210	1.15 1.13 1.15 1.15 1.15 1.15 1.15 1.15	9.735066 .735367 .735668 .735969 .736269 .736570 .736870 .737171 .737471	5.02 5.02 5.02 5.00 5.00 5.00 5.00 5.00	10.264934 .264633 .264332 .264031 .263731 .263430 .263130 .262829 .262529 .262229	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.681213 .681443 .681674 .681905 .682135 .682365 .682595 .682825 .683055 .683284	3.83 3.85 3.85 3.83 3.83 3.83 3.83 3.83	9.943141 .94:072 .943003 .942934 .942864 .942795 .942726 .942656 .942587 .942517	1.15 1.15 1.15 1.17 1.15 1.15 1.17 1.15 1.17 1.15	9.738071 .738371 .738671 .738971 .739271 .739570 .739870 .740169 .740468 .740767	5.00 5.00 5.00 5.00 4.98 5.00 4.98 4.98 4.98	10.261929 .261629 .261329 .261029 .260729 .260430 .260130 .259831 .259532 .259233	19 18 17 16 15 14 13 12 11
51 52 53 54 55 56 57 58 59 60	9.683514 .683743 .683972 .684201 .684430 .684658 .684887 .685115 .685343 9.685571	3.82 3.82 3.82 3.82 3.80 3.80 3.80 3.80 3.80	9.942448 .942378 .942308 .942239 .942069 .942029 .941959 .941889 9.941819	1.17 1.17 1.15 1.17 1.17 1.17 1.17 1.17	9.741066 .741365 .741664 .741962 .742261 .742559 .742858 .743156 .743454 9.743752	4.98 4.98 4.97 4.98 4.97 4.98 4.97 4.97 4.97	10.258934 .258635 .258336 .258038 .257739 .257142 .256844 .256546 10.256248	9 8 7 6 5 4 3 2 1
,	Cosine.	D. 1'.	Sine.	D. 1".	Cotang.	D. 1'.	Tang.	′

29°		IADL						150°
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.685571 .685799 .686027 .686254 .686482 .686709 .686936 .687163 .687849	3.80 3.80 3.78 3.78 3.78 3.78 3.77 3.78 3.78	9.941819 .941749 .941679 .941609 .941539 .941398 .941328 .941328 .941258 .941187	1.17 1.17 1.17 1.17 1.17 1.18 1.17 1.18 1.17 1.18	9.743752 .744050 .744048 .744645 .744645 .745240 .745538 .775835 .745135 .746129 .746726	4.97 4.97 4.95 4.97 4.95 4.97 4.95 4.95 4.95 4.95	10.256248 .255950 .255652 .255355 .255057 .254760 .254462 .254165 .258868 .253871 .253274	59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9. 688069 688295 .688521 .688747 .688972 .689198 .689423 .689648 .689873 .690098	3.77 3.77 3.77 3.77 3.75 3.75 3.75 3.75	9.941046 .940975 .940905 .940834 .940763 .940693 .940622 .940551 .940480 .940409	1.18 1.17 1.18 1.18 1.17 1.18 1.18 1.18	9.747023 .747319 .747616 .747913 .748209 .748505 .748801 .749097 .749393 .749689	4.93 4.93 4.95 4.93 4.93 4.93 4.93 4.93 4.93 4.93	10.252977 .252681 .252384 .252087 .251791 .251499 .251199 .250903 .250607 .250311	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.690323 .690548 .690772 .690996 .691220 .691444 .691668 .691892 .692115 .692339	3.75 3.73 3.73 3.73 3.73 3.73 3.73 3.73	9.940338 .940267 .940196 .940125 .940054 .939982 .939011 .939840 .939768 .939697	1.18 1.18 1.18 1.18 1.20 1.18 1.18 1.20 1.18	9.749985 .750281 .750576 .750872 .751167 .751462 .751757 .752052 .752347 .752642	4.93 4.92 4.93 4.92 4.92 4.92 4.92 4.92 4.92 4.92 4.92	10.250015 .249719 .249424 .249128 .248538 .248538 .248243 .247948 .247653 .247358	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.692562 .692785 .693008 .693231 .693453 .693676 .693898 .694120 .694342 .694564	3.72 3.73 3.73 3.70 3.70 3.70 3.70 3.70	9.939625 .939554 .939482 .939410 .939339 .939267 .939195 .939123 .939052 .938980	1.18 1.20 1.20 1.18 1.20 1.20 1.18 1.20 1.120 1.18	9.752937 .753231 .753526 .753820 .754115 .754409 .754703 .754997 .755291 .755585	4.90 4.92 4.90 4.92 4.90 4.90 4.90 4.90 4.88	10.247063 .246769 .246474 .246180 .245885 .245885 .245591 .245297 .245003 .244709 .244415	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.694786 .695007 .695229 .695450 .695671 .695892 .696113 .696334 .696554 .696775	3.68 3.70 3.68 3.63 3.68 3.68 3.68 3.68 3.68 3.68	9.938908 .938836 .938763 .938619 .938547 .938475 .938402 .938330 .938258	1.20 1.22 1.20 1.20 1.20 1.20 1.22 1.20 1.22	9.755878 .756172 .756465 .756759 .757052 .757345 .757638 .757931 .758224 .758517	4.90 4.88 4.90 4.88 4.88 4.88 4.88 4.88 4.88	10.244122 .243828 .243535 .243241 .242948 .242655 .242362 .242069 .241776 .241483	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.696995 .697215 .697435 .697654 .697874 .698094 .698313 .698532 .698751 9.698970	3.67 3.67 3.65 3.67 3.65 3.65 3.65 3.65 3.65	9.938185 .938113 .938040 .937967 .937895 .937749 .937676 .937604 9.937531	1.20 1.22 1.22 1.20 1.22 1.22 1.22 1.22	9.758810 .759102 .759395 .759687 .759687 .760272 .760564 .760856 .761148 9.761439	4.87 4.88 4.87 4.87 4.87 4.87 4.87 4.87	10.241190 .240898 .240605 .240603 .240021 .239728 .239436 .239144 .238852 10.238561	9 8 7 6 5 4 3 2 1
,	Cosine.	D. 1".	Sine,	D. 1".	Cotang.	D. 1*.	Tang.	,
4								-

0°								149
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4	9.698970 .699189 .699407 .699626 .699844	3.65 3.63 3.65 3.63 3.63	9.937531 .937458 .937385 .937312 .937238	1.22 1.22 1.22 1.23 1.23 1.22	9.761439 .761731 .762023 .762314 .762606	4.87 4.87 4.85 4.87 4.85	10.238561 .238269 .237977 .237686 .237394	60 59 58 57 56
5 6 7 8 9	.700062 .700280 .700498 .700716 .700933 .701151	3.63 3.63 3.63 3.62 3.63 3.62	.937165 .937092 .937019 .936946 .936872 .936799	1.22 1.22 1.22 1.23 1.22 1.23	.762897 .763188 .763479 .763770 .764061 .764352	4.85 4.85 4.85 4.85 4.85	.237103 .236812 .236521 .236230 .235939 .235648	55 54 53 52 51 50
11 12 13 14 15 16 17	9.701368 .7.1585 .701802 .702019 .702236 .702452 .702669	3.62 3.62 3.62 3.62 3.60 3.62	9.936725 .936652 .936578 .936505 .936431 .936357 .936284	1.22 1.23 1.22 1.23 1.23 1.23	9.764643 .764933 .765224 .765514 .765805 .766095 .766285	4.85 4.83 4.85 4.83 4.85 4.83 4.83	10.235357 .235067 .234776 .234486 .234195 .233905 .233615	49 48 47 46 45 41 43
18 19 20 21	.702885 .703101 .703317 9,703533	3.60 3.60 3.60 3.60	.936210 .936136 .936062 9.935988	1,23 1,23 1,23 1,23	.766675 .766965 .767255 9.767545	4.83 4.83 4.83 4.83	.233325 .233035 .232745 10,232455	42 41 40 39
22 23 24 25 26 27 28 29 30	9.703535 .703749 .703964 .704179 .704395 .704610 .704825 .705040 .705254 .705469	3.60 3.58 3.58 3.60 3.58 3.58 3.58 3.57 3.58	9.935938 .935914 .935840 .935766 .935692 .935618 .935543 .93549 .935395	1.23 1.23 1.23 1.23 1.23 1.25 1.23 1.25 1.23	7.67544 .768124 .768124 .768414 .768703 .768992 .769281 .769571 .769560 .770148	4.82 4.83 4.83 4.82 4.82 4.82 4.83 4.82 4.80 4.82	232166 231876 231876 231586 231297 231008 230719 230429 230140 229852	38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.705683 .705898 .706112 .706326 .706539 .706753 .706967 .707180 .707393 .707606	3.58 3.57 3.57 3.55 3.57 3.57 3.55 3.55 3.55	9.935246 .935171 .935097 .935022 .934948 .934873 .934798 .934723 .934649 .934574	1.25 1.23 1.25 1.23 1.25 1.25 1.25 1.25 1.25 1.25	9.770437 .770726 .771015 .771303 .771592 .771880 .772168 .772457 .772745 .773033	4.82 4.82 4.80 4.80 4.80 4.80 4.80 4.80 4.80 4.80	10,229563 ,229274 ,228985 ,228697 ,228408 ,228120 ,227832 ,227343 ,227255 ,226967	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.707819 .708032 .708245 .708458 .708670 .708882 .709094 .709306 .709518 .709730	3.55 3.55 3.55 3.55 3.53 3.53 3.53 3.53	9.934499 .934349 .934374 .934199 .934123 .934048 .933973 .933898 .933822	1.25 1.25 1.25 1.25 1.27 1.25 1.25 1.25 1.25	9.773321 .773608 .773896 .774184 .774471 .774759 .775046 .775333 .775621 .775908	4.78 4.80 4.80 4.78 4.78 4.78 4.78 4.78 4.78	10.226679 .226392 .226104 .225816 .225529 .225241 .224954 .224667 .224379 .224092	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58	9.709941 .710153 .710364 .710575 .710786 .710997 .711208 .711419	3.53 3.52 3.52 3.52 3.52 3.52 3.52 3.52	9.933747 .933671 .933596 .933520 933445 .93369 .933293 .933217	1.27 1.25 1.27 1.25 1.27 1.27 1.27 1.27 1.27	9.776195 .776482 .776768 .777055 .777342 .777628 .777915 .778201	4.78 4.77 4.78 4.78 4.77 4.78 4.77 4.78	10.223805 .223518 .223232 .222945 .222658 .222372 .222085 .221799	9 8 7 6 5 4 3 2
59 60	.711629 9.711839 Cosine.	3.50 D. 1".	9.933141 9.933066 Sine.	1.27 1.25 D. 1'.	.778488 9.778774 Cotang.	4.77	.221512 10.221226 Tang.	0

31.					TILMIO K			148°
,	Sine.	D. 1*.	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.711839 .712050 .712260 .712469 .712679 .712889 .713098 .713308 .713517 .713726 .713935	3.52 3.50 3.48 3.50 3.48 3.50 3.48 3.48 3.48 3.48	9,933066 .932990 .932914 .932838 .932762 .932685 .932609 .932533 .932457 .932380 .932304	1.27 1.27 1.27 1.27 1.27 1.28 1.27 1.27 1.27 1.23 1.27	9.778774 .779060 .779346 .779632 .779918 .780203 .780489 .780775 .781060 .781346 .781631	4.77 4.77 4.77 4.77 4.75 4.77 4.77 4.77	10.221226 .220940 .220654 .220868 .220868 .219797 .219511 .219225 .218940 .218654 .218369	60 59 58 57 56 55 54 53 52 51
11 12 13 14 15 16 17 18 19 20	9.714144 .714352 .714561 .714769 .714978 .715186 .715394 .715602 .715809 .716017	3.47 3.48 3.47 3.48 3.47 3.47 3.47 3.45	9.932228 .932151 .932075 .931992 .931921 .931845 .931768 .931691 .931614 .931537	1.28 1.27 1.28 1.28 1.27 1.28 1.28 1.28 1.28	9.781916 .782201 .782486 .782771 .783056 .783341 .783626 .783910 .784195 .784479	4.75 4.75 4.75 4.75 4.75 4.75 4.75 4.73 4.73 4.73 4.75	10.218084 .217799 .217514 .217229 .216944 .216659 .216374 .216090 .215805 .215521	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.716224 .716432 .716639 .716846 .717053 .717259 .717466 .717673 .717879 .718085	3.47 3.45 3.45 3.45 3.45 3.45 3.45 3.45 3.43 3.43	9.931460 .931383 .931306 .931229 .931152 .931075 .930998 .930921 .930843 .930766	1.28 1.28 1.28 1.28 1.28 1.28 1.28 1.30 1.28 1.30	9.784764 .785048 .785332 .785616 .785900 .786184 .786468 .786752 .787036 .787319	4.73 4.73 4.73 4.73 4.73 4.73 4.73 4.73	10.215236 .214952 .214668 .214384 .214100 .213816 .215532 .213248 .212964 .212681	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.718291 .718497 .718703 .718909 .719114 .719320 .719525 .719730 .719935 .720140	3.43 3.43 3.42 3.42 3.42 3.42 3.42 3.42	9.930688 .930611 .930533 .930456 .930378 .930300 .930223 .930145 .93067 .929989	1.28 1.30 1.28 1.30 1.30 1.30 1.30 1.30 1.30	9.787603 .787886 .788170 .788453 .788736 .789019 .789302 .789585 .789868 .790151	4.72 4.73 4.72 4.72 4.72 4.72 4.72 4.72 4.72 4.72	10.212397 .212114 .211830 .211547 .211264 .210981 .210698 .210415 .210132 .209849	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.720845 .720549 .720754 .720754 .720958 .721162 .721366 .721570 .721774 .721978 .722181	3.40 3.42 3.40 3.40 3.40 3.40 3.40 3.40 3.40 3.40	9.929911 .929833 .929755 .929677 .929599 .929521 .929442 .929364 .929286 .929207	1.30 1.30 1.30 1.30 1.30 1.32 1.30 1.30 1.32 1.30	9.790434 .790716 .790999 .791281 .791563 .791846 .792128 .792410 .792692 .792974	4.70 4.72 4.70 4.70 4.70 4.70 4.70 4.70 4.70 4.70	10.209566 .209284 .209001 .208719 .208437 .208154 .207872 .207590 .207308 .207026	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.722385 .722588 .722791 .722994 .723197 .723400 .723603 .723805 .724007 9.724210	3.38 3.38 3.38 3.38 3.38 3.38 3.37 3.37	9.929129 .929050 .928972 .928893 .928815 .928736 .928657 .928578 .928499 9.928420	1.32 1.30 1.32 1.30 1.32 1.32 1.32 1.32 1.32	9.793256 .793538 .793819 .794101 .794383 .794664 .794946 .795227 .795508 9.795783	4.70 4.68 4.70 4.70 4.68 4.70 4.68 4.68 4.68	10.206744 .206462 .206181 .205899 .205617 .205336 .205054 .204773 .204492 10.204211	9 8 7 6 5 4 3 2 1 0
,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	,

32°		00000	o, imidi	1110, A	ND COIA	MULLI		147
,	Sine.	D. 1'.	Cosine.	D. 1'.	Tang.	D. 1'.	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.724210 .724412 .724614 .724816 .725017 .725219 .725622 .725823 .726024 .726225	3.37 3.37 3.37 3.35 3.37 3.35 3.35 3.35	9.928420 .928342 .928263 .928183 .928104 .928025 .927946 .927867 .927787 .927787	1.30 1.32 1.33 1.32 1.32 1.32 1.32 1.33 1.32 1.32	9.795789 .796070 .796351 .796632 .799113 .797194 .797474 .797755 .798036 .798316 .798596	4.68 4.68 4.68 4.68 4.68 4.67 4.68 4.67 4.68 4.67 4.68	10.204211 .203930 .203649 .203368 .203087 .202806 .202526 .202245 .201964 .201684	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.726426 .726626 .726827 .721027 .727228 .727428 .727628 .727828 .728027 .728227	3.83 3.85 3.85 3.85 3.85 3.83 3.83 3.83	9.927549 .927470 .927390 .927310 .927231 .927751 .927071 .926991 .926911 .926831	1.32 1.33 1.33 1.32 1.33 1.33 1.33 1.33	9.798877 .799157 .799437 .799717 .799997 .800277 .800557 .800836 .801116 .801396	4.67 4.67 4.67 4.67 4.67 4.67 4.65 4.67 4.67 4.65	10.201123 .200843 .200563 .200283 .200003 .199723 .199443 .199164 .198884 .198604	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.728427 .728626 .728825 .729024 .729223 .729422 .729621 .729820 .730018 .730217	3.32 3.32 3.32 3.32 3.32 3.32 3.32 3.32	9.926751 .926671 .926591 .926511 .926431 .926351 .926270 .926190 .926110 .926029	1.33 1.33 1.33 1.33 1.33 1.35 1.33 1.35 1.33	9.801675 .801955 .802234 .802513 .802792 .803072 .803630 .803909 .804187	4.67 4.65 4.65 4.65 4.67 4.65 4.65 4.65 4.63 4.65	10.198325 .198045 .197766 .197487 .197208 .196928 .196649 .196370 .196091 .195813	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.730415 .730613 .730613 .730811 .731009 .731206 .731404 .781602 .731799 .731996 .732193	3.30 3.30 3.30 3.28 3.30 3.30 3.28 3.28 3.28	9.925949 .925868 .925788 .925707 .925626 .925545 .925465 .925384 .925303 .925222	1.35 1.33 1.35 1.35 1.35 1.35 1.35 1.35	9.804466 .804745 .805023 .805302 .805580 .805859 .806137 .806415 .806693 .806971	4.65 4.63 4.65 4.63 4.63 4.63 4.63 4.63 4.63	10.195534 .195255 .194977 .194698 .194420 .194141 .198863 .193585 .193307 .193029	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.732390 .732587 .732784 .732980 .733177 .73373 .73369 .73765 .733961 .734157	3.28 3.27 3.27 3.28 3.27 3.27 3.27 3.27 3.27	9.925141 .925060 .924979 .924897 .924816 .924735 .924654 .924572 .924491 .924409	1.35 1.35 1.37 1.35 1.35 1.35 1.37 1.35 1.37	9.807249 .807527 .807805 .808083 .808361 .808638 .808916 .809193 .809471 .809748	4.63 4.63 4.63 4.63 4.62 4.63 4.62 4.63 4.62 4.62	10.192751 .192473 .192195 .191917 .191639 .191362 .191084 .190807 .190529 .190252	19 18 17 16 15 14 13 12 11
51 52 53 54 55 56 57 58 59 60	9.734353 .734549 .734744 .734939 .735135 .735330 .735525 .735719 .735914 9 .736109	3.27 3.25 3.25 3.27 3.25 3.25 3.25 3.25 3.25 3.25	9.924328 .924246 .924164 .924083 .924001 .923919 .923837 .923755 .923673 9.923591	1.37 1.37 1.35 1.37 1.37 1.37 1.37 1.37	9.810025 .810302 .810580 .810857 .811134 .811410 .811687 .811964 .812241 9.812517	4.62 4.63 4.62 4.62 4.62 4.62 4.62 4.62 4.62 4.62	10.189975 .189698 .189420 .189143 .18866 .188590 .188313 .188036 .187759 10.187483	9 8 6 5 4 3 2 1 0
	Cosine.	D. 1".	Sine.	D. 1'.	Cotang.	D. 1'.	Tang.	-
								-

83°		IAB	LE X.—.	LOGAN.	LITMIC)	SIN ES,		146°
,	Sine.	D. 1'.	Cosine.	D. 1".	Tang.	D. 1'.	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.736109 .736303 .736498 .736692 .736896 .737274 .737467 .737467 .737661 .737855 .738048	3.23 3.25 3.23 3.23 3.23 3.23 3.22 3.22	9.923591 .923509 .923427 .923455 .923263 .923181 .923098 .923016 .922933 .922851 .922768	1.37 1.37 1.37 1.37 1.37 1.38 1.37 1.38 1.37	9.812517 .812794 .813070 .813347 .813623 .813899 .814176 .814452 .815004 .815004	4.62 4.60 4.62 4.60 4.60 4.60 4.60 4.60 4.60 4.58	10.187483 .187206 .186930 .186653 .186677 .186101 .185824 .185548 .185272 .184996 .184720	60 59 58 57 56 55 54 53 52 51
11 12 13 14 15 16 17 18 19 20	9.738241 .738434 .738627 .738820 .739013 .739206 .739398 .739590 .739783 .739975	3.22 3.22 3.22 3.22 3.22 3.20 3.20 3.20	9.922686 .922603 .922520 .922438 .922355 .922272 .922189 .922106 .922023 .921940	1.38 1.38 1.37 1.38 1.38 1.38 1.38 1.38 1.38	9.815555 .815831 .816107 .816382 .816658 .816933 .817209 .817484 .817759 .818065	4.60 4.60 4.58 4.60 4.58 4.58 4.58 4.58 4.58 4.60 4.58	10.184445 .184169 .183893 .183618 .183342 .183067 .182791 .182516 .182241 .181965	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.740167 .740359 .740550 .740742 .740934 .741125 .741316 .741508 .741699 .741889	3.20 3.18 3.20 3.20 3.18 3.18 3.20 3.18 3.17 3.18	9.921857 .921774 .921691 .921607 .921524 .921441 .921357 .921274 .921190 .921107	1.38 1.38 1.40 1.38 1.38 1.40 1.38 1.40 1.38	9.818310 .818585 .818860 .819135 .819410 .819684 .819959 .820234 .820508 .820783	4.58 4.58 4.58 4.57 4.58 4.57 4.58 4.57 4.58 4.57	10.181690 .181415 .181140 .180855 .180590 .180316 .180041 .179766 .179492 .179217	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.742080 .742271 .742462 .742652 .742842 .743023 .743223 .743413 .743602 .743792	3.18 3.18 3.17 3.17 3.18 3.17 3.17 3.15 3.17 3.17	9.921023 .920939 .920856 .920772 .920688 .920520 .920436 .920352 .920268	1.40 1.38 1.40 1.40 1.40 1.40 1.40 1.40 1.40	9.821057 .821332 .821606 .821880 .822154 .822429 .822703 .822977 .823251 .823524	4.58 4.57 4.57 4.57 4.57 4.57 4.57 4.57 4.57	10.178943 .178668 .178394 .178120 .177846 .177571 .177297 .177023 .176749 .176476	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.743982 .744171 .744361 .744550 .744739 .744928 .745117 .745306 .745494 .745683	3.15 3.17 3.15 3.15 3.15 3.15 3.15 3.15 3.15 3.15	9.920184 .920099 .920015 .919931 .919846 .919677 .919593 .919508 .919424	1.42 1.40 1.40 1.42 1.40 1.42 1.40 1.42 1.40 1.42	9.823798 .824072 .824345 .824619 .824893 .825166 .825439 .825713 .825986 .826259	4.57 4.55 4.57 4.57 4.55 4.55 4.55 4.55	10.176202 .175928 .175655 .175811 .175107 .174834 .174561 .174287 .174014 .173741	19 18 17 16 15 14 13 12 11
51 52 53 54 55 56 57 58 59 60	9.745871 .746060 .746248 .746436 .746624 .746812 .746999 .747187 .747374 9.747562	3.15 3.13 3.13 3.13 3.13 3.12 3.12 3.13 3.12	9.919339 .919254 .919169 .919085 .919000 .918915 .918830 .918745 .918659 9.918574	1.42 1.42 1.40 1.42 1.42 1.42 1.42 1.42 1.43 1.43	9.826532 .826805 .827078 .827351 .827624 .827897 .828170 .828442 .828715 9.828987	4.55 4.55 4.55 4.55 4.55 4.55 4.55 4.53 4.53	10.173468 .173195 .172922 .172649 .172876 .172103 .171830 .171558 .171285 10.171013	9 8 7 6 5 4 3 2 1
1	Cosine.	D. 1".	Sine.	D. 1'.	Cotang.	D. 1".	Tang.	′

34								140
,	Sine.	D. 1".	Cosine.	D, 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.747562 .747749 .747936 .748123 .748310 .748497 .748683 .748870 .749056 .749243 .749429	3.12 3.12 3.12 3.12 3.12 3.10 3.12 3.10 3.12 3.10 3.12	9.918574 .918489 .918404 .918318 .918233 .918147 .918062 .917976 .917891 .917805 .917719	1.42 1.42 1.43 1.42 1.43 1.42 1.43 1.43 1.43 1.43 1.42	9.828987 .829260 .829532 .829805 .830075 .830349 .830621 .830893 .831437 .831709	4.55 4.53 4.55 4.53 4.53 4.53 4.53 4.53	10.171013 .170740 .170468 .170195 .169923 .169651 .169879 .169107 .168853 .168563 .168291	60 59 58 57 56 55 54 53 52 51
11 12 13 14 15 16 17 18 19 20	9.749615 .749801 .749987 .750172 .7503543 .750729 .750914 .751099 .751284	3.10 3.10 3.08 3.10 3.08 3.10 3.08 3.10 3.08 3.08 3.08	9.917634 .917548 .917462 .917376 .917290 .917204 .917118 .917032 .916946 .916859	1.43 1.43 1.43 1.43 1.43 1.43 1.43 1.43	9.831981 .832253 .832525 .832796 .833068 .833339 .833611 .833882 .834154 .834425	4.53 4.53 4.53 4.52 4.53 4.52 4.53 4.52 4.53 4.52 4.53 4.52 4.53 4.52 4.53	10.168019 .167747 .167745 .167204 .166932 .166661 .166389 .166118 .165846 .165575	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.751469 .751654 .751839 .752023 .752208 .752392 .752576 .752760 .752944 .753128	3.08 3.08 3.07 3.08 3.07 3.07 3.07 3.07 3.07 3.07	9.916773 .916687 .916600 .916514 .916427 .916341 .916254 .916167 .916081 .915994	1.43 1.45 1.43 1.45 1.45 1.45 1.45 1.45 1.45	9.834696 .834967 .835238 .835509 .835780 .836051 .836322 .836593 .836864 .837134	4.52 4.52 4.52 4.52 4.52 4.52 4.52 4.52	10.165304 .165033 .164762 .164491 .164290 .163949 .163407 .163407 .163136 .162866	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.753312 .753495 .753679 .753862 .754046 .754229 .754412 .754595 .754778 .754960	3.05 3.07 3.07 3.07 3.05 3.05 3.05 3.05 3.05 3.05	9.915907 .915820 .915733 .915646 .915559 .915472 .915385 .915297 .915210 .915123	1.45 1.45 1.45 1.45 1.45 1.47 1.45 1.47	9.837405 .837675 .837946 .838216 .838487 .838757 .839027 .839297 .839568 .839838	4.50 4.52 4.50 4.52 4.50 4.50 4.50 4.50 4.50 4.50	10.162595 .162325 .162054 .161784 .161513 .161243 .160973 .160703 .160432 .160162	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.755143 .755326 .755508 .755690 .755872 .756054 .756236 .756418 .756600 .756782	3.05 3.03 3.03 3.03 3.03 3.03 3.03 3.03	9.915035 .914948 .914860 .914773 .914685 .914598 .914510 .914422 .914334 .914246	1.45 1.47 1.45 1.45 1.47 1.47 1.47 1.47	9.840108 .840378 .840648 .540917 .841187 .841457 .841727 .841996 .842266 .842535	4.50 4.50 4.48 4.50 4.50 4.48 4.50 4.48 4.50	10.159892 .159622 .159352 .159083 .158813 .158543 .158273 .158004 .157734 .157465	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.756963 .757144 .757326 .757507 .757688 .757869 .758050 .758230 .758411 9.758591	3.02 3.03 3.02 3.02 3.02 3.02 3.02 3.00 3.00	9.914158 .914070 .913982 .913894 .913806 .913718 .913630 .913541 .913453 9.913365	1.47 1.47 1.47 1.47 1.47 1.47 1.47 1.48 1.47	9.842805 .843074 .843343 .843612 .843882 .844151 .844420 .844689 .844958 9.845227	4.48 4.48 4.50 4.48 4.48 4.48 4.48	10.157195 156926 .156657 .156388 .156118 .155849 .155311 .155042 10.154773	9 8 7 6 5 4 3 2 1
′	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	′

Sine. D. 1'. Cosine. D. 1'. Tang. D. 1'. Cotang. /	35°	• TABLE X.—LOGARITHMIC SINES, 14										
1 7.58722 3.00 913187 1.48 815164 4.47 1.51296 7.67 8.47 8.47 8.47 8.47 8.47 8.47 8.47 8.4	,	Sine.	D. 1'.	Cosine.	D. 1'.	Tang.	D. 1".	Cotang.	,			
11	1 2 3 4 5 6 7 8 9	.758772 .758952 .759132 .759312 .759492 .759672 .759852 .760031 .760211	3.00 3.00 3.00 3.00 3.00 3.00 2.98 3.00 2.98	.913276 .913187 .913099 .913010 .912922 .912833 .912744 .912655 .912566	1.48 1.47 1.48 1.47 1.48 1.48 1.48 1.48 1.48	.845496 .845764 .846033 .846302 .846570 .846839 .847108 .847376 .847644	4.47 4.48 4.48 4.47 4.48 4.47 4.47 4.47	.154504 .154236 .153967 .153698 .153430 .153161 .152892 .152624 .152356	59 58 57 56 55 54 53 52 51 50			
22 .762534 2.97 .911405 1.50 .851190 4.44 1.48871 38 24 .762889 2.95 .911315 1.50 .851396 4.45 .148004 37 25 .763067 2.97 .91136 1.50 .851391 4.47 .148069 36 26 .763245 2.95 .91046 1.50 .852199 4.45 .147801 34 27 .763423 2.95 .910866 1.50 .852334 4.45 .147534 33 28 .763600 2.97 .910866 1.50 .853203 4.45 .147637 33 30 .76377 2.95 .910866 1.50 .853208 4.45 .147673 33 31 9.764131 3.95 .910506 1.50 .853802 4.45 1.146198 29 32 .764308 2.95 .910415 1.52 .85409 4.45 1.45198 29	12 13 14 15 16 17 18 19 20	.760748 .760927 .761106 .761285 .761464 .761642 .761821 .761999 .762177	2.98 2.98 2.98 2.98 2.98 2.97 2.98 2.97 2.97	.912299 .912210 .912121 .912031 .911942 .911853 .911763 .911674 .911584	1.48 1.48 1.50 1.48 1.50 1.48 1.50 1.48	.848449 .848717 .848986 .849254 .849522 .849790 .850057 .850325 .850593	4.47 4.48 4.47 4.47 4.47 4.47 4.45 4.47 4.47	.151551 .151283 .151014 .150746 .150478 .150210 .149943 .149675 .149407	48 47 46 45 44 43 42 41 40			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	23 24 25 26 27 28 29	.762534 .762712 .762889 .763067 .763245 .763422 .763600 .763777 .763954	2.97 2.95 2.97 2.97 2.95 2.97 2.95 2.95 2.95	.911405 .911315 .911226 .911136 .911046 .910956 .910866 .910776 .910686	1.50 1.48 1.50 1.50 1.50 1.50 1.50 1.50	.851129 .851396 .851664 .851931 .852199 .852466 .852733 .853001 .853268	4.45 4.47 4.45 4.47 4.45 4.45 4.45 4.45	.148871 .148604 .148336 .148069 .147801 .147334 .147267 .146999 .146732	38 37 36 35 34 33 32 31 30			
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	32 33 34 35 36 37 38 39	.764308 .764485 .764662 .764838 .765015 .765191 .765367 .765544 .765720	2.95 2.95 2.93 2.95 2.93 2.93 2.93 2.93	.910506 .910415 .910325 .910235 .910144 .910054 .909963 .909873 .909782	1.52 1.50 1.50 1.52 1.50 1.52 1.50 1.52	.853802 .854069 .854336 .854603 .854870 .855137 .855404 .855671 .855938	4.45 4.45 4.45 4.45 4.45 4.45 4.45 4.45	.146198 .145931 .145664 .145397 .145130 .144863 .144596 .144329	28 27 26 25 24 23 22 21 20			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	42 43 44 45 46 47 48 49 50	.766072 .766247 .766423 .766598 .766774 .766949 .767124 .767300 .767475	2.93 2.92 2.93 2.93 2.93 2.93 2.93 2.93	.909601 .909510 .909419 .909328 .909237 .909146 .909055 .908964 .908873	1.50 1.52 1.52 1.52 1.52 1.52 1.52 1.52 1.52	.856471 .856737 .857004 .857270 .857537 .857803 .858069 .858336	4.43 4.45 4.43 4.45 4.43 4.43 4.43 4.45 4.43	.143529 .143263 .142996 .142730 .142463 .142197 .141931 .141664	18 17 16 15 14 13 12 11			
Cosine, D. 1". Sine, D. 1". Cotang, D. 1". Tang,	52 53 54 55 56 57 58 59	.767824 .767999 .768173 .768348 .768522 .768697 .768871 .769045	2.92 2.92 2.90 2.92 2.90 2.92 2.90 2.90	.908690 .908599 .908507 .908416 .908324 .908233 .908141 .908049	1.52 1.53 1.53 1.52 1.53 1.52 1.53 1.53	.859134 .859400 .859666 .859932 .860198 .860464 .860730 .860995	4.43 4.43 4.43 4.43 4.43 4.43 4.43 4.42	.140866 .140600 .140334 .140068 .139802 .139536 .139270 .139005	9 8 7 6 5 4 3 2 1			
	1	Cosine,	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	,			

30°								143
,	Sine.	D. 1".	Cosine.	D. 1'.	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.769219 769393 769566 769740 769913 770087 770260 770433 770606 770779 770952	2.90 2.88 2.90 2.88 2.90 2.88 2.88 2.88 2.88 2.88	9.907958 .907866 .907774 .907682 .907590 .907498 .907406 .907314 .907222 .907129 .907037	1.53 1.53 1.53 1.53 1.53 1.53 1.53 1.53	9,861261 .861527 .861792 .862058 .862323 .862589 .862854 .863119 .863385 .863650 .863915	4.43 4.42 4.43 4.42 4.43 4.42 4.42 4.42	10.138739 .138473 .138208 .137942 .137677 .137411 .137146 .136881 .136615 .136350 .136085	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.771125 .771298 .771470 .771643 .771815 .771987 .772159 .772331 .772503 .772675	2.88 2.87 2.88 2.87 2.87 2.87 2.87 2.87	9.906945 .906852 .906760 .906667 .906575 .906482 .906389 .906296 .906204 .906111	1.55 1.53 1.55 1.55 1.55 1.55 1.55 1.55	9.864180 .864445 .864710 .864975 .865240 .865505 .865770 .866035 .866300 .866564	4.42 4.42 4.42 4.42 4.42 4.42 4.42 4.42	10.135820 .135555 .135290 .135025 .134760 .134495 .134230 .133965 .138700 .133436	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.772847 .773018 .773190 .773361 .773533 .773704 .773875 .774046 .774217 .774388	2.85 2.87 2.85 2.85 2.85 2.85 2.85 2.85 2.85 2.85	9.906018 .905925 .905832 .905739 .905645 .905552 .905459 .905366 .905272 .905179	1.55 1.55 1.55 1.57 1.55 1.55 1.55 1.55	9.866829 .867094 .867358 .867623 .867827 .868152 .868416 .868680 .868945 .869209	4.42 4.40 4.42 4.40 4.42 4.40 4.42 4.40 4.42 4.40 4.40	10.133171 .132906 .132642 .132377 .132113 .131848 .131584 .131320 .131055 .130791	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.774558 .774729 .774899 .775070 .775240 .775410 .775580 .775750 .775920 .776090	2.85 2.83 2.85 2.83 2.83 2.83 2.83 2.83 2.83 2.83	9.905085 .904992 .904898 .904804 .904711 .904617 .904523 .904429 .904335 .904241	1.55 1.57 1.57 1.55 1.57 1.57 1.57 1.57	9.869473 .869737 .870001 .870265 .870529 .870793 .871057 .871321 .871585 .871849	4.40 4.40 4.40 4.40 4.40 4.40 4.40 4.40	10.130527 .130263 .129999 .129735 .129471 .129207 .128943 .128679 .128415 .128151	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.776259 .776429 .776598 .776768 .776937 .7777106 .777275 .777444 .777613 .777781	2.83 2.82 2.83 2.82 2.82 2.82 2.82 2.82	9,904147 .904053 .903959 .903864 .903770 .903676 .903581 .903487 .903392 .903298	1.57 1.57 1.58 1.57 1.58 1.57 1.58 1.57 1.58	9.872112 .872376 .872640 .872903 .873167 .873430 .873694 .873957 .874220 .874484	4.40 4.40 4.38 4.40 4.38 4.40 4.38 4.40 4.38	10.127888 .127624 .127360 .127097 .126833 .126570 .126306 .126043 .125780 .125516	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.777950 .778119 .778287 .778455 .778624 .778792 .778960 .779128 .779295 9.779463	2.82 2.80 2.80 2.80 2.80 2.80 2.80 2.80	9.903203 .903108 .903014 .902919 .902824 .902729 .902634 .902539 .902444 9.902349	1.58 1.57 1.58 1.58 1.58 1.58 1.58 1.58	9.874747 .875010 .875273 .875273 .875537 .875800 .876063 .876326 .876589 .876852 9.877114	4.38 4.38 4.40 4.38 4.38 4.38 4.38 4.38 4.37	10.125253 .124990 .124727 .124463 .124200 .123937 .123674 .123411 .123148 10.122886	9 8 7 6 5 4 3 2 1
,	Cosine.	D. 1".	Sine.	D. 1*.	Cotang.	D. 1".	Tang.	,

87°								142°
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.779463 .779631 .779798 .779966 .780133 .780300 .780467 .780634 .780801 .780968 .781134	2.80 2.78 2.80 2.78 2.78 2.78 2.78 2.78 2.78 2.77 2.78	9.902349 .902253 .902158 .902063 .901967 .901872 .901776 .901681 .901585 .901490 .901394	1.60 1.58 1.58 1.60 1.58 1.60 1.58 1.60 1.58 1.60	9.877114 .877377 .877640 .877903 .878165 .878428 .878691 .878953 .879216 .879478 .879741	4.38 4.38 4.38 4.37 4.38 4.37 4.38 4.37 4.38 4.37	10.122886 1122623 1122360 1122397 1121835 1121572 1121309 1121047 1120784 120522 120259	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.781301 .781468 .781634 .781800 .781966 .782132 .782298 .782464 .782630 .782796	2.78 2.77 2.77 2.77 2.77 2.77 2.77 2.77	9.901298 .901202 .901106 .901010 .900914 .900818 .900722 .900626 .900529 .900433	1.60 1.60 1.60 1.60 1.60 1.60 1.60 1.60	9.880003 .880265 .880528 .880790 .881052 .881314 .881577 .881839 .882101 .882363	4.37 4.38 4.37 4.37 4.38 4.37 4.37 4.37 4.37	10.119997 .119735 .119472 .119210 .118948 .118686 .118423 .118,61 .117899 .117637	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.782961 .783127 .783292 .783458 .783623 .783788 .783953 .784118 .784282 .784447	2.77 2.75 2.77 2.75 2.75 2.75 2.75 2.75	9.900337 .900240 .900144 .900047 .899951 .899854 .899660 .899664 .899467	1.62 1.60 1.62 1.60 1.62 1.62 1.62 1.62 1.62	9.882625 .882887 .883148 .883410 .883672 .883934 .884196 .884457 .884719 .884980	4.37 4.35 4.37 4.37 4.37 4.37 4.35 4.37 4.35	10.117375 .117113 .116852 .116590 .116328 .116066 .115804 .115543 .115281 .115020	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.784612 .784776 .784941 .785105 .785269 .785433 .785597 .785761 .785925 .786089	2.13 2.15 2.15 2.17 2.17 2.17 2.17 2.17 2.17 2.17 2.17	9.899370 .899273 .899176 .899078 .898981 .898884 .898787 .898689 .898592 .898494	1.62 1.62 1.63 1.62 1.62 1.62 1.63 1.62 1.63	9.885242 .885504 .885765 .886026 .886288 .886549 .886811 .887072 .887333 .887594	4.37 4.35 4.35 4.37 4.35 4.37 4.35 4.35 4.35 4.35	10.114758 .114496 .114235 .118974 .118712 .118451 .118189 .112928 .112667 .112406	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.786259 .786416 .786579 .786742 .786906 .787069 .787232 .787395 .787557 .787720	2.73 2.72 2.72 2.72 2.72 2.72 2.72 2.72	9.898397 .898290 .898202 .898104 .898006 .897908 .897810 .897712 .897614 .897516	1.63 1.62 1.63 1.63 1.63 1.63 1.63 1.63 1.63	9.887855 .888116 .888378 .888639 .888900 .889161 .889421 .859682 .889943 .890204	4.35 4.37 4.35 4.35 4.35 4.35 4.35 4.35 4.35 4.35	10.112145 .111884 .111622 .111361 .111100 .110839 .110579 .110318 .110057 .109796	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.787883 .788045 .788208 .788370 .788532 .788694 .78856 .789018 .789180 9.789342	2.70 2.70 2.70 2.70 2.70 2.70 2.70 2.70	9.897418 .897320 .897222 .897123 .897025 .896926 .896828 .896729 .896631 9.896532	1.63 1.63 1.63 1.65 1.63 1.65 1.63 1.65 1.63	9.890465 .890725 .890986 .891247 .891507 .891768 .892028 .892289 .892549 9.892810	4.33 4.35 4.35 4.35 4.35 4.35 4.35 4.33 4.35 4.35	10.109535 .109275 .109014 .108753 .108493 .108232 .107972 .107711 .107451 10.107190	9 8 7 6 5 4 3 2 1 0
,	Cosine.	D 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	7

								141°
/	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.789342 .789504 .789665, .789827 .789988 .790149 .790310 .790471 .790632 .790793 .790954	2.70 2.68 2.70 2.68 2.68 2.68 2.68 2.68 2.68 2.68 2.68	9.896532 .896433 .896335 .896336 .896137 .896038 .895939 .895840 .895741 .895641	1.65 1.63 1.65 1.65 1.65 1.65 1.65 1.65 1.67 1.67	9.892810 .893070 .893331 .893591 .893851 .894111 .894372 .894632 .894892 .895152 .895412	4.33 4.35 4.33 4.33 4.33 4.33 4.33 4.33	10.107190 .106930 .106669 .106409 .10589 .105628 .105368 .105108 .104848 .104588	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.791115 .791275 .791436 .791596 .791757 .791917 .792077 .792237 .792397 .792557	2.67 2.68 2.67 2.68 2.67 2.67 2.67 2.67 2.67 2.67	9.895443 .895343 .895244 .895145 .895045 .894945 .894846 .894746 .894646 .894546	1.67 1.65 1.65 1.67 1.67 1.67 1.67 1.67 1.67	9.895672 .895932 .896192 .896452 .896712 .89671 .897231 .897491 .897751 .898010	4.33 4.33 4.33 4.33 4.33 4.33 4.33 4.33	10.104328 .104068 .103808 .103548 .103029 .102769 .102509 .102249 .101990	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.792716 .792876 .793035 .793195 .793514 .793514 .793673 .793832 .793991 .794150	2.67 2.65 2.67 2.65 2.67 2.65 2.65 2.65 2.65 2.65	9.894446 .894346 .894246 .894146 .894046 .893946 .893846 .893745 .893645 .893544	1.67 1.67 1.67 1.67 1.67 1.67 1.68 1.67 1.68	9.898270 .898530 .898789 .899049 .899308 .899568 .899827 .900087 .900346 .900605	4.33 4.32 4.33 4.33 4.32 4.33 4.32 4.32	10.101730 .101470 .101211 .100951 .100692 .100432 .100173 .099913 .099654 .099395	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.794308 .794467 .794626 .794784 .794942 .795101 .795259 .795417 .795575 .795733	2.65 2.65 2.63 2.63 2.63 2.63 2.63 2.63 2.63 2.63	9.893444 .893343 .893243 .893142 .893041 .892940 .892839 .892739 .892638 .892536	1.68 1.67 1.68 1.68 1.68 1.68 1.67 1.68 1.70	9.900864 .901124 .901383 .901642 .901901 .902160 .902420 .902679 .902938 .903197	4.33 4.32 4.32 4.32 4.32 4.33 4.32 4.32	10.099136 .098876 .098617 .098358 .098099 .097840 .097580 .097321 .097062 .096803	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.795891 .796049 .796206 .796364 .796521 .796679 .796836 .796993 .797150 .797307	2.63 2.62 2.63 2.62 2.63 2.62 2.62 2.62	9.892435 .892334 .892233 .892132 .892030 .891929 .891827 .891726 .891624 .891523	1.68 1.68 1.68 1.70 1.68 1.70 1.68 1.70 1.68	9.903456 .903714 .903973 .904232 .904491 .904750 .905008 .905267 .905526 .905785	4.30 4.32 4.32 4.32 4.30 4.32 4.32 4.32 4.32 4.30	10.096544 .096286 .096027 .095768 .095509 .095250 .094992 .094733 .094474 .094215	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.797464 .797621 .797777 .797934 .798091 .798247 .798403 .798560 .798716 9.798872	2.62 2.60 2.62 2.62 2.60 2.60 2.60 2.60	9.891421 .891319 .891217 .891115 .891013 .890911 .890809 .890707 .890605 9.890503	1.70 1.70 1.70 1.70 1.70 1.70 1.70 1.70	9.906043 .906302 .906560 .906819 .907077 .907336 .907594 .907853 .908111 9.908369	4.32 4.30 4.32 4.30 4.32 4.30 4.32 4.30 4.32 4.30	10.093957 .093698 .093440 .093181 .092923 .092664 .092406 .092147 .091889 10.091631	9 8 7 6 5 4 3 2 1 0
/	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	,

Sine, D. 1', Cosine, D. 1', Tang, D. 1', Cotang, C	00								110
1 7,99028 2,00 8,9029 1,72 9,90828 4,33 0,91372 59 3 7,9939 2,58 8,90195 1,72 9,90144 4,30 0,90536 57 4 7,9945 2,60 8,9003 1,72 9,90144 4,30 0,90536 57 5 7,99651 2,60 8,9003 1,72 9,90660 4,30 0,90340 55 6 7,9986 2,58 8,8985 1,70 9,90618 4,30 0,90340 55 8 8,80117 2,58 8,8955 1,72 9,91047 4,30 0,89833 53 8 8,80117 2,58 8,8852 1,72 9,91043 4,30 0,89835 53 8 8,80117 2,58 8,8852 1,72 9,91636 4,30 0,89807 51 10 8,00272 2,58 8,88157 1,70 9,91636 4,30 0,89807 51 11 9,80052 2,58 8,8917 1,70 9,91603 4,30 0,89807 51 12 8,00737 2,58 8,8916 1,72 9,91129 1,430 1,08879 1,49 12 8,00737 2,58 8,8916 1,72 9,91129 1,430 1,08879 1,49 14 8,01047 2,58 8,8916 1,72 9,91129 1,430 1,08879 1,49 15 8,0120 2,57 8,88961 1,72 9,91290 4,30 0,88523 45 16 8,0136 2,58 8,88153 1,72 9,91298 4,28 0,88018 46 15 8,0120 2,57 8,88961 1,72 9,1125 4,23 0,88018 46 16 8,0136 2,58 8,88153 1,72 9,1129 4,30 0,88770 45 16 8,0137 2,58 8,88553 1,72 9,1129 8,4 30 0,8770 45 17 8,01511 2,58 8,88553 1,72 9,1129 8,4 30 0,8770 45 18 8,01615 2,57 8,88561 1,73 9,1357 4,30 0,87720 45 19 8,01819 2,57 8,88561 1,73 9,1357 4,30 0,8724 43 19 8,01819 2,57 8,88561 1,73 9,1357 4,30 0,88724 43 20 8,01973 2,58 8,8815 1,73 9,1357 4,30 0,86721 40 20 8,01973 2,58 8,8841 1,73 9,13529 4,30 0,86724 43 20 8,01973 2,55 8,88513 1,72 9,13570 4,30 0,86729 41 21 9,802188 2,57 8,88581 1,73 9,13529 4,30 0,86729 41 22 8,00282 2,57 8,88581 1,73 9,13529 4,30 0,86739 42 23 8,02366 2,55 8,88675 1,73 9,13571 4,28 0,86868 37 24 8,02589 2,57 8,88581 1,73 9,13529 4,30 0,86739 42 25 8,02282 2,57 8,88581 1,73 9,13529 4,30 0,86729 44 26 8,02074 2,55 8,88675 1,73 9,13571 4,28 0,86883 32 27 8,02367 2,55 8,88675 1,73 9,14644 4,30 0,86368 39 28 8,02364 2,57 8,88581 1,73 9,13579 4,30 0,86729 44 29 8,02367 2,55 8,88675 1,73 9,14644 4,30 0,86368 39 29 8,02367 2,57 8,88581 1,73 9,13529 4,30 0,86729 44 29 8,02569 2,55 8,88675 1,73 9,14664 4,30 0,86368 39 30 8,03511 2,57 8,88581 1,73 9,13529 4,30 0,86879 39 31 9,803664 2,55 8,88675 1,73 9,14664 4,28 0,08333 29 32 8,03867 2,55 8,88675 1,73 9,14664 4,28 0,08333 29 34 8	1	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	′
11 9,800582 2,58 8,88971 1,72 9,911407 4,30 10,688791 49 13 8,00892 2,58 8,89168 1,72 9,911467 4,30 ,088733 48 14 8,01047 2,58 8,89064 1,73 9,911292 4,30 ,088736 41 15 8,01201 2,58 8,88061 1,72 9,91249 4,30 ,087760 45 16 8,01356 2,58 8,88858 1,72 9,12498 4,30 ,087760 45 17 8,01511 2,57 8,88858 1,72 9,12498 4,30 ,087302 44 19 8,01519 2,57 8,88858 1,72 9,13271 4,28 ,086986 42 21 9,802128 2,57 8,88821 1,73 9,14372 4,30 ,085411 42 22 8,02282 2,57 8,88821 1,73 9,14362 4,30 ,08546 32	1 2 3 4 5 6 7 8 9	.799028 .799184 .799339 .799495 .799651 .799806 .799962 .800117 .800272	2.60 2.58 2.60 2.60 2.58 2.60 2.58 2.58 2.58	.890400 .890298 .890195 .890093 .889990 .889888 .889785 .889682 .889579	1.70 1.72 1.70 1.72 1.70 1.72 1.72 1.72 1.72	.908628 .908886 .909144 .909402 .90960 .909918 .910177 .910435 .916693	4.30 4.30 4.30 4.30 4.30 4.32 4.30 4.30 4.30	.091372 .091114 .090856 .090598 .090340 .090082 .089823 .089565 .089307	59 58 57 56 55 54 53 52 51
21 9.802128 2.57 8888311 1.73 9.913787 4.28 10.086213 38 23 8.02436 2.55 888134 1.73 9.914044 4.30 0.85956 38 24 8.02589 2.57 888703 1.73 9.914500 4.28 0.085400 36 25 8.02743 2.57 887926 1.73 9.915075 4.30 0.085183 35 26 8.03804 2.57 887926 1.73 9.915075 4.28 0.084668 33 28 8.03204 2.57 887510 1.73 9.915302 4.28 0.084668 33 29 8.03357 2.57 887610 1.73 9.916104 4.28 0.084668 33 30 8.03511 2.55 887406 1.73 9.916362 4.28 0.084153 31 31 9.803664 2.55 887406 1.73 9.916104 4.30 0.083638 2.2 <t< td=""><td>12 13 14 15 16 17 18 19</td><td>.800737 .800892 .801047 .801201 .801356 .801511 .801665 .801819</td><td>2.58 2.58 2.58 2.57 2.58 2.58 2.57 2.57 2.57</td><td>.889271 .889168 .889064 .888961 .88858 .888755 .888651 .888548</td><td>1.72 1.72 1.73 1.72 1.72 1.72 1.73 1.73 1.73</td><td>.911467 .911725 .911982 .912240 .912498 .912756 .913014 .913271</td><td>4.30 4.30 4.28 4.30 4.30 4.30 4.30 4.30 4.30</td><td>.088533 .088275 .088018 .087760 .087502 .087244 .086986 .086729</td><td>48 47 46 45 44 43 42 41</td></t<>	12 13 14 15 16 17 18 19	.800737 .800892 .801047 .801201 .801356 .801511 .801665 .801819	2.58 2.58 2.58 2.57 2.58 2.58 2.57 2.57 2.57	.889271 .889168 .889064 .888961 .88858 .888755 .888651 .888548	1.72 1.72 1.73 1.72 1.72 1.72 1.73 1.73 1.73	.911467 .911725 .911982 .912240 .912498 .912756 .913014 .913271	4.30 4.30 4.28 4.30 4.30 4.30 4.30 4.30 4.30	.088533 .088275 .088018 .087760 .087502 .087244 .086986 .086729	48 47 46 45 44 43 42 41
31 9.803664 2.55 9.887302 1.73 9.916362 4.28 10.083638 28 28 33 803970 2.55 887938 1.75 9.16517 4.28 0.83381 28 33 803970 2.55 886089 1.73 9.17391 4.28 0.83381 27 38 38 804276 2.55 886685 1.73 9.17391 4.28 0.82362 27 36 80428 2.55 886685 1.73 9.17391 4.28 0.82362 25 37 804581 2.55 886676 1.73 9.17648 4.28 0.82352 24 4.28 0.83383 28 4.28 0.83381 28 4.28 0.83381 27 4.28 0.83381 28 4.28 0	22 23 24 25 26 27 28 29	.802282 .802436 .802589 .802743 .802897 .803050 .803204 .803357	2.57 2.57 2.55 2.57 2.57 2.57 2.55 2.57 2.55 2.57	.888237 .888134 .888030 .887926 .887822 .887718 .887614 .887510	1.73 1.72 1.73 1.73 1.73 1.73 1.73 1.73	.914044 .914302 .914560 .914817 .915075 .915332 .915590 .915847	4.28 4.30 4.28 4.30 4.28 4.30 4.28 4.30 4.28	.085956 .085698 .085440 .085183 .084925 .084668 .084410	38 37 36 35 34 33 32 31
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	32 33 34 35 36 37 38 39	.803817 .803970 .804123 .804276 .804428 .804581 .804734 .804886	2.55 2.55 2.55 2.55 2.55 2.55 2.55 2.55	.887198 .887093 .886989 .886885 .886780 .886676 .886571	1.73 1.75 1.73 1.73 1.73 1.75 1.75 1.75 1.75	.916619 .916877 .917134 .917391 .917648 .917906 .918163 .918420	4.28 4.30 4.28 4.28 4.28 4.30 4.28 4.28 4.28	.083381 .083123 .082866 .082609 .082352 .082094 .081837 .081580	28 27 26 25 24 23 22 21
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	42 43 44 45 46 47 48 49 50	.805343 .805495 .805647 .805799 .805951 .806103 .806254 .806406 .806557	2.53 2.53 2.53 2.53 2.53 2.53 2.53 2.52 2.53 2.52	.886152 .886047 .885942 .885837 .885732 .885627 .885522 .885416 .885311	1.75 1.75 1.75 1.75 1.75 1.75 1.75 1.77	.919191 .919448 .919705 .919962 .920219 .920476 .920733 .920990 .921247	4.28 4.28 4.28 4.28 4.28 4.28 4.28 4.28	.080809 .080552 .080295 .080038 .079781 .079524 .079267 .079010 .078753	18 17 16 15 14 13 12 11
Cosine. D. 1". Sine. D. 1". Cotang. D. 1'. Tang.	52 53 54 55 56 57 58 59	.806860 .807011 .807163 .807314 .807465 .807615 .807766 .807917	2.52 2.52 2.53 2.52 2.52 2.50 2.52 2.52	.885100 .884994 .884889 .884783 .884677 .884572 .884466 .884360	1.75 1.77 1.75 1.77 1.77 1.77 1.75 1.77	.921760 .922017 .922274 .922530 .922787 .923044 .923300 .923557	4.28 4.28 4.28 4.27 4.28 4.27 4.28 4.27 4.28	.078240 .077983 .077726 .077470 .077213 .076956 .076700	8 7 6 5 4 3 2
		Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1'.	Tang.	,

40°								139°
,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.808067 808218 808368 808519 808669 808819 808969 809119 809269 809419 809569	2.52 2.50 2.52 2.50 2.50 2.50 2.50 2.50	9.884254 .884148 .884042 .883936 .883829 .883723 .883617 .883510 .883404 .883297 .883191	1.77 1.77 1.77 1.78 1.77 1.78 1.77 1.78 1.77	9.923814 .924070 .924327 .924583 .924840 .925096 .925352 .925609 .925865 .926122 .926378	4.27 4.28 4.27 4.28 4.27 4.27 4.28 4.27 4.28 4.27 4.28 4.27	10.076186 .075930 .075673 .075417 .075160 .074904 .074648 .074391 .074135 .073878 .073622	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 18 19 20	9.809718 .809868 .810017 .810167 .810316 .810465 .810614 .810763 .810912 .811061	2.50 2.48 2.50 2.48 2.48 2.48 2.48 2.48 2.48 2.48	9.883084 .882977 .882871 .882764 .882657 .882550 .882443 .882336 .882229 .882121	1.78 1.77 1.78 1.78 1.78 1.78 1.78 1.78	9.926634 .926890 .927147 .927403 .927659 .927915 .928171 .928427 .928684 .928940	4.27 4.28 4.27 4.27 4.27 4.27 4.27 4.27 4.27 4.27	10.073366 .073110 .072853 .072597 .072341 .072085 .071829 .071573 .071316 .071060	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.811210 .811358 .811507 .811655 .811804 .811952 .812100 .812248 .812396 .812544	2.47 2.48 2.47 2.48 2.47 2.47 2.47 2.47 2.47 2.47	9.882014 .881907 .881799 .881692 .881584 .881477 .881369 .881261 .881153 .881046	1.78 1.80 1.78 1.80 1.78 1.80 1.80 1.78 1.80	9.929196 .929452 .929708 .929964 .930220 .930475 .930731 .930987 .931243 .931499	4.27 4.27 4.27 4.27 4.25 4.27 4.27 4.27 4.27 4.27 4.27	10.070804 .070548 .070292 .070036 .069780 .069525 .069269 .069013 .068757 .068501	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.812692 .812840 .812988 .813135 .813283 .813430 .813578 .813725 .813872 .814019	2.47 2.47 2.45 2.45 2.47 2.45 2.47 2.45 2.45 2.45 2.45	9.880938 .880830 .880722 .880613 .880505 .880397 .880289 .880180 .880072 .879963	1.80 1.80 1.82 1.80 1.80 1.80 1.82 1.80 1.82 1.80	9.931755 .932010 .932266 .932522 .932778 .933033 .933289 .933545 .933800 .934056	4.25 4.27 4.27 4.27 4.27 4.27 4.27 4.27 4.27	10.068245 .067990 .067734 .067478 .067222 .066967 .066711 .066455 .066200 .065944	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.814166 .814313 .814460 .814607 .814753 .814900 .815046 .815193 .815339 .815485	2.45 2.45 2.45 2.43 2.45 2.43 2.45 2.43 2.43 2.43	9.879855 .879746 .879637 .879529 .879420 .879311 .879202 .879093 .878984 .878875	1.82 1.80 1.80 1.82 1.82 1.82 1.82 1.82 1.82	9.934311 .934567 .934822 .935078 .935333 .935589 .935844 .936100 .936355 .936611	4.27 4.25 4.27 4.25 4.27 4.25 4.27 4.25 4.27 4.25	10.065689 .065433 .065178 .064922 .064667 .064411 .064156 .063900 .063645 .063389	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.815632 .815778 .815924 .816069 .816215 .816361 .816507 .816652 .816798 9.816943	2.43 2.43 2.42 2.43 2.43 2.43 2.43 2.42 2.43 2.42 2.43	9.878766 .878656 .878547 .878438 .878328 .878219 .878109 .877999 .877890 9.877780	1.83 1.82 1.82 1.83 1.82 1.83 1.83 1.83	9.936866 .937121 .937377 .937632 .937887 .938142 .938398 .938653 .938908 9.939163	4.25 4.27 4.25 4.25 4.25 4.25 4.25 4.25 4.25	10.063134 .062879 .062623 .062368 .062113 .061858 .061602 .061347 .061092 10.060837	9 8 7 6 5 4 3 2 1
,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1'.	Tang.	, I

Sine D. 1' Cosine D. 1' Tang D. 1' Cotang /	41°		IADD	11 A. D	OGARI	111110	114 150,		199
1	,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	'
11	1 2 3 4 5 6 7 8	.817088 .817233 .817379 .817524 .817668 .817813 .817958 .818103 .818247	2.42 2.43 2.42 2.40 2.42 2.42 2.42 2.42 2.40 2.42	.877670 .877560 .877450 .877340 .877340 .877120 .877010 .876899 .876789	1.83 1.83 1.83 1.83 1.83 1.83 1.85 1.85	.939418 .939673 .939928 .940183 .940439 .940694 .941949 .941204 .941459	4.25 4.25 4.27 4.27 4.25 4.25 4.25 4.25 4.25	.060582 .060327 .060072 .059817 .059561 .059306 .059051 .058796 .058541	59 58 57 56 55 54 53 52 51
52 .820120 2.40 .875348 1.55 .944771 4.25 .055229 83 23 .820263 2.38 .875237 1.85 .915026 4.25 .054974 83 24 .820406 2.40 .875126 1.87 .945281 4.25 .054974 38 26 .820500 2.38 .874903 1.87 .945535 4.23 .054465 33 27 .820836 2.38 .874903 1.87 .945790 4.25 .054410 34 28 .820979 2.38 .874680 1.85 .946045 4.25 .053761 32 29 .821120 2.38 .874588 1.87 .946584 4.25 .053466 31 30 .821265 2.38 .87458 1.87 .946808 4.23 .05346 31 31 9.821407 2.38 .874321 1.87 .947608 4.23 .052882 28 <td< td=""><td>13 13 14 15 16 17 18 19</td><td>.818681 .818825 .818969 .819113 .819257 .819401 .819545 .819689</td><td>2.42 2.40 2.40 2.40 2.40 2.40 2.40 2.40</td><td>.876457 .876347 .876236 .876125 .876014 .875904 .875793 .875682</td><td>1.85 1.83 1.85 1.85 1.85 1.83 1.85 1.85</td><td>.942223 .942478 .942733 .942988 .943243 .943498 .943752 .944007</td><td>4.25 4.25 4.25 4.25 4.25 4.25 4.25 4.25</td><td>.057777 .057522 .057267 .057012 .056757 .056502 .056248 .055993 .055738</td><td>48 47 46 45 44 43 42 41 40</td></td<>	13 13 14 15 16 17 18 19	.818681 .818825 .818969 .819113 .819257 .819401 .819545 .819689	2.42 2.40 2.40 2.40 2.40 2.40 2.40 2.40	.876457 .876347 .876236 .876125 .876014 .875904 .875793 .875682	1.85 1.83 1.85 1.85 1.85 1.83 1.85 1.85	.942223 .942478 .942733 .942988 .943243 .943498 .943752 .944007	4.25 4.25 4.25 4.25 4.25 4.25 4.25 4.25	.057777 .057522 .057267 .057012 .056757 .056502 .056248 .055993 .055738	48 47 46 45 44 43 42 41 40
31 9.821407 2.38 9.874344 1.87 9.917063 4.25 .052682 28 32 .821550 2.38 .874232 1.85 .947318 4.25 .052682 28 33 .821693 2.37 .874091 1.87 .947372 4.25 .052428 27 34 .821835 2.37 .874090 1.87 .947872 4.23 .052173 26 35 .821977 2.38 .873846 1.87 .948801 4.23 .051605 24 36 .822102 2.37 .873662 1.87 .948305 4.25 .05140 23 38 .822404 2.37 .873484 1.87 .94844 4.23 .051605 24 40 .822688 2.37 .873335 1.87 .949808 4.23 .0501156 22 41 9.822890 2.37 .873323 1.88 .949608 4.23 .050047 20	22 23 24 25 26 27 28 29	.820120 .820263 .820406 .820550 .820693 .820836 .820979 .821122	2.40 2.38 2.38 2.40 2.38 2.38 2.38 2.38 2.38 2.38	.875348 .875237 .875126 .875014 .874903 .874791 .874680 .874568	1.85 1.85 1.85 1.87 1.87 1.87 1.85 1.87 1.87	.944771 .945026 .945281 .945535 .945790 .946045 .946299 .946554	4.23 4.25 4.25 4.23 4.25 4.25 4.23 4.25 4.23	.055229 .054974 .054719 .054465 .054210 .053955 .053701 .053446	\$37 36 35 34 33 32 31
41 9.822830 2.37 8.73223 1.88 9.949608 4.23 10.050392 18 42 822972 2.37 8.73110 1.87 9.949602 4.23 .050138 18 43 823114 2.35 8.72898 1.88 .950116 4.25 .049884 17 44 823255 2.37 872772 1.88 .950021 4.23 .049629 16 46 823539 2.37 872659 1.88 .950625 4.23 .049629 16 47 823680 2.35 .872547 1.88 .950879 4.23 .049875 15 48 823963 2.37 .872639 1.88 .951888 4.23 .04867 13 49 .823963 2.35 .872341 1.88 .951898 4.23 .04867 12 49 .823968 2.35 .872321 1.88 .951642 4.23 .048812 12 50<	32 33 34 35 36 37 38 39	.821550 .821693 .821835 .821977 .822120 .822262 .822404 .822546	2.38 2.38 2.37 2.37 2.38 2.37 2.37 2.37 2.37	.874232 .874121 .874009 .873896 .873784 .873672 .873560 .873448	1.87 1.85 1.87 1.88 1.87 1.87 1.87 1.87	.947318 .947572 .947827 .948081 .948335 .948590 .948844 .949099	4.25 4.23 4.25 4.23 4.23 4.25 4.23 4.25 4.23	.052682 .052428 .052173 .051919 .051665 .051410 .051156 .050901	28 27 26 25 24 23 22 21
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	42 43 44 45 46 47 48 49	822972 .823114 .823255 .823397 .823539 .823680 .823821 .823963	2.37 2.37 2.35 2.37 2.37 2.35 2.35 2.35 2.35	.873110 .872998 .872885 .872772 .872659 .872547 .872434 .872321	1.88 1.87 1.88 1.88 1.88 1.87 1.88 1.88	.949862 .950116 .950371 .950625 .950879 .951133 .951388 .951642	4.23 4.23 4.25 4.23 4.23 4.23 4.23 4.25 4.28 4.28	.050138 .049884 .049629 .049375 .049121 .048867 .048612 .048358	18 17 16 15 14 13 12 11
Cosine. D. 1". Sine. D. 1". Cotang. D. 1". Tang.	52 53 54 55 56 57 58 59	.824386 .824527 .824668 .824808 .824949 .825090 .825230 .825371	2.35 2.35 2.35 2.33 2.35 2.35 2.35 2.33	.871981 .871868 .871755 .871641 .871528 .871414 .871301 .871187	1.90 1.88 1.88 1.90 1.88 1.90 1.88 1.90	.952405 .952659 .952913 .953167 .953421 .953675 .953929 .954183	4.25 4.23 4.23 4.23 4.23 4.23 4.23 4.23	.047595 .047341 .047087 .046833 .046579 .046325 .046071 .045817	8 7 6 5 4 3 2
	,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	1 '

420								137*
,	Sine.	D. 1*.	Cosine.	D. 1'.	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.825511 .825651 .825791 .825931 .826071 .826311 .826351 .826491 .826631 .826770 .826910	2.83 2.83 2.83 2.83 2.83 2.83 2.83 2.83	9.871073 .870960 .870846 .870732 .870618 .870504 .870390 .870276 .870161 .870047 .869933	1.88 1.90 1.90 1.90 1.90 1.90 1.90 1.92 1.90 1.90	9.954437 .954691 .954946 .955200 .955454 .955708 .955961 .956215 .956469 .956723 .956977	4.23 4.25 4.23 4.23 4.23 4.23 4.23 4.23 4.23 4.23	10.045563 .045309 .045054 .044800 .044546 .044292 .044039 .043785 .043531 .043277 .043023	60 59 58 57 56 55 54 53 52 51 50
11 12 13 14 15 16 17 13 19 20	9.827049 .827189 .827328 .827467 .827606 .827745 .827884 .828023 .828162 .828301	2.33 2.32 2.32 2.32 2.32 2.32 2.32 2.32	9.869818 .869704 .869589 .869474 .869360 .869245 .869130 .869015 .868900 .868785	1.90 1.92 1.92 1.90 1.92 1.92 1.92 1.92 1.92 1.92	9.957231 .957485 .957739 .957993 .958247 .958500 .958754 .959008 .959262 .959516	4.23 4.23 4.23 4.22 4.22 4.23 4.23 4.23	10.042769 .042515 .042261 .042007 .041753 .041500 .041246 .040992 .040738 .040484	49 48 47 46 45 41 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.828439 .828578 .828716 .828855 .828993 .829131 .829269 .829407 .829545 .829683	2.32 2.30 2.32 2.30 2.30 2.30 2.30 2.30	9.868670 .868555 .868440 .868324 .868209 .868093 .867978 .867862 .867747 .867631	1.92 1.92 1.93 1.92 1.93 1.92 1.93 1.92 1.93	9.959769 .960023 .960277 .960530 .960784 .961038 .961292 .961545 .961799 .962052	4.23 4.23 4.22 4.23 4.23 4.23 4.22 4.23 4.22 4.23 4.22 4.23	10.040231 .039977 .039723 .039470 .039216 .038962 .038708 .038455 .038201 .037948	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.829821 .829959 .830097 .830234 .830372 .830509 .830646 .830784 .830921 .831058	2.30 2.30 2.28 2.28 2.28 2.28 2.28 2.28 2.28	9.867515 .867399 .867283 .867167 .867051 .866935 .866819 .866703 .866586 .866470	1.93 1.93 1.93 1.93 1.93 1.93 1.95 1.95	9.962306 .962560 .962813 .963067 .963320 .903574 .963828 .964081 .964335 .964588	4.23 4.23 4.23 4.23 4.23 4.23 4.23 4.22 4.23 4.22 4.23	10.037694 .037440 .037187 .036933 .036680 .036426 .036172 .035919 .035665 .035412	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.831195 .831332 .831469 .831606 .831742 .831879 .832015 .832152 .832288 .832425	2.28 2.28 2.27 2.28 2.27 2.28 2.27 2.28 2.27 2.28	9.866353 .866237 .866120 .866004 .865887 .865770 .865653 .865536 .865419 .865302	1.93 1.95 1.93 1.95 1.95 1.95 1.95 1.95 1.95	9.964842 .965095 .965349 .965602 .965855 .966109 .966362 .966616 .966869 .967123	4.22 4.23 4.22 4.23 4.23 4.22 4.23 4.22 4.23 4.22 4.23	10.035158 .034905 .034651 .034398 .034145 .033891 .033638 .033384 .033131 .032877	19 18 17 16 15 14 13 12 11
51 52 53 54 55 56 57 58 59 60	9 · 832561	2.27 2.27 2.27 2.27 2.27 2.27 2.27 2.25 2.27 2.25	9.865185 .865068 .864950 .864833 .864716 .864598 .864481 .864363 .864245 9.864127	1.95 1.97 1.95 1.95 1.95 1.97 1.97 1.97	9.967376 .967629 .967883 .968136 .968389 .968643 .968896 .969149 .969403 9.969656	4.22 4.23 4.22 4.22 4.23 4.22 4.22 4.22	10.032624 .032371 .032117 .031864 .031611 .031357 .031104 .030851 .030597 10.030344	9 8 7 6 5 4 3 2 1 0
,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	′

Sine D. 1' Cosine D. 1' Tang D. 1' Cotang /	43°		TABL	E X.—L	OGARI.	inmic s	INES,		136°
2 8,31054 2.25 803992 1.97 970602 4.22 0.30091 59 2 8,31054 2.25 803952 1.97 970602 4.22 0.20383 56 3 8,31189 2.25 803538 1.97 970602 4.22 0.20383 56 6 8,31505 2.25 80310 1.96 970602 4.22 0.20383 56 6 8,31505 2.25 80310 1.96 971075 4.22 0.20383 56 6 8,31505 2.25 80310 1.97 970602 4.22 0.20383 56 6 8,31505 2.25 80310 1.97 970602 4.22 0.20807 55 8 8,83160 2.25 80310 1.97 971082 4.22 0.28065 51 10 8,3160 2.23 863064 1.93 971055 4.22 0.28065 51 10 8,33269 2.23 862946 1.98 971285 4.22 0.28065 51 11 9,833269 2.23 862706 1.98 972948 4.22 0.27559 49 12 8,35403 2.25 863153 1.97 972495 4.22 0.27559 49 13 8,35558 2.25 86358 1.97 972948 4.22 0.27559 49 14 8,35672 2.23 862234 1.98 973201 4.22 0.26759 46 15 8,35907 2.25 86336 1.97 973454 4.22 0.26759 46 16 8,33941 2.23 862234 1.98 973707 4.22 0.26566 45 16 8,33941 2.23 862234 1.98 973707 4.22 0.26566 45 16 8,33941 2.23 862234 1.98 973707 4.22 0.26566 45 17 8,36075 2.23 862151 1.98 973490 4.22 0.26556 45 18 8,36209 2.23 861056 1.93 973490 4.22 0.26556 45 19 8,83613 2.23 861057 1.98 973490 4.22 0.26556 45 19 8,83613 2.23 861651 1.98 973470 4.22 0.26556 45 19 8,83614 2.23 861651 1.98 973490 4.22 0.26556 45 22 8,83741 2.23 861651 1.98 973490 4.22 0.26556 45 22 8,83742 2.23 861651 1.98 973490 4.22 0.26556 45 23 8,83675 2.23 861658 1.98 973490 4.22 0.26556 45 24 8,87012 2.23 861651 1.98 973490 4.22 0.26556 45 25 8,87146 2.23 861661 1.98 973690 4.22 0.26560 43 25 8,83751 2.22 861650 2.00 975750 4.22 0.26560 33 26 8,83751 2.23 861651 1.98 975266 4.22 0.26576 34 26 8,83729 2.23 861661 1.98 975266 4.22 0.26576 34 27 8,83741 2.23 861651 1.98 975266 4.22 0.26576 34 28 8,83750 2.23 861661 1.98 975260 4.22 0.26560 33 38 8,8414 2.22 8.66682 2.00 975770 4.22 0.26560 33 38 8,83871 2.22 860682 2.00 975780 4.22 0.26576 35 38 8,83844 2.22 8.66682 2.00 975780 4.22 0.26576 35 38 8,83844 2.22 8.66682 2.00 975780 4.22 0.26769 30 39 8,83940 2.20 8.58869 2.00 975780 4.22 0.20370 30 40 8,83940 2.20 8.58869 2.00 975780 4.22 0.20370 30 41 9,83968 2.20 8.58869 2.00 975780 4.22 0.20173 32 42 8,83040 2.20	,	Sine.	D. 1".	Cosine.	D. 1".	Tang.	D. 1".	Cotang.	,
11 9.835269 2.23 9.862827 1.97 9.72441 4.23 10.027559 49 12 835408 2.25 862500 1.98 9.73493 4.22 0.27559 49 13 8.83538 2.25 862500 1.98 9.73493 4.22 0.27503 48 14 8.835672 2.23 8.62471 1.98 9.73414 4.22 0.26709 46 15 835807 2.23 8.62234 1.98 9.73417 4.22 0.26393 44 17 836075 2.23 8.62234 1.98 9.73407 4.22 0.26233 1.98 18 8.36209 2.23 8.61996 1.98 9.73407 4.22 0.26233 4.19 19 836318 2.23 8.61877 1.98 9.74466 4.22 0.25787 42 20 836477 2.23 8.61519 1.98 9.74466 4.22 0.25587 42 21 9.836611 2.23 9.861539 1.98 9.74466 4.22 0.25580 40 21 9.836611 2.23 8.61519 1.98 9.744720 4.23 0.25280 40 22 836745 2.23 8.61519 1.98 9.75226 4.22 0.025280 40 23 836745 2.23 8.61519 1.98 9.75226 4.22 0.025280 40 24 887012 2.23 8.61519 1.98 9.75226 4.22 0.025280 40 25 887146 2.23 8.68159 1.98 9.75226 4.22 0.025280 40 26 887279 2.23 8.6101 1.98 9.7526 4.22 0.02528 36 27 887412 2.23 8.60802 2.00 9.7538 4.22 0.02528 36 28 887369 2.22 8.60101 1.98 9.75286 4.22 0.02528 36 28 887546 2.23 8.60802 2.00 9.75985 4.22 0.024015 35 29 887679 2.22 8.60682 2.00 9.7641 4.22 0.02528 36 29 887679 2.22 8.60682 2.00 9.76491 4.22 0.02356 32 29 887679 2.22 8.60682 2.00 9.77641 4.22 0.02356 32 29 887679 2.22 8.60682 2.00 9.77644 4.22 0.02356 32 29 887679 2.22 8.60682 2.00 9.77649 4.22 0.02356 32 29 887679 2.22 8.60682 2.00 9.77649 4.22 0.02356 32 29 887679 2.22 8.60682 2.00 9.77644 4.22 0.02356 32 30 887812 2.22 8.60682 2.00 9.77644 4.22 0.02356 32 31 9.887945 2.22 8.60682 2.00 9.77644 4.22 0.02356 32 32 8889678 2.22 8.60682 2.00 9.77644 4.22 0.02356 32 33 888911 2.22 8.60682 2.00 9.77644 4.22 0.02356 32 34 889404 2.20 8.68682 2.00 9.77650 4.22 0.02930 31 35 888712 2.22 8.60682 2.00 9.776997 4.22 0.02930 31 36 888763 2.20 8.68682 2.00 9.77674 4.22 0.02030 31 37 888947 2.22 8.60682 2.00 9.77674 4.22 0.02030 31 38 888914 2.22 8.60682 2.00 9.78690 4.22 0.02030 31 38 888914 2.22 8.60682 2.00 9.78690 4.22 0.02030 31 39 889007 2.22 8.60682 2.00 9.78690 4.22 0.02030 31 30 887812 2.22 8.60682 2.00 9.78690 4.22 0.02030 31 30 887812 2.02 8.60682 2.00 9.78690 4.22 0.02030	1 2 3 4 5 6 7 8 9	.833919 .834054 .834189 .834325 .834460 .834595 .834730 .834865 .834999	2.25 2.25 2.27 2.25 2.25 2.25 2.25 2.25	.864010 .863892 .863774 .863656 .863538 .863419 .863301 .863183 .863064	1.97 1.97 1.97 1.97 1.98 1.97 1.98 1.97	.969909 .970162 .970416 .970669 .970922 .971175 .971429 .971682 .971935	4.22 4.23 4.22 4.22 4.22 4.23 4.23 4.22 4.22	.030091 .029838 .029584 .029331 .029078 .028825 .028571 .028318 .028065	59 58 57 56 55 54 53 52 51
22 .836745 2.22 .861519 1.98 .975226 4.22 .024774 38 24 .837012 2.23 .861280 2.00 .975479 4.22 .024528 36 25 .837146 2.23 .861161 2.00 .975832 4.22 .024368 36 26 .837279 2.22 .861041 2.00 .975835 4.22 .023762 34 27 .837412 2.23 .86082 2.00 .976491 4.22 .02356 32 28 .83756 2.23 .86082 2.00 .976974 4.22 .02356 32 29 .83769 2.22 .860682 2.00 .97750 4.22 .02356 32 31 9.837945 2.22 9.860442 2.00 .977503 4.22 .022474 29 32 8.83676 2.22 .860322 2.00 .977509 4.22 .021738 26 33 </td <td>12 13 14 15 16 17 18 19 20</td> <td>.835403 .835538 .835672 .835807 .835941 .836075 .836209 .836343 .836477</td> <td>2.23 2.25 2.23 2.25 2.23 2.23 2.23 2.23</td> <td>.862709 .862590 .862471 .862353 .862234 .862115 .861996 .861877 .861758</td> <td>1.97 1.98 1.98 1.97 1.98 1.98 1.98 1.98</td> <td>.972695 .972948 .973201 .973454 .973707 .973960 .974213 .974466 .974720</td> <td>4.23 4.22 4.22 4.22 4.22 4.22 4.22 4.22</td> <td>.027305 .027052 .026799 .026546 .026293 .026040 .025787 .025534 .025280</td> <td>48 47 46 45 44 43 42 41 40</td>	12 13 14 15 16 17 18 19 20	.835403 .835538 .835672 .835807 .835941 .836075 .836209 .836343 .836477	2.23 2.25 2.23 2.25 2.23 2.23 2.23 2.23	.862709 .862590 .862471 .862353 .862234 .862115 .861996 .861877 .861758	1.97 1.98 1.98 1.97 1.98 1.98 1.98 1.98	.972695 .972948 .973201 .973454 .973707 .973960 .974213 .974466 .974720	4.23 4.22 4.22 4.22 4.22 4.22 4.22 4.22	.027305 .027052 .026799 .026546 .026293 .026040 .025787 .025534 .025280	48 47 46 45 44 43 42 41 40
31 9.837945 2.22 8.860322 2.00 9.77756 4.22 10.022497 29 32 8.88078 2.22 8.860322 2.00 9.77809 4.22 0.21991 27 34 8.88341 2.22 8.860082 2.00 9.78009 4.22 0.21191 27 35 8.88477 2.22 8.860082 2.00 9.78515 4.22 0.21191 27 36 8.88610 2.22 8.85962 2.00 9.78515 4.22 0.21185 25 37 8.88742 2.20 8.859721 2.02 9.79021 4.22 0.02193 24 38 8.88875 2.22 8.859721 2.02 9.79021 4.22 0.02193 24 39 8.89007 2.20 8.85960 2.00 9.78768 4.22 0.02132 24 40 8.89140 2.20 8.85960 2.00 9.79274 4.22 0.02076 22 41 9.839272 2.0 8.59380 2.00 9.79274 4.22 0.02076 22 42 8.89404 2.20 8.859119 2.02 9.79578 4.22 0.02020 20 41 9.839272 2.0 8.85919 2.00 9.80033 4.22 0.021973 14 42 8.89404 2.20 8.859119 2.02 9.80086 4.20 0.019714 18 43 8.89536 2.20 8.85875 2.02 9.80058 4.22 0.019967 19 44 8.89688 2.20 8.85875 2.02 9.80038 4.22 0.019967 19 45 8.89800 2.20 8.888756 2.02 9.81044 4.22 0.18956 15 46 8.89982 2.20 8.858635 2.02 9.81297 4.22 0.18508 14 47 8.40064 2.20 8.858635 2.02 9.81297 4.22 0.018508 14 48 8.40196 2.20 8.858635 2.02 9.81297 4.22 0.018508 14 48 8.40196 2.20 8.858635 2.02 9.81297 4.22 0.018508 14 48 8.40196 2.20 8.858635 2.02 9.81297 4.22 0.018508 14 49 8.40282 2.18 8.85708 2.02 9.82309 4.22 0.018708 11 50 8.40459 2.18 8.85708 2.02 9.82309 4.22 0.018708 11 51 9.840591 2.18 8.857086 2.03 9.82306 4.22 0.017094 11 52 8.40722 2.18 8.857086 2.03 9.83320 4.22 0.017086 8 53 8.40854 2.20 8.85766 2.03 9.83320 4.22 0.017086 8 55 8.41116 2.18 8.85718 2.03 9.83320 4.22 0.016080 6 55 8.41160 2.18 8.857183 2.03 9.83320 4.22 0.016080 6 55 8.41160 2.18 8.857183 2.03 9.83320 4.22 0.015081 3 58 8.41509 2.18 8.857086 2.03 9.84079 4.22 0.015081 3 58 8.41640 2.18 8.857183 2.03 9.84384 4.20 0.015468 0 58 8.41640 2.18 8.857086 2.03 9.84384 4.20 0.015468 0 59 8.41640 2.18 8.857086 2.03 9.84384 4.20 0.015468 0 59 8.41640 2.18 8.857086 2.03 9.84384 4.20 0.015468 0 50 8.41640 2.18 8.857086 2.03 9.84384 4.20 0.015468 0 50 8.41640 2.18 8.857086 2.03 9.84384 4.20 0.015468 0 50 8.41640 2.18 8.857086 2	22 23 24 25 26 27 28 29	.836745 .836878 .837012 .837146 .837279 .837412 .837546 .837679	2.22 2.23 2.23 2.22 2.22 2.22 2.23 2.23	.861519 .861400 .861280 .861161 .861041 .860922 .860802 .860682	1.98 2.00 1.98 2.00 1.98 2.00 2.00 2.00	.975226 .975479 .975732 .975985 .976238 .976491 .976744 .976997	4.22 4.22 4.22 4.22 4.22 4.22 4.22 4.22	.024774 .024521 .024268 .024015 .023762 .023509 .023256 .023003	38 37 36 35 34 33 32 31 30
41 9.839272 2.20 9.859239 2.00 9.980033 4.22 10.019967 18 42 839404 2.20 859119 2.02 9.80286 4.22 0.019714 18 43 839536 2.20 858988 2.02 980538 4.22 0.019402 17 44 839608 2.20 858577 2.02 981044 4.22 0.019402 17 45 839800 2.20 858635 2.02 981297 4.22 0.018956 15 46 839982 2.20 858635 2.02 981297 4.22 0.018956 15 47 840644 2.20 858514 2.02 981297 4.22 0.018450 13 48 84038 2.18 8588722 2.02 982056 4.22 0.01845 14 49 840328 2.18 858511 2.02 982066 4.22 0.01794 11 50	32 33 34 35 36 37 38 39	.838078 .838211 .838344 .838477 .838610 .838742 .838875 .839007	2.32 2.32 2.32 2.32 2.32 2.32 2.30 2.32 2.30 2.32	.860322 .860202 .860082 .859962 .859842 .859721 .859601 .859480	2.00 2.00 2.00 2.00 2.00 2.02 2.00 2.02 2.00 2.02	.977756 .978009 .978262 .978515 .978768 .979021 .979274 .979527	4.22 4.22 4.22 4.22 4.22 4.22 4.22 4.22	.022244 .021991 .021738 .021485 .021232 .020979 .020726 .020473	28 27 26 25 24 23 22 21
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	42 43 44 45 46 47 48 49	.839404 .839536 .839668 .839800 .839932 .840064 .840196 .840328	2.20 2.20 2.20 2.20 2.20 2.20 2.20 2.20	.859119 .858998 .858877 .858756 .858635 .858393 .858272	2.00 2.02 2.02 2.02 2.02 2.02 2.02 2.02	.980286 .980538 .980791 .981044 .981297 .981550 .981803 .982056	4.22 4.20 4.22 4.22 4.22 4.22 4.22 4.22	.019714 .019462 .019209 .018956 .018703 .018450 .018197 .017944	18 17 16 15 14 13 12 11
' Cosine. D. 1'. Sine. D. 1'. Cotang. D. 1'. Tang. '	52 53 54 55 56 57 58 59	.840722 .840854 .840985 .841116 .841247 .841378 .841509 .841640	2.18 2.20 2.18 2.18 2.18 2.18 2.18 2.18 2.18	.857908 .857786 .857665 .857543 .857422 .857300 .857178 .857056	2.02 2.03 2.02 2.03 2.02 2.03 2.03 2.03	.982814 .983067 .983320 .983573 .983826 .984079 .984332 .984584	4.20 4.22 4.22 4.22 4.22 4.22 4.22 4.22	.017186 .016933 .016680 .016427 .016174 .015921 .015668 .015416	8 7 6 5 4 3 2
	,	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1".	Tang.	,

44.							~~	135
,	Sine.	D. 1".	Cosine.	D. 1*.	Tang.	D. 1".	Cotang.	,
0 1 2 3 4 5 6 7 8 9	9.841771 .841902 .842033 .842163 .842294 .84244 .84255 .842685 .842815 .842946 .843076	2.18 2.18 2.17 2.18 2.17 2.18 2.17 2.18 2.17 2.18 2.17 2.17	9.856934 .856812 .856690 .856568 .856446 .856323 .856201 .856078 .855936 .855833 .855711	2.03 2.03 2.03 2.05 2.05 2.05 2.03 2.05 2.03 2.05 2.03 2.05 2.03	9.984837 .985090 .985343 .985596 .985848 .986101 .986354 .986607 .986860 .987112 .987365	4.22 4.22 4.22 4.20 4.22 4.22 4.22 4.22	10.015163 .014910 .014657 .014404 .014152 .013899 .013646 .013393 .013140 .012888	60 59 58 57 56 55 54 53 52 51
11 12 13 14 15 16 17 18 19 20	9.843206 .843336 .843466 .843595 .843725 .843855 .84384 .844114 .844243 .814372	2.17 2.17 2.15 2.17 2.17 2.17 2.15 2.17 2.15 2.17	9.855588 .855465 .855342 .855219 .855096 .854973 .854850 .854727 .854603 .854480	2.05 2.05 2.05 2.05 2.05 2.05 2.05 2.07 2.05 2.07	9.987618 .987871 .988123 .988376 .988629 .988882 .989134 .989387 .989640 .989893	4.22 4.20 4.22 4.22 4.22 4.20 4.22 4.22	10.012382 .012129 .011877 .011624 .011371 .011118 .010866 .010613 .010360 .010107	49 48 47 46 45 44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	9.844502 .844631 .844760 .844889 .845018 .845147 .845276 .845405 .845533 .845662	2.15 2.15 2.15 2.15 2.15 2.15 2.15 2.15	9.854356 .854233 .854109 .853986 .853862 .853738 .853614 .853490 .853366 .853242	2.05 2.07 2.05 2.07 2.07 2.07 2.07 2.07 2.07 2.07 2.07	9.990145 .990398 .990651 .990903 .991156 .991409 .991662 .991914 .992167 .992420	4.22 4.23 4.20 4.22 4.22 4.22 4.22 4.22 4.20 4.22 4.22	10.009855 .009602 .009349 .009897 .008844 .008591 .00838 .008086 .007833 .007580	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	9.845790 .845919 .846047 .846175 .846304 .846432 .846560 .846688 .846816 .846944	2.15 2.13 2.13 2.15 2.15 2.13 2.13 2.13 2.13 2.13 2.13	9.853118 .852994 .852869 .852745 .852620 .852496 .852371 .852247 .852122 .851997	2.07 2.08 2.07 2.08 2.07 2.08 2.07 2.08 2.07 2.08 2.08 2.08	9.992672 .992925 .993178 .993431 .993683 .993936 .994189 .994441 .994694 .994947	4.22 4.22 4.20 4.20 4.22 4.20 4.20 4.22 4.20 4.22 4.20	10.007328 .007075 .006822 .006569 .006317 .006064 .005811 .005559 .005306 .005053	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	9.847071 .847199 .847327 .847454 .847582 .847709 .847836 .847964 .848091 .848218	2.13 2.13 2.12 2.13 2.12 2.12 2.13 2.12 2.12	9.851872 .851747 .851622 .851497 .851372 .851246 .851121 .850996 .850870 .850745	2.08 2.08 2.08 2.08 2.10 2.08 2.10 2.08 2.10 2.08	9.995199 .995452 .995705 .995957 .996210 .996463 .996715 .996968 .997221 .997473	4.22 4.22 4.20 4.22 4.22 4.20 4.22 4.20 4.22 4.20 4.22	10.004801 .004548 .004295 .004043 .003790 .003537 .003285 .003032 .002779 .002527	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	9.848345 .848472 .848599 .848726 .848852 .848979 .849106 .849232 .849359 9.849485	2 12 2 12 2 12 2 10 2 12 2 12 2 12 2 10 2 12 2 10 2 12 2 10	9.850619 .850493 .850368 .850242 .850116 .849990 .849864 .849738 .849611 9.849485	2.10 2.08 2.10 2.10 2.10 2.10 2.10 2.10 2.10 2.10	9.997726 .997979 .998231 .998484 .998737 .998989 .999242 .999495 .999747 10 000000	4.22 4.20 4.22 4.22 4.20 4.22 4.20 4.22 4.20 4.22	10.002274 .002021 .001769 .001516 .001263 .001011 .000758 .000505 .000253 10.000000	9 8 7 6 5 4 3 2 1
′	Cosine.	D. 1".	Sine.	D. 1".	Cotang.	D. 1'.	Tang.	7









